

NAG Library Routine Document

G13BAF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of ***bold italicised*** terms and other implementation-dependent details.

1 Purpose

G13BAF filters a time series by an ARIMA model.

2 Specification

```
SUBROUTINE G13BAF(Y, NY, MR, NMR, PAR, NPAR, CY, WA, NWA, B, NB, IFAIL)
INTEGER          NY, MR(NMR), NMR, NPAR, NWA, NB, IFAIL
double precision Y(NY), PAR(NPAR), CY, WA(NWA), B(NB)
```

3 Description

From a given series $y_1, y_2, \dots, y_n$, a new series $b_1, b_2, \dots, b_n$ is calculated using a supplied (filtering) ARIMA model. This model will be one which has previously been fitted to a series x_t with residuals a_t . The equations defining b_t in terms of y_t are very similar to those by which a_t is obtained from x_t . The only dissimilarity is that no constant correction is applied after differencing. This is because the series y_t is generally distinct from the series x_t with which the model is associated, though y_t may be related to x_t . Whilst it is appropriate to apply the ARIMA model to y_t so as to preserve the same relationship between b_t and a_t as exists between y_t and x_t , the constant term in the ARIMA model is inappropriate for y_t . The consequence is that b_t will not necessarily have zero mean.

The equations are precisely:

$$w_t = \nabla^d \nabla_s^D y_t, \quad (1)$$

the appropriate differencing of y_t ; both the seasonal and non-seasonal inverted autoregressive operations are then applied,

$$u_t = w_t - \Phi_1 w_{t-s} - \dots - \Phi_P w_{t-s \times P} \quad (2)$$

$$v_t = u_t - \phi_1 u_{t-1} - \dots - \phi_p u_{t-p} \quad (3)$$

followed by the inverted moving average operations

$$z_t = v_t + \Theta_1 z_{t-s} + \dots + \Theta_Q z_{t-s \times Q} \quad (4)$$

$$b_t = z_t + \theta_1 b_{t-1} + \dots + \theta_q b_{t-q}. \quad (5)$$

Because the filtered series value b_t depends on present and past values $y_t, y_{t-1}, \dots$, there is a problem arising from ignorance of $y_0, y_{-1}, \dots$ which particularly affects calculation of the early values $b_1, b_2, \dots$, causing 'transient errors'. The routine allows two possibilities.

- (i) The equations (1), (2) and (3) are applied from successively later time points so that all terms on their right-hand sides are known, with v_t being defined for $t = (1 + d + s \times D + s \times P), \dots, n$. Equations (4) and (5) are then applied over the same range, taking any values on the right-hand side associated with previous time points to be zero.

This procedure may still however result in unacceptably large transient errors in early values of b_t .

- (ii) The unknown values $y_0, y_{-1}, \dots$ are estimated by backforecasting. This requires that an ARIMA model distinct from that which has been supplied for filtering, should have been previously fitted to y_t .

For efficiency, you are asked to supply both this ARIMA model for y_t and a limited number of backforecasts which are prefixed to the known values of y_t . Within the routine further backforecasts of y_t ,

and the series w_t , u_t , v_t in (1), (2) and (3) are then easily calculated, and a set of linear equations solved for backforecasts of z_t , b_t for use in (4) and (5) in the case that $q + Q > 0$.

Even if the best model for y_t is not available, a very approximate guess such as

$$y_t = c + e_t$$

or

$$\nabla y_t = e_t$$

can help to reduce the transients substantially.

The backforecasts which need to be prefixed to y_t are of length $Q'_y = q_y + s_y \times Q_y$, where q_y and Q_y are the non-seasonal and seasonal moving average orders and s_y the seasonal period for the ARIMA model of y_t . Thus you need not carry out the backforecasting exercise if $Q'_y = 0$. Otherwise, the series $y_1, y_2, \dots, y_n$ should be reversed to obtain $y_n, y_{n-1}, \dots, y_1$ and G13AJF should be used to forecast Q'_y values, $\hat{y}_0, \dots, \hat{y}_{1-Q'_y}$. The ARIMA model used is that fitted to y_t (as a forward series) except that, if $d_y + D_y$ is odd, the constant should be changed in sign (to allow, for example, for the fact that a forward upward trend is a reversed downward trend). The ARIMA model for y_t supplied to the filtering routine must however have the appropriate constant for the forward series.

The series $\hat{y}_{1-Q'_y}, \dots, \hat{y}_0, y_1, \dots, y_n$ is then supplied to the routine, and a corresponding set of values returned for b_t .

