

NAG Library Routine Document

F07NWF (ZSYTRI)

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

1 Purpose

F07NWF (ZSYTRI) computes the inverse of a complex symmetric matrix A , where A has been factorized by F07NRF (ZSYTRF).

2 Specification

```
SUBROUTINE F07NWF(UPLO, N, A, LDA, IPIV, WORK, INFO)
  INTEGER          N, LDA, IPIV(*), INFO
  complex*16      A(LDA,*), WORK(2*N)
  CHARACTER*1      UPLO
```

The routine may be called by its LAPACK name *zsytri*.

3 Description

F07NWF (ZSYTRI) is used to compute the inverse of a complex symmetric matrix A , the routine must be preceded by a call to F07NRF (ZSYTRF), which computes the Bunch–Kaufman factorization of A .

If $UPLO = 'U'$, $A = PUDU^T P^T$ and A^{-1} is computed by solving $U^T P^T X P U = D^{-1}$ for X .

If $UPLO = 'L'$, $A = PLDL^T P^T$ and A^{-1} is computed by solving $L^T P^T X P L = D^{-1}$ for X .

4 References

Du Croz J J and Higham N J (1992) Stability of methods for matrix inversion *IMA J. Numer. Anal.* **12** 1–19

5 Parameters

- 1: $UPLO$ – CHARACTER*1 *Input*
On entry: indicates how A has been factorized.
 $UPLO = 'U'$
 $A = PUDU^T P^T$, where U is upper triangular.
 $UPLO = 'L'$
 $A = PLDL^T P^T$, where L is lower triangular.
Constraint: $UPLO = 'U'$ or $'L'$.
- 2: N – INTEGER *Input*
On entry: n , the order of the matrix A .
Constraint: $N \geq 0$.
- 3: $A(LDA,*)$ – **complex*16** array *Input/Output*
Note: the second dimension of the array A must be at least $\max(1, N)$.
On entry: details of the factorization of A , as returned by F07NRF (ZSYTRF).

On exit: the factorization is overwritten by the n by n symmetric matrix A^{-1} .

If UPLO = 'U', the upper triangle of A^{-1} is stored in the upper triangular part of the array.

If UPLO = 'L', the lower triangle of A^{-1} is stored in the lower triangular part of the array.

4: LDA – INTEGER *Input*

On entry: the first dimension of the array A as declared in the (sub)program from which F07NWF (ZSYTRI) is called.

Constraint: $LDA \geq \max(1, N)$.

5: IPIV(*) – INTEGER array *Input*

Note: the dimension of the array IPIV must be at least $\max(1, N)$.

On entry: details of the interchanges and the block structure of D , as returned by F07NRF (ZSYTRF).

6: WORK($2 \times N$) – **complex*16** array *Workspace*

7: INFO – INTEGER *Output*

On exit: INFO = 0 unless the routine detects an error (see Section 6).

6 Error Indicators and Warnings

Errors or warnings detected by the routine:

INFO < 0

If INFO = $-i$, the i th parameter had an illegal value. An explanatory message is output, and execution of the program is terminated.

INFO > 0

If INFO = i , $d(i, i)$ is exactly zero; D is singular and the inverse of A cannot be computed.

7 Accuracy

The computed inverse X satisfies a bound of the form

if UPLO = 'U', $|DU^T P^T X P U - I| \leq c(n)\epsilon(|D||U^T|P^T|X|P|U| + |D||D^{-1}|)$;

if UPLO = 'L', $|DL^T P^T X P L - I| \leq c(n)\epsilon(|D||L^T|P^T|X|P|L| + |D||D^{-1}|)$,

$c(n)$ is a modest linear function of n , and ϵ is the **machine precision**.

8 Further Comments

The total number of real floating-point operations is approximately $\frac{8}{3}n^3$.

The real analogue of this routine is F07MJF (DSYTRI).

9 Example

This example computes the inverse of the matrix A , where

$$A = \begin{pmatrix} -0.39 - 0.71i & 5.14 - 0.64i & -7.86 - 2.96i & 3.80 + 0.92i \\ 5.14 - 0.64i & 8.86 + 1.81i & -3.52 + 0.58i & 5.32 - 1.59i \\ -7.86 - 2.96i & -3.52 + 0.58i & -2.83 - 0.03i & -1.54 - 2.86i \\ 3.80 + 0.92i & 5.32 - 1.59i & -1.54 - 2.86i & -0.56 + 0.12i \end{pmatrix}.$$

Here A is symmetric and must first be factorized by F07NRF (ZSYTRF).

9.1 Program Text

```
*      F07NWF Example Program Text
*      Mark 15 Release. NAG Copyright 1991.
*      .. Parameters ..
      INTEGER          NIN, NOUT
      PARAMETER        (NIN=5,NOUT=6)
      INTEGER          NMAX, LDA, LWORK
      PARAMETER        (NMAX=8,LDA=NMAX,LWORK=64*NMAX)
*      .. Local Scalars ..
      INTEGER          I, IFAIL, INFO, J, N
      CHARACTER        UPLO
*      .. Local Arrays ..
      COMPLEX *16      A(LDA,NMAX), WORK(LWORK)
      INTEGER          IPIV(NMAX)
      CHARACTER        CLABS(1), RLABS(1)
*      .. External Subroutines ..
      EXTERNAL         X04DBF, ZSYTRF, ZSYTRI
*      .. Executable Statements ..
      WRITE (NOUT,*) 'F07NWF Example Program Results'
*      Skip heading in data file
      READ (NIN,*)
      READ (NIN,*) N
      IF (N.LE.NMAX) THEN
*
*          Read A from data file
*
*          READ (NIN,*) UPLO
*          IF (UPLO.EQ.'U') THEN
*              READ (NIN,*) ((A(I,J),J=I,N),I=1,N)
*          ELSE IF (UPLO.EQ.'L') THEN
*              READ (NIN,*) ((A(I,J),J=1,I),I=1,N)
*          END IF
*
*          Factorize A
*
*          CALL ZSYTRF(UPLO,N,A,LDA,IPIV,WORK,LWORK,INFO)
*
*          WRITE (NOUT,*)
*          IF (INFO.EQ.0) THEN
*
*              Compute inverse of A
*
*              CALL ZSYTRI(UPLO,N,A,LDA,IPIV,WORK,INFO)
*
*              Print inverse
*
*              IFAIL = 0
*              CALL X04DBF(UPLO,'Nonunit',N,N,A,LDA,'Bracketed','F7.4',
+                  'Inverse','Integer',RLABS,'Integer',CLABS,80,0,
+                  IFAIL)
*              ELSE
*                  WRITE (NOUT,*) 'The factor D is singular'
*              END IF
*          END IF
*
*          END

```

9.2 Program Data

F07NWF Example Program Data

```

4                                     :Value of N
'L'                                 :Value of UPLO
(-0.39,-0.71)
( 5.14,-0.64) ( 8.86, 1.81)
(-7.86,-2.96) (-3.52, 0.58) (-2.83,-0.03)
( 3.80, 0.92) ( 5.32,-1.59) (-1.54,-2.86) (-0.56, 0.12) :End of matrix A

```

9.3 Program Results

F07NWF Example Program Results

```

Inverse
                                     1               2               3               4
1  (-0.1562,-0.1014)
2  ( 0.0400, 0.1527) ( 0.0946,-0.1475)
3  ( 0.0550, 0.0845) (-0.0326,-0.1370) (-0.1320,-0.0102)
4  ( 0.2162,-0.0742) (-0.0995,-0.0461) (-0.1793, 0.1183) (-0.2269, 0.2383)

```
