

NAG Library Routine Document

G13DSF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of **bold italicised** terms and other implementation-dependent details.

1 Purpose

G13DSF is a diagnostic checking routine suitable for use after fitting a vector ARMA model to a multivariate time series using G13DDF. The residual cross-correlation matrices are returned along with an estimate of their asymptotic standard errors and correlations. Also, G13DSF calculates the modified Li-McLeod portmanteau statistic and its significance level for testing model adequacy.

2 Specification

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SUBROUTINE G13DSF(K, N, V, KMAX, IP, IQ, M, PAR, PARHLD, QQ, ISHOW, RO,
1      R, RCM, LDRCM, CHI, IDF, SIGLEV, IW, LIW, WORK, LWORK,
2      IFAIL)

  INTEGER      K, N, KMAX, IP, IQ, M, ISHOW, LDRCM, IDF, IW(LIW),
1      LIW, LWORK, IFAIL
  double precision V(KMAX,N), PAR((IP+IQ)*K*K), QQ(KMAX,K), RO(KMAX,K),
1      R(KMAX,KMAX,M), RCM(LDRCM,M*K*K), CHI, SIGLEV,
2      WORK(LWORK)
  LOGICAL      PARHLD((IP+IQ)*K*K)

```

3 Description

Let $W_t = (w_{1t}, w_{2t}, \dots, w_{kt})^T$, for $t = 1, 2, \dots, n$, denote a vector of k time series which is assumed to follow a multivariate ARMA model of the form

$$W_t - \mu = \phi_1(W_{t-1} - \mu) + \phi_2(W_{t-2} - \mu) + \dots + \phi_p(W_{t-p} - \mu) + \epsilon_t - \theta_1\epsilon_{t-1} - \theta_2\epsilon_{t-2} - \dots - \theta_q\epsilon_{t-q}, \quad (1)$$

where $\epsilon_t = (\epsilon_{1t}, \epsilon_{2t}, \dots, \epsilon_{kt})^T$, for $t = 1, 2, \dots, n$, is a vector of k residual series assumed to be Normally distributed with zero mean and positive-definite covariance matrix Σ . The components of ϵ_t are assumed to be uncorrelated at non-simultaneous lags. The ϕ_i and θ_j are k by k matrices of parameters. $\{\phi_i\}$, for $i = 1, 2, \dots, p$, are called the autoregressive (AR) parameter matrices, and $\{\theta_i\}$, for $i = 1, 2, \dots, q$, the moving average (MA) parameter matrices. The parameters in the model are thus the p (k by k) ϕ -matrices, the q (k by k) θ -matrices, the mean vector μ and the residual error covariance matrix Σ . Let

$$A(\phi) = \begin{bmatrix} \phi_1 & I & 0 & . & . & . & 0 \\ \phi_2 & 0 & I & 0 & . & . & 0 \\ . & & & . & & & \\ . & & & & . & & \\ \phi_{p-1} & 0 & . & . & . & 0 & I \\ \phi_p & 0 & . & . & . & 0 & 0 \end{bmatrix}_{pk \times pk} \quad \text{and} \quad B(\theta) = \begin{bmatrix} \theta_1 & I & 0 & . & . & . & 0 \\ \theta_2 & 0 & I & 0 & . & . & 0 \\ . & & & . & & & \\ . & & & & . & & \\ \theta_{q-1} & 0 & . & . & . & . & I \\ \theta_q & 0 & . & . & . & . & 0 \end{bmatrix}_{qk \times qk}$$

where I denotes the k by k identity matrix.

The ARMA model (1) is said to be stationary if the eigenvalues of $A(\phi)$ lie inside the unit circle, and invertible if the eigenvalues of $B(\theta)$ lie inside the unit circle. The ARMA model is assumed to be both stationary and invertible. Note that some of the elements of the ϕ - and/or θ -matrices may have been fixed at pre-specified values (for example by calling G13DDF).

The estimated residual cross-correlation matrix at lag l is defined to the k by k matrix $\hat{R}_l$ whose (i, j) th element is computed as

$$\hat{r}_{ij}(l) = \frac{\sum_{t=l+1}^n (\hat{\epsilon}_{it-l} - \bar{\epsilon}_i)(\hat{\epsilon}_{jt} - \bar{\epsilon}_j)}{\sqrt{\sum_{t=1}^n (\hat{\epsilon}_{it} - \bar{\epsilon}_i)^2 \sum_{t=1}^n (\hat{\epsilon}_{jt} - \bar{\epsilon}_j)^2}}, \quad l = 0, 1, \dots, i \text{ and } j = 1, 2, \dots, k,$$

where $\hat{\epsilon}_{it}$ denotes an estimate of the t th residual for the i th series ϵ_{it} and $\bar{\epsilon}_i = \sum_{t=1}^n \hat{\epsilon}_{it}/n$. (Note that $\hat{R}_l$ is an estimate of $E(\epsilon_{t-l}\epsilon_t^T)$, where E is the expected value.)

A modified portmanteau statistic, $Q_{(m)}^*$, is calculated from the formula (see Li and McLeod (1981))

$$Q_{(m)}^* = \frac{k^2 m(m+1)}{2n} + n \sum_{l=1}^m \hat{r}(l)^T (\hat{R}_0^{-1} \otimes \hat{R}_0^{-1}) \hat{r}(l),$$

