

# SIMULATING RELATIVISTIC PLASMAS IN HIGH ENERGY ASTROPHYSICS: THE CASE OF PULSAR WIND NEBULAE

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INAF

PLUS  
Collaboration

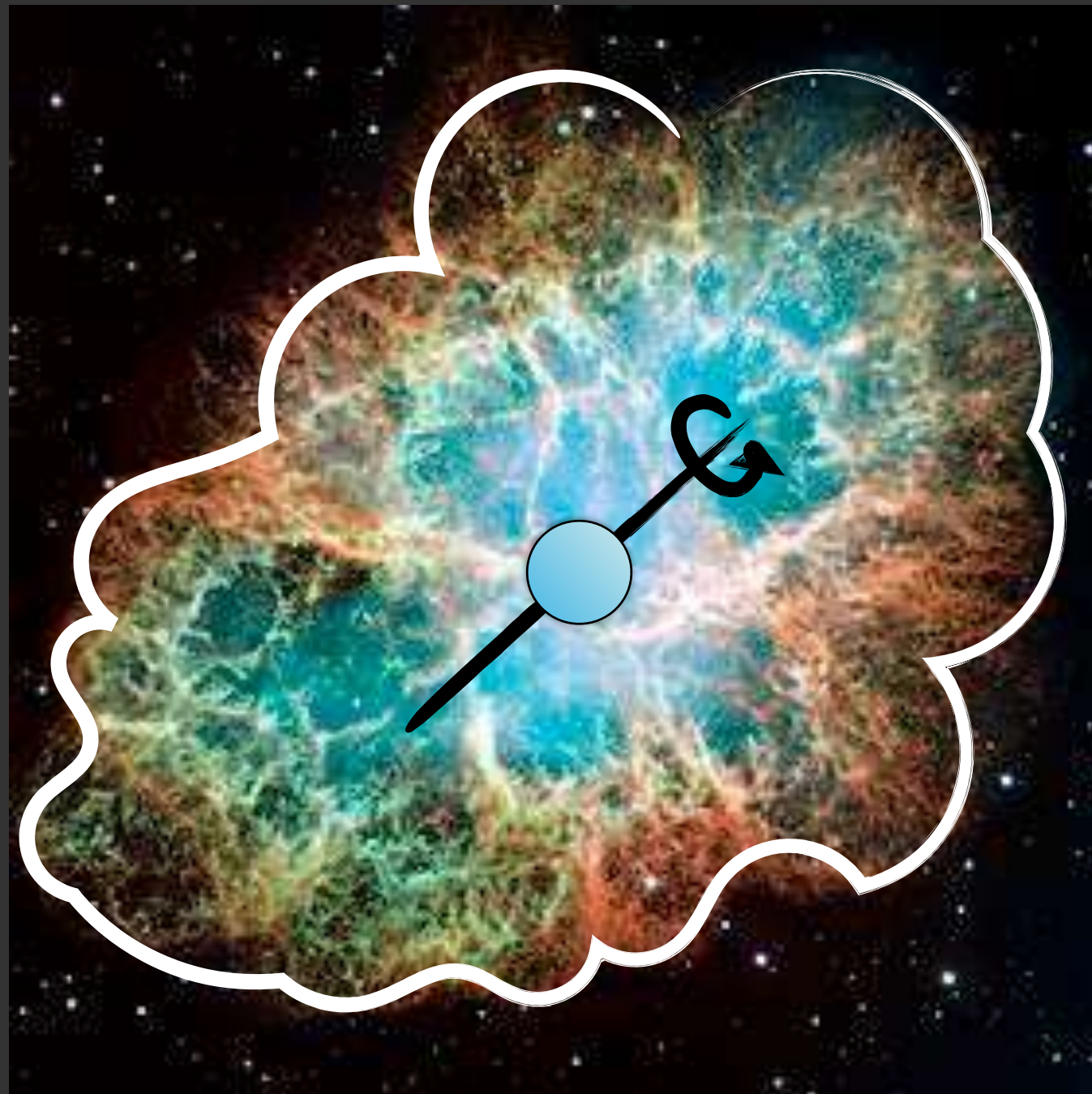
Plasma in Laboratory and Universe Systems



Webinar  
Dec. 17 2021

# WHAT IS A PWN?

The debris of the supernova explosion of a massive star  $\gtrsim 8 M_{\odot}$



[NOT IN SCALE!!]