4 References

Box G E P and Jenkins G M (1976) *Time Series Analysis: Forecasting and Control* (Revised Edition) Holden-Day

5 Parameters

- 1: Y(NY) – *double precision* array *Input*

On entry: the Q'_y backforecasts, starting with backforecast at time $1 - Q'_y$ to backforecast at time 0, followed by the time series starting at time 1, where $Q'_y = \text{MR}(10) + \text{MR}(13) \times \text{MR}(14)$. If there are no backforecasts, either because the ARIMA model for the time series is not known, or because it is known but has no moving average terms, then the time series starts at the beginning of Y.

- 2: NY – INTEGER *Input*

On entry: the total number of backforecasts and time series data points in array Y.

Constraint: $\text{NY} \geq \max(1 + Q'_y, \text{NPAR})$.

- 3: MR(NMR) – INTEGER array *Input*

On entry: the orders vector for the filtering model, followed by the orders vector for the ARIMA model for the time series if the latter is known. The orders appear in the standard sequence (p, d, q, P, D, Q, s) as given in the G13 Chapter Introduction. If the ARIMA model for the time series is supplied, then the routine will assume that the first Q'_y values of the array Y are backforecasts.

Constraints:

the filtering model is restricted in the following ways:

$\text{MR}(1) + \text{MR}(3) + \text{MR}(4) + \text{MR}(6) > 0$, i.e., filtering by a model which contains only differencing terms is not permitted;

$\text{MR}(k) \geq 0$, for $k = 1, 2, \dots, 7$;

if $\text{MR}(7) = 0$, $\text{MR}(4) + \text{MR}(5) + \text{MR}(6) = 0$;

if $\text{MR}(7) \neq 0$, $\text{MR}(4) + \text{MR}(5) + \text{MR}(6) \neq 0$;

$\text{MR}(7) \neq 1$.

the ARIMA model for the time series is restricted in the following ways:

$MR(k) \geq 0$, for $k = 8, 9, \dots, 14$;
 if $MR(14) = 0$, $MR(11) + MR(12) + MR(13) = 0$;
 if $MR(14) \neq 0$, $MR(11) + MR(12) + MR(13) \neq 0$;
 $MR(14) \neq 1$.

- 4: NMR – INTEGER *Input*
- On entry:* the number of values specified in the array MR. It takes the value 7 if no ARIMA model for the time series is supplied but otherwise it takes the value 14. Thus NMR acts as an indicator as to whether backforecasting can be carried out.
- Constraint:* NMR = 7 or 14.
- 5: PAR(NPAR) – **double precision** array *Input*
- On entry:* the parameters of the filtering model, followed by the parameters of the ARIMA model for the time series, if supplied. Within each model the parameters are in the standard order of non-seasonal AR and MA followed by seasonal AR and MA.
- 6: NPAR – INTEGER *Input*
- On entry:* the total number of parameters held in array PAR.
- Constraints:*
- if NMR = 7, $NPAR = MR(1) + MR(3) + MR(4) + MR(6)$;
 if NMR = 14, $NPAR = MR(1) + MR(3) + MR(4) + MR(6) + MR(8) + MR(10) + MR(11) + MR(13)$.
- Note:** the first constraint (i.e., $MR(1) + MR(3) + MR(4) + MR(6) > 0$) on the orders of the filtering model, in parameter MR, ensures that NPAR > 0.
- 7: CY – **double precision** *Input*
- On entry:* if the ARIMA model is known (i.e., NMR = 14), CY must specify the constant term of the ARIMA model for the time series. If this model is not known (i.e., NMR = 7), then CY is not used.
- 8: WA(NWA) – **double precision** array *Workspace*
- 9: NWA – INTEGER *Input*
- On entry:* the dimension of the array WA as declared in the (sub)program from which G13BAF is called. Workspace is only required if the ARIMA model for the time series is known.
- Constraints:*
- let $K = MR(3) + MR(6) \times MR(7) + MR(8) + MR(9) + (MR(11) + MR(12)) \times MR(14)$,
 then
- if NMR = 14, $NWA \geq K \times (K + 2)$;
 if NMR = 7, $NWA \geq 1$.
- 10: B(NB) – **double precision** array *Output*
- On exit:* the filtered output series. If the ARIMA model for the time series was known, and hence Q'_y backforecasts were supplied in Y, then B contains Q'_y ‘filtered’ backforecasts followed by the filtered series. Otherwise, the filtered series begins at the start of B just as the original series began at the start of Y. In either case, if the value of the series at time t is held in $Y(t)$, then the filtered value at time t is held in $B(t)$.