where $\otimes$ denotes Kronecker product, $\hat{R}_0$ is the estimated residual cross-correlation matrix at lag zero and $\hat{r}(l) = \text{vec}(\hat{R}_l^T)$, where vec of a k by k matrix is a vector with the (i, j) th element in position $(i-1)k + j$. m denotes the number of residual cross-correlation matrices computed. (Advice on the choice of m is given in Section 8.2.) Let l_C denote the total number of ‘free’ parameters in the ARMA model excluding the mean, μ , and the residual error covariance matrix Σ . Then, under the hypothesis of model adequacy, $Q_{(m)}^*$ has an asymptotic χ^2 -distribution on $mk^2 - l_C$ degrees of freedom.

Let $\hat{r} = (\text{vec}(R_1^T), \text{vec}(R_2^T), \dots, \text{vec}(R_m^T))$ then the covariance matrix of $\hat{r}$ is given by

$$\text{Var}(\hat{r}) = [Y - X(X^T G G^T X)^{-1} X^T] / n,$$

where $Y = I_m \otimes (\Delta \otimes \Delta)$ and $G = I_m (G G^T)$. Δ is the dispersion matrix Σ in correlation form and G a nonsingular k by k matrix such that $G G^T = \Delta^{-1}$ and $G \Delta G^T = I_k$. The construction of the matrix X is discussed in Li and McLeod (1981). (Note that the mean, μ , plays no part in calculating $\text{Var}(\hat{r})$ and therefore is not required as input to G13DSF.)

4 References

Li W K and McLeod A I (1981) Distribution of the residual autocorrelations in multivariate ARMA time series models *J. Roy. Statist. Soc. Ser. B* **43** 231–239

5 Parameters

The output quantities K, N, V, KMAX, IP, IQ, PAR, PARHLD and QQ from G13DDF are suitable for input to G13DSF.

- 1: K – INTEGER *Input*
On entry: k , the number of residual time series.
Constraint: $K \geq 1$.
- 2: N – INTEGER *Input*
On entry: n , the number of observations in each residual series.
- 3: V(KMAX,N) – **double precision** array *Input*
On entry: $V(i, t)$ must contain an estimate of the i th component of ϵ_t , for $i = 1, 2, \dots, k$ and $t = 1, 2, \dots, n$.
Constraints:
 no two rows of V may be identical;
 in each row there must be at least two distinct elements.

- 4: KMAX – INTEGER Input
On entry: the first dimension of the arrays V, QQ and R0 and
Constraint: $KMAX \geq K$.
- 5: IP – INTEGER Input
On entry: p , the number of AR parameter matrices.
Constraint: $IP \geq 0$.
- 6: IQ – INTEGER Input
On entry: q , the number of MA parameter matrices.
Constraint: $IQ \geq 0$.
Note: $IP = IQ = 0$ is **not permitted**.
- 7: M – INTEGER Input
On entry: the value of m , the number of residual cross-correlation matrices to be computed. See Section 8.2 for advice on the choice of M.
Constraint: $IP + IQ < M < N$.
- 8: PAR($((IP + IQ) \times K \times K)$) – **double precision** array Input
On entry: the parameter estimates read in row by row in the order $\phi_1, \phi_2, \dots, \phi_p, \theta_1, \theta_2, \dots, \theta_q$.
Thus,
if $IP > 0$, PAR($((l - 1) \times k \times k + (i - 1) \times k + j)$) must be set equal to an estimate of the (i, j) th element of ϕ_l , for $l = 1, 2, \dots, p$ and $i, j = 1, 2, \dots, k$;
if $IQ \geq 0$, PAR($(p \times k \times k + (l - 1) \times k \times k + (i - 1) \times k + j)$) must be set equal to an estimate of the (i, j) th element of θ_l , for $l = 1, 2, \dots, q$ and $i, j = 1, 2, \dots, k$.
The first $p \times k \times k$ elements of PAR must satisfy the stationarity condition and the next $q \times k \times k$ elements of PAR must satisfy the invertibility condition.
- 9: PARHLD($((IP + IQ) \times K \times K)$) – LOGICAL array Input
On entry: PARHLD(i) must be set to .TRUE. if PAR(i) has been held constant at a pre-specified value and .FALSE. if PAR(i) is a free parameter, for $i = 1, 2, \dots, (p + q) \times k \times k$.
- 10: QQ(KMAX, K) – **double precision** array Input/Output
On entry: QQ(i, j) is an efficient estimate of the (i, j) th element of Σ . The lower triangle only is needed.
Constraint: QQ must be positive-definite.
On exit: if IFAIL $\neq 1$, then the upper triangle is set equal to the lower triangle.
- 11: ISHOW – INTEGER Input