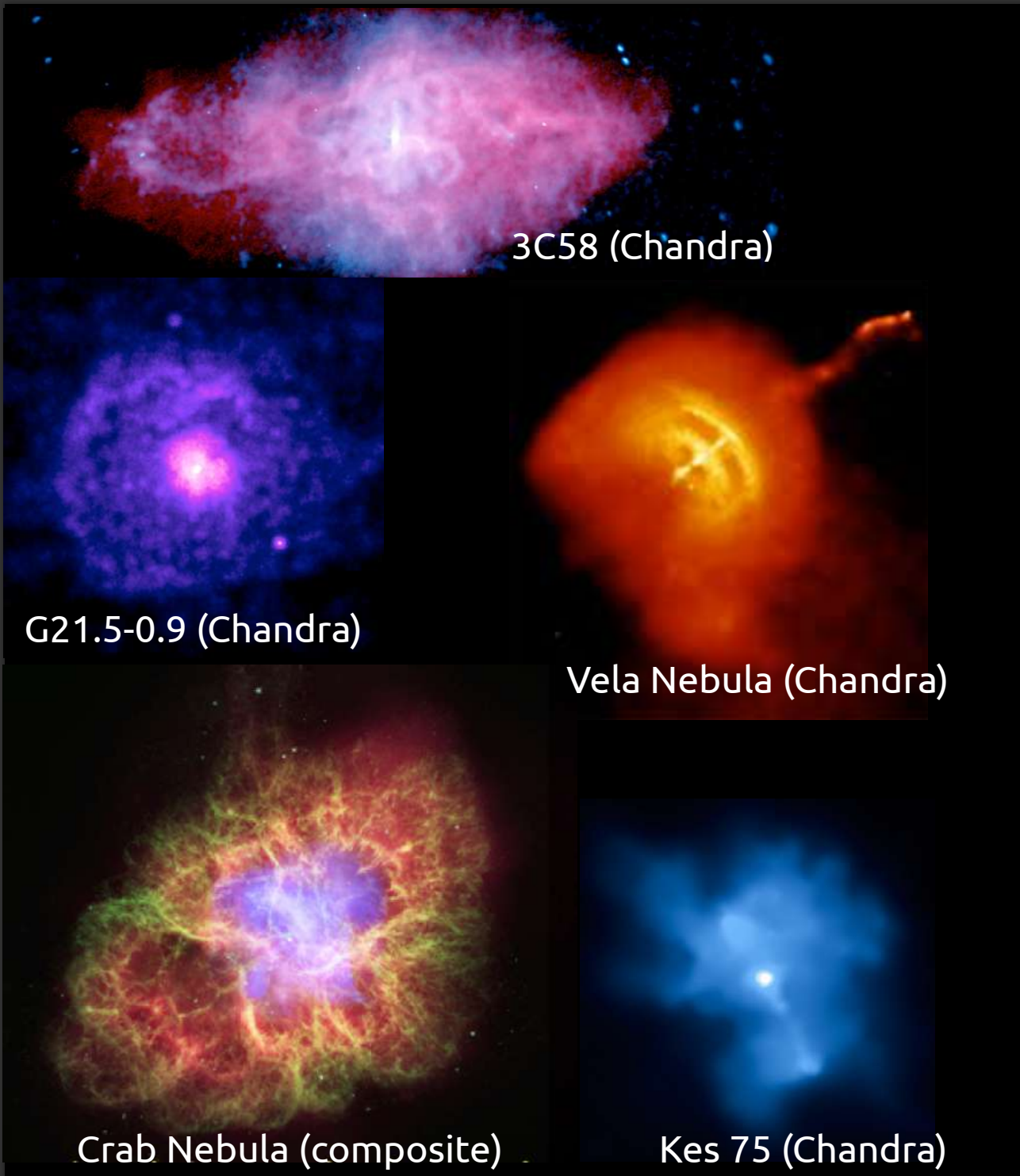
## MAIN INGREDIENTS

- a rapidly rotating neutron star (PULSAR)