11: NB – INTEGER

Input

On entry: the dimension of the array B as declared in the (sub)program from which G13BAF is called. In addition to holding the returned filtered series, B is also used as an intermediate work array if the ARIMA model for the time series was known.

Constraints:

if $NMR = 14$, $NB \geq NY + \max(K_3, K_1 + K_2)$;

if $NMR = 7$, $NB \geq NY$.

Where

$$K_1 = MR(1) + MR(4) \times MR(7);$$

$$K_2 = MR(2) + MR(5) \times MR(7);$$

$$K_3 = MR(3) + MR(6) \times MR(7).$$

12: IFAIL – INTEGER

Input/Output

On entry: IFAIL must be set to 0, -1 or 1. If you are unfamiliar with this parameter you should refer to Section 3.3 in the Essential Introduction for details.

On exit: IFAIL = 0 unless the routine detects an error (see Section 6).

For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, if you are not familiar with this parameter, the recommended value is 0. **When the value -1 or 1 is used it is essential to test the value of IFAIL on exit.**

6 Error Indicators and Warnings

If on entry IFAIL = 0 or -1, explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

IFAIL = 1

On entry, $NMR \neq 7$ and $NMR \neq 14$.

IFAIL = 2

On entry, the orders vector MR does not satisfy the constraints given in Section 5.

IFAIL = 3

On entry, NPAR is inconsistent with the contents of MR (see Section 5).

IFAIL = 4

On entry, NY is too small to successfully carry out the requested filtering, (see Section 5).

IFAIL = 5

On entry, the work array WA is too small.

IFAIL = 6

On entry, the array B is too small.

IFAIL = 7

The orders vector for the filtering model is invalid.

IFAIL = 8

The orders vector for the ARIMA model is invalid. (Only occurs if NMR = 14.)

IFAIL = 9

The initial values of the filtered series are indeterminate for the given models.

IFAIL = -999

Internal memory allocation failed.

7 Accuracy

Accuracy and stability are high except when the MA parameters are close to the invertibility boundary.

8 Further Comments

If an ARIMA model is supplied, a local workspace array of fixed length is allocated internally by G13BAF. The total size of this array amounts to K INTEGER elements, where K is the expression defined in the description of the parameter WA.

The time taken by G13BAF is approximately proportional to

$$NY \times (MR(1) + MR(3) + MR(4) + MR(6)),$$

with an appreciable fixed increase if an ARIMA model is supplied for the time series.

9 Example

This example reads a time series of length 296. It reads the univariate ARIMA (4,0,2,0,0,0,0) model and the ARIMA filtering (3,0,0,0,0,0,0) model for the series. Two initial backforecasts are required and these are calculated by a call to G13AJF. The backforecasts are inserted at the start of the series and G13BAF is called to perform the calculations.