On entry: must be nonzero if the residual cross-correlation matrices $\{\hat{r}_{ij}(l)\}$ and their standard errors $\{se(\hat{r}_{ij}(l))\}$, the modified portmanteau statistic with its significance and a summary table are to be printed. The summary table indicates which elements of the residual correlation matrices are significant at the 5% level in either a positive or negative direction; i.e., if $\hat{r}_{ij}(l) > 1.96 \times se(\hat{r}_{ij}(l))$ then a '+' is printed, if $\hat{r}_{ij}(l) < -1.96 \times se(\hat{r}_{ij}(l))$ then a '-' is printed, otherwise a fullstop (.) is printed. The summary table is only printed if $k \leq 6$ on entry.
The residual cross-correlation matrices, their standard errors and the modified portmanteau statistic with its significance are available also as output variables in R, RCM, CHI, IDF and SIGLEV.

- 12: R0(KMAX,K) – **double precision** array Output
On exit: if $i \neq j$, then $R0(i, j)$ contains an estimate of the (i, j) th element of the residual cross-correlation matrix at lag zero, $\hat{R}_0$. When $i = j$, $R0(i, j)$ contains the standard deviation of the i th residual series. If IFAIL = 3 on exit then the first K rows and columns of R0 are set to zero.
- 13: R(KMAX,KMAX,M) – **double precision** array Output
On exit: $R(i, j, l)$ is an estimate of the (i, j) th element of the residual cross-correlation matrix at lag l , for $i, j = 1, 2, \dots, k$ and $l = 1, 2, \dots, m$. If IFAIL = 3 on exit then all elements of R are set to zero.
- 14: RCM(LDRCM, $M \times K \times K$) – **double precision** array Output
On exit: the estimated standard errors and correlations of the elements in the array R. The correlation between $R(i, j, l)$ and $R(i_2, j_2, l_2)$ is returned as $RCM(s, t)$ where $s = (l - 1) \times k \times k + (j - 1) \times k + i$ and $t = (l_2 - 1) \times k \times k + (j_2 - 1) \times k + i_2$ except that if $s = t$, then $RCM(s, t)$ contains the standard error of $R(i, j, l)$. If on exit, IFAIL ≥ 5 , then all off-diagonal elements of RCM are set to zero and all diagonal elements are set to $1/\sqrt{n}$.
- 15: LDRCM – INTEGER Input
On entry: the first dimension of the array RCM as declared in the (sub)program from which G13DSF is called.
Constraint: $LDRCM \geq M \times K \times K$.
- 16: CHI – **double precision** Output
On exit: the value of the modified portmanteau statistic, $Q_{(m)}^*$. If IFAIL = 3 on exit then CHI is returned as zero.
- 17: IDF – INTEGER Output
On exit: the number of degrees of freedom of CHI.
- 18: SIGLEV – **double precision** Output
On exit: the significance level of CHI based on IDF degrees of freedom. If IFAIL = 3 on exit, SIGLEV is returned as one.
- 19: IW(LIW) – INTEGER array Workspace
20: LIW – INTEGER Input
On entry: the dimension of the array IW as declared in the (sub)program from which G13DSF is called.
Constraint: $LIW \geq K \times \max(IP, IQ)$.
- 21: WORK(LWORK) – **double precision** array Workspace
22: LWORK – INTEGER Input
On entry: the dimension of the array WORK as declared in the (sub)program from which G13DSF is called.
Constraint: if $LWORK \geq k(n + KMAX + 2) + mk^2(NPAR + mk^2 + 1) + 3k^2 + (NPAR + 1)NPAR$, $NPAR = (p + q)k^2$.
- 23: IFAIL – INTEGER Input/Output
On entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this parameter you should refer to Section 3.3 in the Essential Introduction for details.
On exit: IFAIL = 0 unless the routine detects an error (see Section 6).

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, because for this routine the values of the output parameters may be useful even if $IFAIL \neq 0$ on exit, the recommended value is -1 . **When the value -1 or 1 is used it is essential to test the value of $IFAIL$ on exit.**

6 Error Indicators and Warnings

If on entry $IFAIL = 0$ or -1 , explanatory error messages are output on the current error message unit (as defined by $X04AAF$).

Note: G13DSF may return useful information for one or more of the following detected errors or warnings.

Errors or warnings detected by the routine:

$IFAIL = 1$

On entry, $K < 1$,
 or $KMAX < K$,