- ejecta of the stellar explosion

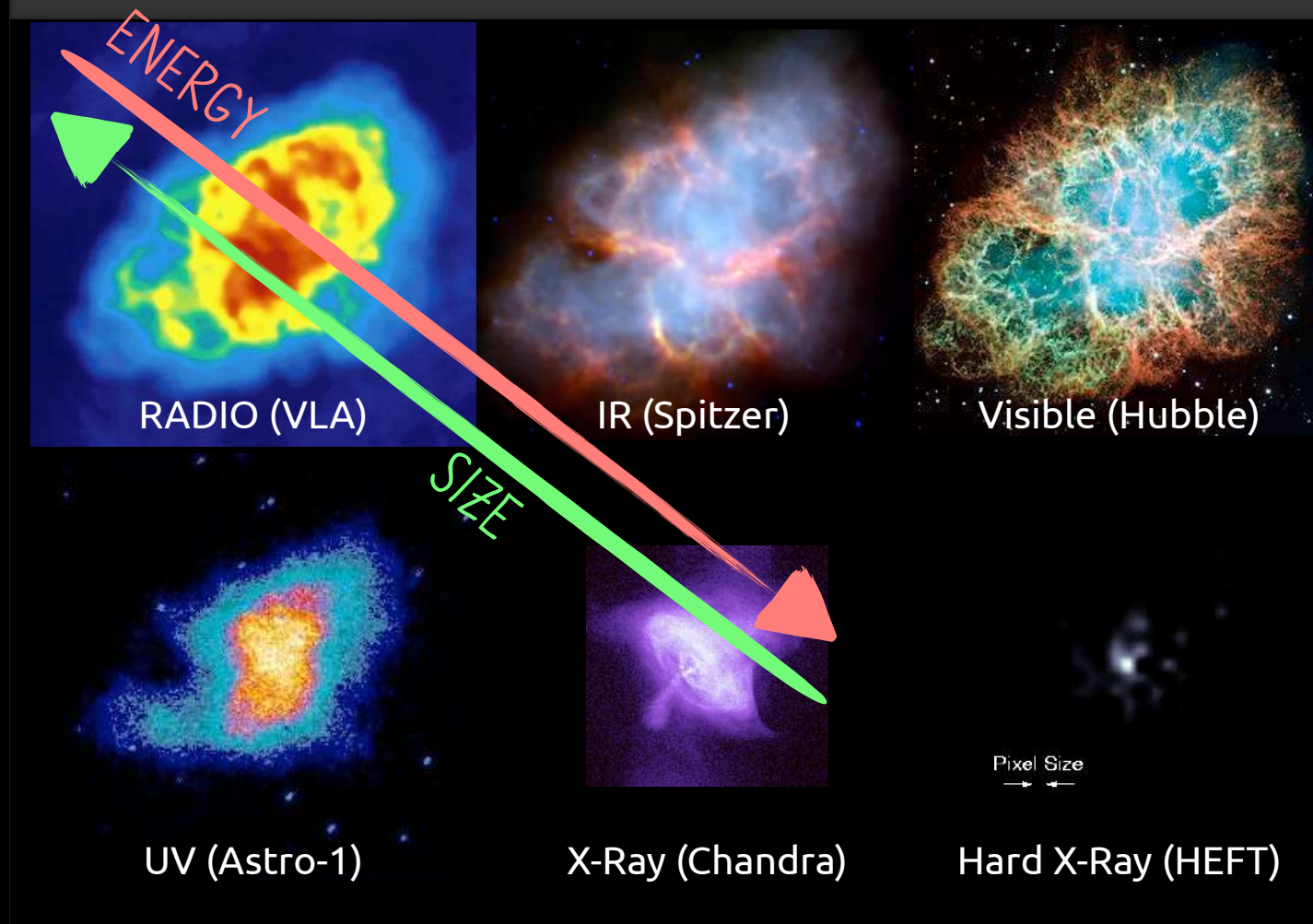
# HOW THEY LOOK?