9.1 Program Text

```
*      G13BAF Example Program Text
*      Mark 14 Revised. NAG Copyright 1989.
*      .. Parameters ..
      INTEGER          NXMAX, NPMAX, ISTMAX, IFVMAX, IW, IQXDMX, NYMAX,
+                     NBMAX
      PARAMETER        (NXMAX=300,NPMAX=10,ISTMAX=20,IFVMAX=2,IW=2200,
+                     IQXDMX=5,NYMAX=NXMAX+IQXDMX,NBMAX=320)
      INTEGER          NIN, NOUT
      PARAMETER        (NIN=5,NOUT=6)
*      .. Local Scalars ..
      DOUBLE PRECISION A1, A2, CX, CY, RMS
      INTEGER          I, IDD, IFAIL, II, IJ, IQXD, J, K, N, NB, NI,
+                     NMR, NPAR, NPARX, NST, NWA, NX, NY
*      .. Local Arrays ..
      DOUBLE PRECISION B(NBMAX), FSD(IFVMAX), FVA(IFVMAX), PAR(NPMAX),
+                     PARX(NPMAX), ST(ISTMAX), WA(IW), X(NXMAX),
+                     Y(NYMAX)
      INTEGER          ISF(4), MR(14), MRX(7)
*      .. External Subroutines ..
      EXTERNAL         G13AJF, G13BAF
*      .. Intrinsic Functions ..
      INTRINSIC        MAX, MIN, MOD
*      .. Executable Statements ..
      WRITE (NOUT,*) 'G13BAF Example Program Results'
*      Skip heading in data file
      READ (NIN,*)
      READ (NIN,*) NX
      IF (NX.GT.0 .AND. NX.LE.NXMAX) THEN
        READ (NIN,*) (X(I),I=1,NX)
```

```

*      Read univariate ARIMA for series
      READ (NIN,*) (MRX(I),I=1,7)
      READ (NIN,*) CX
      NPARX = MRX(1) + MRX(3) + MRX(4) + MRX(6)
      IF (NPARX.GT.0 .AND. NPARX.LE.NPMAX) THEN
*          Read model by which to filter series
          READ (NIN,*) (PARX(I),I=1,NPARX)
          READ (NIN,*) (MR(I),I=1,7)
          NPAR = MR(1) + MR(3) + MR(4) + MR(6)
          IF (NPAR.GT.0 .AND. NPAR+NPARX.LE.NPMAX) THEN
*              Initially backforecast QY values
*              (1) Reverse series in situ
              N = NX/2
              NI = NX
              DO 20 I = 1, N
                  A1 = X(I)
                  A2 = X(NI)
                  X(I) = A2
                  X(NI) = A1
                  NI = NI - 1
20          CONTINUE
              IDD = MRX(2) + MRX(5)
*              (2) Possible sign reversal for ARIMA constant
              IF (MOD(IDD,2).NE.0) CX = -CX
*              (3) Calculate number of backforecasts required
              IQXD = MRX(3) + MRX(6)*MRX(7)
              IF (IQXD.NE.0) THEN
*                  (4) Set up parameter list for call to forecast
*                  routine G13AJF
*                  IFAIL = 0
*
*                  CALL G13AJF(MRX,PARX,NPARX,CX,1,X,NX,RMS,ST,ISTMAX,
+                      NST,IQXD,FVA,FSD,IFVMAX,ISF,WA,IW,IFAIL)
*
*                  J = IQXD
*                  DO 40 I = 1, IQXD
*                      Y(I) = FVA(J)
*                      J = J - 1
40          CONTINUE
*              Move series into Y
              J = IQXD + 1
              K = NX
              DO 60 I = 1, NX
                  IF (J.GT.NYMAX) GO TO 160
                  Y(J) = X(K)
                  J = J + 1
                  K = K - 1
60          CONTINUE
              END IF
*              Calculate series length
              NY = NX + IQXD
*              Move ARIMA for series into MR
              DO 80 I = 1, 7
                  MR(7+I) = MRX(I)
80          CONTINUE
*              Move parameters of ARIMA for Y into PAR
              DO 100 I = 1, NPARX
                  PAR(NPAR+I) = PARX(I)
100         CONTINUE
              NPAR = NPAR + NPARX
*              Move constant and reset sign reversal
              CY = CX
              IF (MOD(IDD,2).NE.0) CY = -CY
*              Set parameters for call to filter routine G13BAF
              NMR = 14
              NWA = MR(3) + MR(6)*MR(7) + MR(8) + MR(9) + (MR(11)
+                  +MR(12))*MR(14)
              NWA = NWA*(NWA+2)
              NB = NY + MAX(MR(3)+MR(6)*MR(7),MR(1)+MR(2)+(MR(4)+MR(5))
+                  *MR(7))

```

```

      IF (NWA.LE.IW .AND. NB.LE.NBMAX) THEN
        IFAIL = 0
*      Filter series by call to G13BAF
        CALL G13BAF(Y,NY,MR,NMR,PAR,NPAR,CY,WA,NWA,B,NB,IFAIL)
*
        WRITE (NOUT,*)
        WRITE (NOUT,*)
+      '
+      'Original
+      'Filtered'
        WRITE (NOUT,*)
+      'Backforecasts
+      'y-series
+      'series'
        IF (IQXD.NE.0) THEN
          IJ = -IQXD
          DO 120 I = 1, IQXD
            WRITE (NOUT,99999) IJ, Y(I), B(I)
            IJ = IJ + 1
120          CONTINUE
          END IF
          WRITE (NOUT,*)
          WRITE (NOUT,*)
+      '
+      'Filtered
+      'Filtered
+      'Filtered
+      'Filtered'
          WRITE (NOUT,*)
+      '
+      'series
+      'series
+      'series
+      'series'
          DO 140 I = IQXD + 1, NY, 4
            WRITE (NOUT,99998) (II-IQXD,B(II),II=I,MIN(NY,I+3))
140          CONTINUE
          END IF
        END IF
      END IF
    END IF
  END IF
160 CONTINUE
*
99999 FORMAT (1X,I8,F17.4,F15.4)
99998 FORMAT (1X,I5,F9.4,I7,F9.4,I7,F9.4,I7,F9.4)
END