 or $IP < 0$,
 or $IQ < 0$,
 or $IP = IQ = 0$,
 or $M \leq IP + IQ$,
 or $M \geq N$,
 or $LDRCM < M \times K \times K$,
 or LIW is too small,
 or $LWORK$ is too small.

$IFAIL = 2$

On entry, either QQ is not positive-definite or the autoregressive parameter matrices are extremely close to or outside the stationarity region, or the moving average parameter matrices are extremely close to or outside the invertibility region. To proceed, you must supply different parameter estimates in the arrays PAR and QQ .

$IFAIL = 3$

On entry, at least one of the k residual series is such that all its elements are practically identical giving zero (or near zero) variance or at least two of the residual series are identical. In this case CHI is set to zero, $SIGLEV$ to one and all the elements of $R0$ and R set to zero.

$IFAIL = 4$

This is an unlikely exit brought about by an excessive number of iterations being needed to evaluate the zeros of the determinantal polynomials $\det(A(\phi))$ and $\det(B(\theta))$. All output parameters are undefined.

$IFAIL = 5$

On entry, either the eigenvalues and eigenvectors of Δ (the matrix QQ in correlation form) could not be computed or the determinantal polynomials $\det(A(\phi))$ and $\det(B(\theta))$ have a factor in common. To proceed, you must either supply different parameter estimates in the array QQ or delete this common factor from the model. In this case, the off-diagonal elements of RCM are returned as zero and the diagonal elements set to $1/\sqrt{n}$. All other output quantities will be correct.

$IFAIL = 6$

This is an unlikely exit. At least one of the diagonal elements of RCM was found to be either negative or zero. In this case all off-diagonal elements of RCM are returned as zero and all diagonal elements of RCM set to $1/\sqrt{n}$.

7 Accuracy

The computations are believed to be stable.

8 Further Comments

8.1 Timing

The time taken by G13DSF depends upon the number of residual cross-correlation matrices to be computed, m , and the number of time series, k .

8.2 Choice of m

The number of residual cross-correlation matrices to be computed, m , should be chosen to ensure that when the ARMA model (1) is written as either an infinite order autoregressive process, i.e.,

$$W_t - \mu = \sum_{j=1}^{\infty} \pi_j (W_{t-j} - \mu) + \epsilon_t$$

or as an infinite order moving average process, i.e.,

$$W_t - \mu = \sum_{j=1}^{\infty} \psi_j \epsilon_{t-j} + \epsilon_t$$

then the two sequences of k by k matrices $\{\pi_1, \pi_2, \dots\}$ and $\{\psi_1, \psi_2, \dots\}$ are such that π_j and ψ_j are approximately zero for $j > m$. An overestimate of m is therefore preferable to an under-estimate of m . In many instances the choice $m = 10$ will suffice. In practice, to be on the safe side, you should try setting $m = 20$.

8.3 Checking a ‘White Noise’ Model

If you have fitted the ‘white noise’ model

$$W_t - \mu = \epsilon_t$$

then G13DSF should be entered with $p = 1$, $q = 0$, and the first k^2 elements of PAR and PARHLD set to zero and .TRUE. respectively.

8.4 Approximate Standard Errors

When IFAIL = 5 or 6 all the standard errors in RCM are set to $1/\sqrt{n}$. This is the asymptotic standard error of $\hat{r}_{ij}(l)$ when all the autoregressive and moving average parameters are assumed to be known rather than estimated.

8.5 Alternative Tests

$\hat{R}_0$ is useful in testing for instantaneous causality. If you wish to carry out a likelihood ratio test then the covariance matrix at lag zero ($\hat{C}_0$) can be used. It can be recovered from $\hat{R}_0$ by setting

$$\begin{aligned} \hat{C}_0(i, j) &= \hat{R}_0(i, j) \times \hat{R}_0(i, i) \times \hat{R}_0(j, j), \quad \text{for } i \neq j \\ &= \hat{R}_0(i, j) \times \hat{R}_0(i, j), \quad \text{for } i = j \end{aligned}$$

9 Example

This example fits a bivariate AR(1) model to two series each of length 48. μ has been estimated but $\phi_1(2, 1)$ has been constrained to be zero. Ten residual cross-correlation matrices are to be computed.

9.1 Program Text