## EMISSION MORPHOLOGY AT MULTI-WAVELENGTHS

Fill-centered morphology

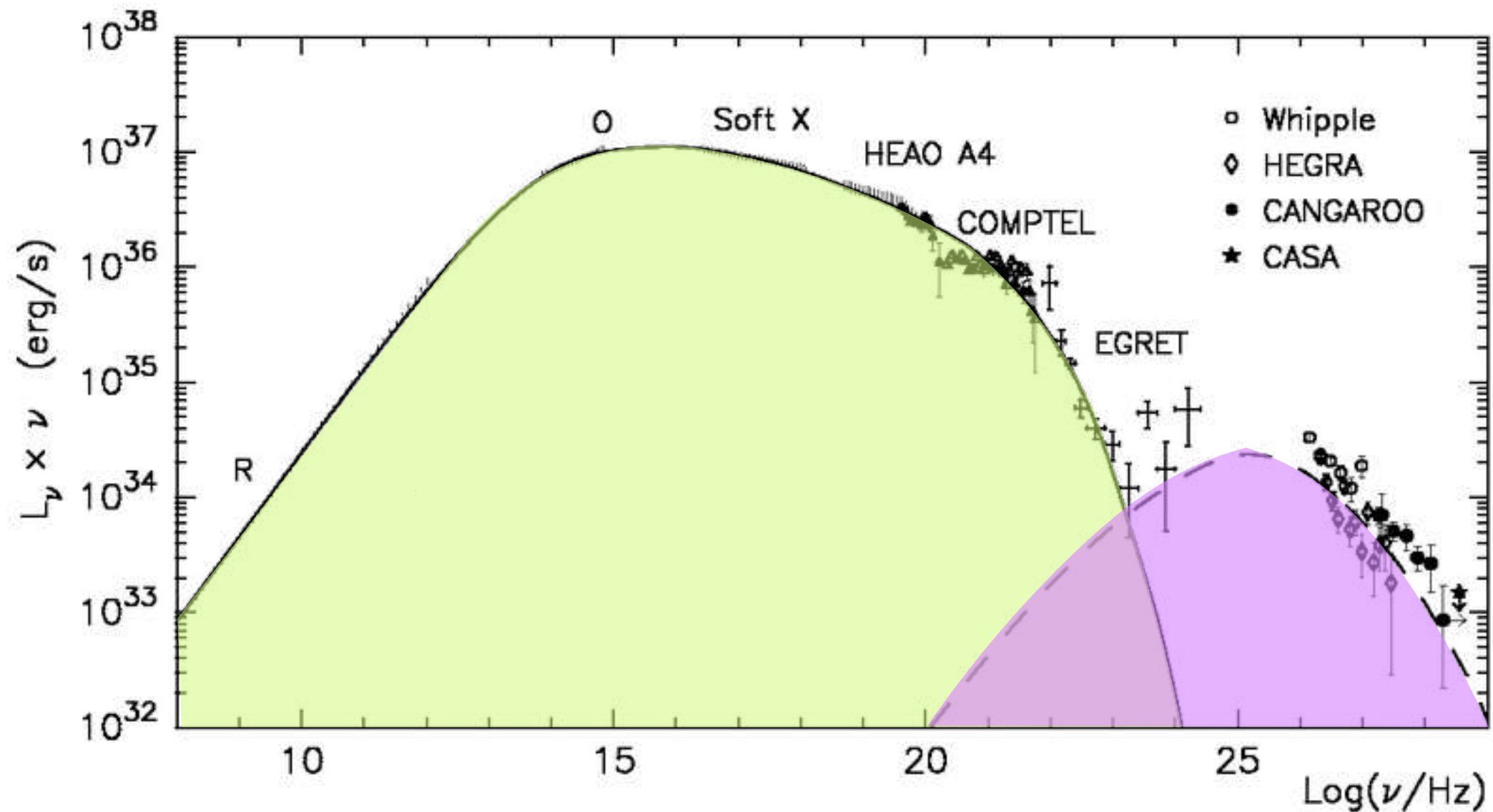


Decreasing size with energy



# BROAD BAND NON-THERMAL SPECTRUM

CRAB NEBULA spectrum [adapted from Atoyan & Aharonian 1996]



Primary mechanism: **synchrotron radiation** by relativistic particles in the nebular magnetic field