```

9.2 Program Data

G13BAF Example Program Data

```

296
53.8 53.6 53.5 53.5 53.4 53.1 52.7 52.4 52.2 52.0 52.0 52.4 53.0 54.0 54.9 56.0
56.8 56.8 56.4 55.7 55.0 54.3 53.2 52.3 51.6 51.2 50.8 50.5 50.0 49.2 48.4 47.9
47.6 47.5 47.5 47.6 48.1 49.0 50.0 51.1 51.8 51.9 51.7 51.2 50.0 48.3 47.0 45.8
45.6 46.0 46.9 47.8 48.2 48.3 47.9 47.2 47.2 48.1 49.4 50.6 51.5 51.6 51.2 50.5
50.1 49.8 49.6 49.4 49.3 49.2 49.3 49.7 50.3 51.3 52.8 54.4 56.0 56.9 57.5 57.3
56.6 56.0 55.4 55.4 56.4 57.2 58.0 58.4 58.4 58.1 57.7 57.0 56.0 54.7 53.2 52.1
51.6 51.0 50.5 50.4 51.0 51.8 52.4 53.0 53.4 53.6 53.7 53.8 53.8 53.8 53.3 53.0
52.9 53.4 54.6 56.4 58.0 59.4 60.2 60.0 59.4 58.4 57.6 56.9 56.4 56.0 55.7 55.3
55.0 54.4 53.7 52.8 51.6 50.6 49.4 48.8 48.5 48.7 49.2 49.8 50.4 50.7 50.9 50.7
50.5 50.4 50.2 50.4 51.2 52.3 53.2 53.9 54.1 54.0 53.6 53.2 53.0 52.8 52.3 51.9
51.6 51.6 51.4 51.2 50.7 50.0 49.4 49.3 49.7 50.6 51.8 53.0 54.0 55.3 55.9 55.9
54.6 53.5 52.4 52.1 52.3 53.0 53.8 54.6 55.4 55.9 55.9 55.2 54.4 53.7 53.6 53.6
53.2 52.5 52.0 51.4 51.0 50.9 52.4 53.5 55.6 58.0 59.5 60.0 60.4 60.5 60.2 59.7
59.0 57.6 56.4 55.2 54.5 54.1 54.1 54.4 55.5 56.2 57.0 57.3 57.4 57.0 56.4 55.9
55.5 55.3 55.2 55.4 56.0 56.5 57.1 57.3 56.8 55.6 55.0 54.1 54.3 55.3 56.4 57.2
57.8 58.3 58.6 58.8 58.8 58.6 58.0 57.4 57.0 56.4 56.3 56.4 56.4 56.0 55.2 54.0
53.0 52.0 51.6 51.6 51.1 50.4 50.0 50.0 52.0 54.0 55.1 54.5 52.8 51.4 50.8 51.2
52.0 52.8 53.8 54.5 54.9 54.9 54.8 54.4 53.7 53.3 52.8 52.6 52.6 53.0 54.3 56.0
57.0 58.0 58.6 58.5 58.3 57.8 57.3 57.0
4      0      2      0      0      0      0
0.000
2.420      -2.380      1.160      -0.230      0.310      -0.470
3      0      0      0      0      0
1.970      -1.370      0.340