```

*      G13DSF Example Program Text
*      Mark 15 Revised. NAG Copyright 1991.
*      .. Parameters ..
      INTEGER          NIN, NOUT
      PARAMETER        (NIN=5,NOUT=6)
      INTEGER          KMAX, IPMAX, IQMAX, NMAX, NPARMX, LWORK, LIW,
+      MMAX, LDRCM, LDCM
      PARAMETER        (KMAX=3,IPMAX=3,IQMAX=3,NMAX=100,
+      NPARMX=(IPMAX+IQMAX)*KMAX*KMAX+KMAX,LWORK=2000,
+      LIW=100,MMAX=20,LDRCM=MMAX*KMAX*KMAX,LDCM=NPARMX)
*      .. Local Scalars ..
      DOUBLE PRECISION CGETOL, CHI, RLOGL, SIGLEV
      INTEGER          I, IDF, IFAIL, IP, IPRINT, IQ, ISHOW, J, K, M,
+      MAXCAL, N, NITER, NPAR, OUTCHN
      LOGICAL          EXACT, MEAN
*      .. Local Arrays ..
      DOUBLE PRECISION CM(LDCM,NPARMX), G(NPARMX), PAR(NPARMX),
+      QQ(KMAX,KMAX), R(KMAX,KMAX,MMAX), RO(KMAX,KMAX),
+      RCM(LDRCM,MMAX*KMAX*KMAX), V(KMAX,NMAX),
+      W(KMAX,NMAX), WORK(LWORK)
      INTEGER          IW(LIW)
      LOGICAL          PARHLD(NPARMX)
*      .. External Subroutines ..
      EXTERNAL          G13DDF, G13DSF, X04ABF
*      .. Executable Statements ..
      WRITE (NOUT,*) 'G13DSF Example Program Results'
      OUTCHN = NOUT
*      Skip heading in data file
      READ (NIN,*)
      READ (NIN,*) K, N
*
      CALL X04ABF(1,OUTCHN)
*
      IF (K.GT.0 .AND. K.LE.KMAX .AND. N.GE.3 .AND. N.LE.NMAX) THEN
        DO 20 I = 1, K
          READ (NIN,*) (W(I,J),J=1,N)
20      CONTINUE
          READ (NIN,*) IP, IQ, MEAN, M
          IF (IP.GE.0 .AND. IP.LE.IPMAX .AND. IQ.GE.0 .AND. IQ.LE.IQMAX)
+          THEN
            NPAR = (IP+IQ)*K*K
            IF (MEAN) NPAR = NPAR + K
            IF (NPAR.LE.NPARMX) THEN
              DO 40 I = 1, NPAR
                PAR(I) = 0.0D0
                PARHLD(I) = .FALSE.
40          CONTINUE
                DO 80 J = 1, K
                  DO 60 I = J, K
                    QQ(I,J) = 0.0D0
60          CONTINUE
80          CONTINUE
                PARHLD(3) = .TRUE.
                EXACT = .TRUE.
*          ** Set IPRINT > 0 to obtain intermediate output **
                IPRINT = -1
                CGETOL = 0.0001D0
                MAXCAL = 40*NPAR*(NPAR+5)
                ISHOW = 2
                IFAIL = 1
*
                CALL G13DDF(K,N,IP,IQ,MEAN,PAR,NPAR,QQ,KMAX,W,PARHLD,
+                EXACT,IPRINT,CGETOL,MAXCAL,ISHOW,NITER,RLOGL,
+                V,G,CM,LDCM,IFAIL)
*
                WRITE (NOUT,*)
                IF (IFAIL.LT.0) THEN
                  WRITE (NOUT,*)
                  WRITE (NOUT,99999) ' ** G13DDF returned with'//

```

