

NAG Library Routine Document

G13FDF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

G13FDF forecasts the conditional variances, $h_t, t = T + 1, \dots, T + \xi$ from a type II AGARCH(p, q) sequence, where ξ is the forecast horizon and T is the current time (see Engle and Ng (1993)).

2 Specification

```
SUBROUTINE G13FDF(NUM, NT, IP, IQ, THETA, GAMMA, FHT, HT, ET, IFAIL)
INTEGER          NUM, NT, IP, IQ, IFAIL
double precision THETA(IQ+IP+1), GAMMA, FHT(NT), HT(NUM), ET(NUM)
```

3 Description

Assume the GARCH(p, q) process can be represented by:

$$h_t = \alpha_0 + \sum_{i=1}^q \alpha_i (|\epsilon_{t-i}| + \gamma \epsilon_{t-i})^2 + \sum_{i=1}^p \beta_i h_{t-i}, \quad t = 1, 2, \dots, T.$$

where $\epsilon_t | \psi_{t-1} = N(0, h_t)$ or $\epsilon_t | \psi_{t-1} = S_t(df, h_t)$, has been modelled by G13FCF and the estimated conditional variances and residuals are contained in the arrays HT and ET respectively.

G13FDF will then use the last $\max(p, q)$ elements of the arrays HT and ET to estimate the conditional variance forecasts, $h_t | \psi_T$, where $t = T + 1, \dots, T + \xi$ and ξ is the forecast horizon.

4 References

Bollerslev T (1986) Generalised autoregressive conditional heteroskedasticity *Journal of Econometrics* **31** 307–327

Engle R (1982) Autoregressive conditional heteroskedasticity with estimates of the variance of United Kingdom inflation *Econometrica* **50** 987–1008

Engle R and Ng V (1993) Measuring and Testing the Impact of News on Volatility *Journal of Finance* **48** 1749–1777

Hamilton J (1994) *Time Series Analysis* Princeton University Press

5 Parameters

- 1: NUM – INTEGER *Input*
On entry: the number of terms in the arrays HT and ET from the modelled sequence.
Constraint: $\max(IP, IQ) \leq \text{NUM}$.
- 2: NT – INTEGER *Input*
On entry: ξ , the forecast horizon.
Constraint: $\text{NT} > 0$.
- 3: IP – INTEGER *Input*
On entry: the number of coefficients, β_i , for $i = 1, 2, \dots, p$.

Constraints:

$$\begin{aligned}\max(\text{IP}, \text{IQ}) &\leq 20; \\ \text{IP} &\geq 0.\end{aligned}$$

4: IQ – INTEGER *Input*

On entry: the number of coefficients, α_i , for $i = 1, 2, \dots, q$.

Constraints:

$$\begin{aligned}\max(\text{IP}, \text{IQ}) &\leq 20; \\ \text{IQ} &\geq 1.\end{aligned}$$

5: THETA(IQ + IP + 1) – **double precision** array *Input*

On entry: the first element must contain the coefficient α_o and the next IQ elements must contain the coefficients α_i , for $i = 1, 2, \dots, q$. The remaining IP elements must contain the coefficients β_j , for $j = 1, 2, \dots, p$.

6: GAMMA – **double precision** *Input*

On entry: the asymmetry parameter γ for the GARCH(p, q) sequence.

7: FHT(NT) – **double precision** array *Output*

On exit: the forecast values of the conditional variance, h_t , for $t = T + 1, \dots, T + \xi$.

8: HT(NUM) – **double precision** array *Input*

On entry: the sequence of past conditional variances for the GARCH(p, q) process, h_t , for $t = 1, 2, \dots, T$.

9: ET(NUM) – **double precision** array *Input*

On entry: the sequence of past residuals for the GARCH(p, q) process, ϵ_t , for $t = 1, 2, \dots, T$.

10: IFAIL – INTEGER *Input/Output*

On entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this parameter you should refer to Section 3.3 in the Essential Introduction for details.

On exit: IFAIL = 0 unless the routine detects an error (see Section 6).

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, if you are not familiar with this parameter, the recommended value is 0. **When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.**

6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

IFAIL = 1

On entry, NUM < max(IP, IQ),
or IQ < 1,
or IP < 0,
or max(IP, IQ) > 20,
or NT ≤ 0.

7 Accuracy

Not applicable.

8 Further Comments

None.

9 Example

See Section 9 in G13FCF.