```

9.3 Program Results

G13BAF Example Program Results

Backforecasts	Original y-series	Filtered series		
-2	49.9807	3.4222		
-1	52.6714	3.0809		
Filtered series	Filtered series	Filtered series	Filtered series	Filtered series
1 2.9813	2 2.7803	3 3.7057	4 3.2450	
5 3.0760	6 3.0070	7 3.0610	8 3.1720	
9 3.1170	10 3.0360	11 3.2580	12 3.4520	
13 3.3320	14 3.6980	15 3.3140	16 3.8070	
17 3.3330	18 2.9580	19 3.2800	20 3.0960	
21 3.2270	22 3.0830	23 2.6410	24 3.1870	
25 2.9910	26 3.1110	27 2.8460	28 3.0240	
29 2.7030	30 2.6130	31 2.8060	32 2.9560	
33 2.8170	34 2.8950	35 2.8510	36 2.9160	
37 3.2530	38 3.3050	39 3.1830	40 3.3760	
41 2.9730	42 2.8610	43 3.0490	44 2.8420	
45 2.3190	46 2.3660	47 2.9410	48 2.3810	
49 3.3420	50 2.9340	51 3.1800	52 2.9230	
53 2.6470	54 2.8860	55 2.5310	56 2.6200	
57 3.4170	58 3.4940	59 3.2590	60 3.1310	
61 3.1420	62 2.6710	63 2.8990	64 2.8180	
65 3.2150	66 2.8800	67 2.9610	68 2.8800	
69 3.0020	70 2.8930	71 3.1210	72 3.2210	
73 3.2040	74 3.5360	75 3.7520	76 3.5630	
77 3.7260	78 3.1560	79 3.6310	80 2.9380	
81 3.1480	82 3.4490	83 3.1400	84 3.7380	
85 4.1200	86 3.1540	87 3.7480	88 3.3280	
89 3.3640	90 3.3400	91 3.3950	92 3.0720	
93 3.0050	94 2.8520	95 2.7810	96 3.1950	
97 3.2490	98 2.6370	99 3.0080	100 3.2410	
101 3.5570	102 3.2080	103 3.0880	104 3.3980	
105 3.1660	106 3.1960	107 3.2460	108 3.2870	
109 3.1590	110 3.2620	111 2.7280	112 3.4130	
113 3.2190	114 3.6750	115 3.8550	116 4.0100	
117 3.5380	118 3.8440	119 3.4660	120 3.0640	
121 3.4780	122 3.1140	123 3.5300	124 3.2400	
125 3.3630	126 3.2610	127 3.3020	128 3.1150	
129 3.3280	130 2.8730	131 3.0800	132 2.8390	
133 2.6570	134 3.0260	135 2.4580	136 3.2600	
137 2.8380	138 3.2150	139 3.1140	140 3.1050	
141 3.1400	142 2.9100	143 3.1370	144 2.7500	
145 3.1160	146 3.0680	147 2.8590	148 3.3840	
149 3.5500	150 3.4160	151 3.1770	152 3.3390	
153 3.0190	154 3.1780	155 3.0110	156 3.1940	
157 3.2680	158 3.0500	159 2.8060	160 3.1850	
161 3.0560	162 3.2690	163 2.7940	164 3.0900	
165 2.7100	166 2.7890	167 2.9510	168 3.2440	
169 3.2570	170 3.4360	171 3.4450	172 3.3780	
173 3.3520	174 3.9180	175 2.9190	176 3.1780	
177 2.2580	178 3.5150	179 2.8010	180 3.6030	
181 3.2610	182 3.5300	183 3.3270	184 3.4420	
185 3.5240	186 3.2720	187 3.1110	188 2.8240	
189 3.2330	190 3.1500	191 3.5710	192 3.0810	
193 2.7820	194 2.9040	195 3.2350	196 2.7970	
197 3.1320	198 3.1680	199 4.5210	200 2.6650	
201 4.6870	202 3.9470	203 3.2220	204 3.3410	
205 3.9950	206 3.4820	207 3.3630	208 3.4550	
209 3.2950	210 2.6910	211 3.4600	212 2.9440	
213 3.4400	214 3.1830	215 3.4200	216 3.4100	
217 4.0550	218 2.9990	219 3.8250	220 3.1340	
221 3.5010	222 3.0430	223 3.2660	224 3.3660	
225 3.2650	226 3.3720	227 3.2880	228 3.5470	
229 3.6840	230 3.3100	231 3.6790	232 3.1780	
233 2.9360	234 2.7910	235 3.8020	236 2.6100	
237 4.1690	238 3.7460	239 3.4560	240 3.3910	

241	3.5820	242	3.6220	243	3.4870	244	3.5770
245	3.4240	246	3.3960	247	3.1220	248	3.4300
249	3.4580	250	3.0280	251	3.7660	252	3.3770
253	3.2470	254	3.0180	255	2.9720	256	2.8000
257	3.2040	258	2.8020	259	3.4100	260	3.1680
261	2.4600	262	2.8810	263	3.1750	264	3.1740
265	4.8640	266	3.0600	267	2.9600	268	2.2530
269	2.5620	270	3.3150	271	3.3480	272	3.5900
273	3.2560	274	3.2320	275	3.6160	276	3.1700
277	3.2890	278	3.1200	279	3.3300	280	2.9910
281	2.9420	282	3.4070	283	2.8720	284	3.3470
285	3.1920	286	3.4880	287	4.0680	288	3.7550
289	3.0510	290	3.9680	291	3.3900	292	3.1380
293	3.6170	294	3.1700	295	3.4150	296	3.4830