```

+          ' IFAIL = ', IFAIL
      ELSE
        IF (IFAIL.NE.0) THEN
          WRITE (NOUT,99999) 'G13DDF fails. IFAIL =', IFAIL
          WRITE (NOUT,*)
        END IF
        IF ((IFAIL.EQ.0 .OR. IFAIL.GE.4) .AND. M.LE.MMAX) THEN
          WRITE (NOUT,*) 'Output from G13DSF'
          WRITE (NOUT,*)
          ISHOW = 1
          IFAIL = -1
*
          CALL G13DSF(K,N,V,KMAX,IP,IQ,M,PAR,PARHLD,QQ,ISHOW,
+                R0,R,RCM,LDRCM,CHI,IDF,SIGLEV,IW,LIW,
+                WORK,LWORK,IFAIL)
*
          IF (IFAIL.NE.0) WRITE (NOUT,99999)
+                'G13DSF fails. IFAIL =', IFAIL
        END IF
      END IF
    END IF
  END IF
END IF
END IF
END IF
*
99999 FORMAT (1X,A,I5)
END

```

9.2 Program Data

G13DSF Example Program Data

2 48 : K, no. of time series, N, no. of obs in each time series

```

-1.490 -1.620 5.200 6.230 6.210 5.860
 4.090 3.180 2.620 1.490 1.170 0.850
-0.350 0.240 2.440 2.580 2.040 0.400
 2.260 3.340 5.090 5.000 4.780 4.110
 3.450 1.650 1.290 4.090 6.320 7.500
 3.890 1.580 5.210 5.250 4.930 7.380
 5.870 5.810 9.680 9.070 7.290 7.840
 7.550 7.320 7.970 7.760 7.000 8.350
 7.340 6.350 6.960 8.540 6.620 4.970
 4.550 4.810 4.750 4.760 10.880 10.010
11.620 10.360 6.400 6.240 7.930 4.040
 3.730 5.600 5.350 6.810 8.270 7.680
 6.650 6.080 10.250 9.140 17.750 13.300
 9.630 6.800 4.080 5.060 4.940 6.650
 7.940 10.760 11.890 5.850 9.010 7.500
10.020 10.380 8.150 8.370 10.730 12.140 : End of time series
1 0 T 10 : IP, IQ, MEAN and M

```

9.3 Program Results

G13DSF Example Program Results

VALUE OF IFAIL PARAMETER ON EXIT FROM G13DDF = 0

VALUE OF LOG LIKELIHOOD FUNCTION ON EXIT = -0.20280E+03

MAXIMUM LIKELIHOOD ESTIMATES OF AR PARAMETER MATRICES

```

-----
PHI(1)    ROW-WISE :    0.802    0.065
                   (0.091) (0.102)

                   0.000    0.575
                   (0.000) (0.121)

```

MAXIMUM LIKELIHOOD ESTIMATE OF PROCESS MEAN

```

-----
                4.271    7.825

```

(1.219) (0.776)

MAXIMUM LIKELIHOOD ESTIMATE OF SIGMA MATRIX

2.964

0.637 5.380

RESIDUAL SERIES NUMBER 1

T	1	2	3	4	5	6	7	8
V(T)	-3.33	-1.24	5.75	1.27	0.32	0.11	-1.27	-0.73
T	9	10	11	12	13	14	15	16
V(T)	-0.58	-1.26	-0.67	-1.13	-2.02	-0.57	1.24	-0.13
T	17	18	19	20	21	22	23	24
V(T)	-0.77	-2.09	1.34	0.95	1.71	0.23	-0.01	-0.60
T	25	26	27	28	29	30	31	32
V(T)	-0.68	-1.89	-0.77	2.05	2.11	0.94	-3.32	-2.50
T	33	34	35	36	37	38	39	40
V(T)	3.16	0.47	0.05	2.77	-0.82	0.25	3.99	0.20
T	41	42	43	44	45	46	47	48
V(T)	-0.70	1.07	0.44	0.28	1.09	0.50	-0.10	1.70

RESIDUAL SERIES NUMBER 2

T	1	2	3	4	5	6	7	8
V(T)	-0.19	-1.20	-0.02	1.21	-1.62	-2.16	-1.63	-1.13
T	9	10	11	12	13	14	15	16
V(T)	-1.34	-1.30	4.82	0.43	2.54	0.35	-2.88	-0.77
T	17	18	19	20	21	22	23	24
V(T)	1.02	-3.85	-1.92	0.13	-1.20	0.41	1.03	-0.40
T	25	26	27	28	29	30	31	32
V(T)	-1.09	-1.07	3.43	-0.08	9.17	-0.23	-1.34	-2.06
T	33	34	35	36	37	38	39	40
V(T)	-3.16	-0.61	-1.30	0.48	0.79	2.87	2.38	-4.31
T	41	42	43	44	45	46	47	48
V(T)	2.32	-1.01	2.38	1.29	-1.14	0.36	2.59	2.64

Output from G13DSF

RESIDUAL CROSS-CORRELATION MATRICES

LAG	1	:	0.130	0.112
			(0.119)	(0.143)
			0.094	0.043
			(0.069)	(0.102)
LAG	2	:	-0.312	0.021
			(0.128)	(0.144)
			-0.162	0.098
			(0.125)	(0.132)
LAG	3	:	0.004	-0.176
			(0.134)	(0.144)
			-0.168	-0.091
			(0.139)	(0.140)

```

LAG      4      :   -0.090  -0.120
                   (0.137) (0.144)
                   0.099  -0.232
                   (0.142) (0.143)

LAG      5      :    0.041   0.093
                   (0.140) (0.144)
                  -0.009  -0.089
                   (0.144) (0.144)

LAG      6      :    0.234  -0.008
                   (0.141) (0.144)
                   0.069  -0.103
                   (0.144) (0.144)

LAG      7      :   -0.076   0.007
                   (0.142) (0.144)
                   0.168   0.000
                   (0.144) (0.144)

LAG      8      :   -0.074   0.559
                   (0.143) (0.144)
                   0.008  -0.101
                   (0.144) (0.144)

LAG      9      :    0.091   0.193
                   (0.144) (0.144)
                   0.055   0.170
                   (0.144) (0.144)

LAG     10      :   -0.060   0.061
                   (0.144) (0.144)
                   0.191   0.089
                   (0.144) (0.144)

```

SUMMARY TABLE

LAGS 1 - 10

```

*****
*           *           *
*  .-..... * .....+. *
*           *           *
*****
*           *           *
*  ..... * ..... *
*           *           *
*****

```

```

LI-MCLEOD PORTMANTEAU STATISTIC =    49.234
      SIGNIFICANCE LEVEL =      0.086
(BASED ON  37 DEGREES OF FREEDOM)

```

```

VALUE OF IFAIL PARAMETER ON EXIT FROM G13DSF =  0

```