Gamma-rays: **Inverse Compton scattering** with local photon field

# WHY THEY ARE INTERESTING?

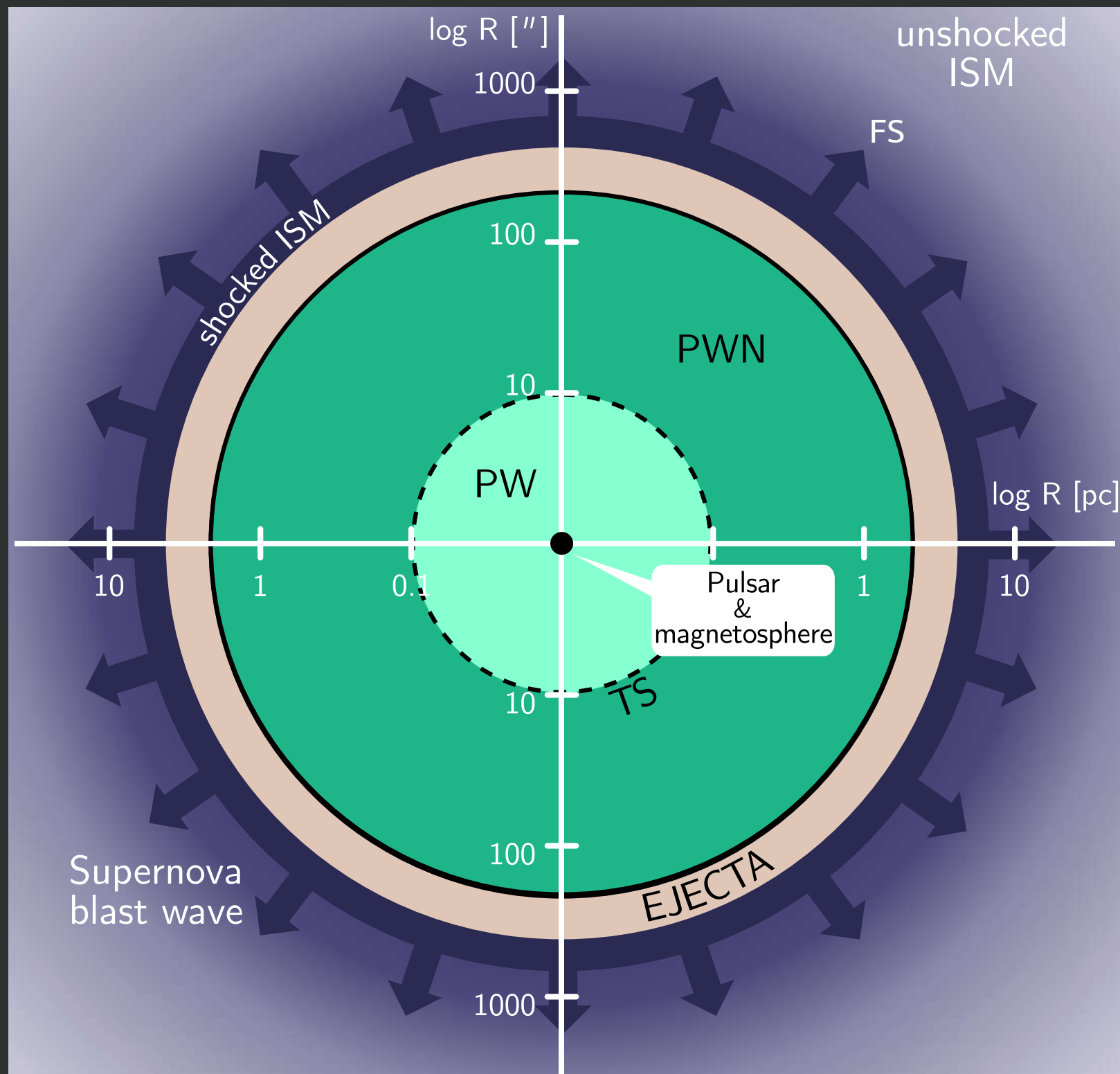
They enclose most of the energy lost by the pulsar → PULSAR PHYSICS

Extreme conditions of the plasma in close and bright sources → PLASMA PHYSICS

Evidence of particle acceleration up to PeV → PARTICLE ACCELERATION IN EXTREME ENVIRONMENTS

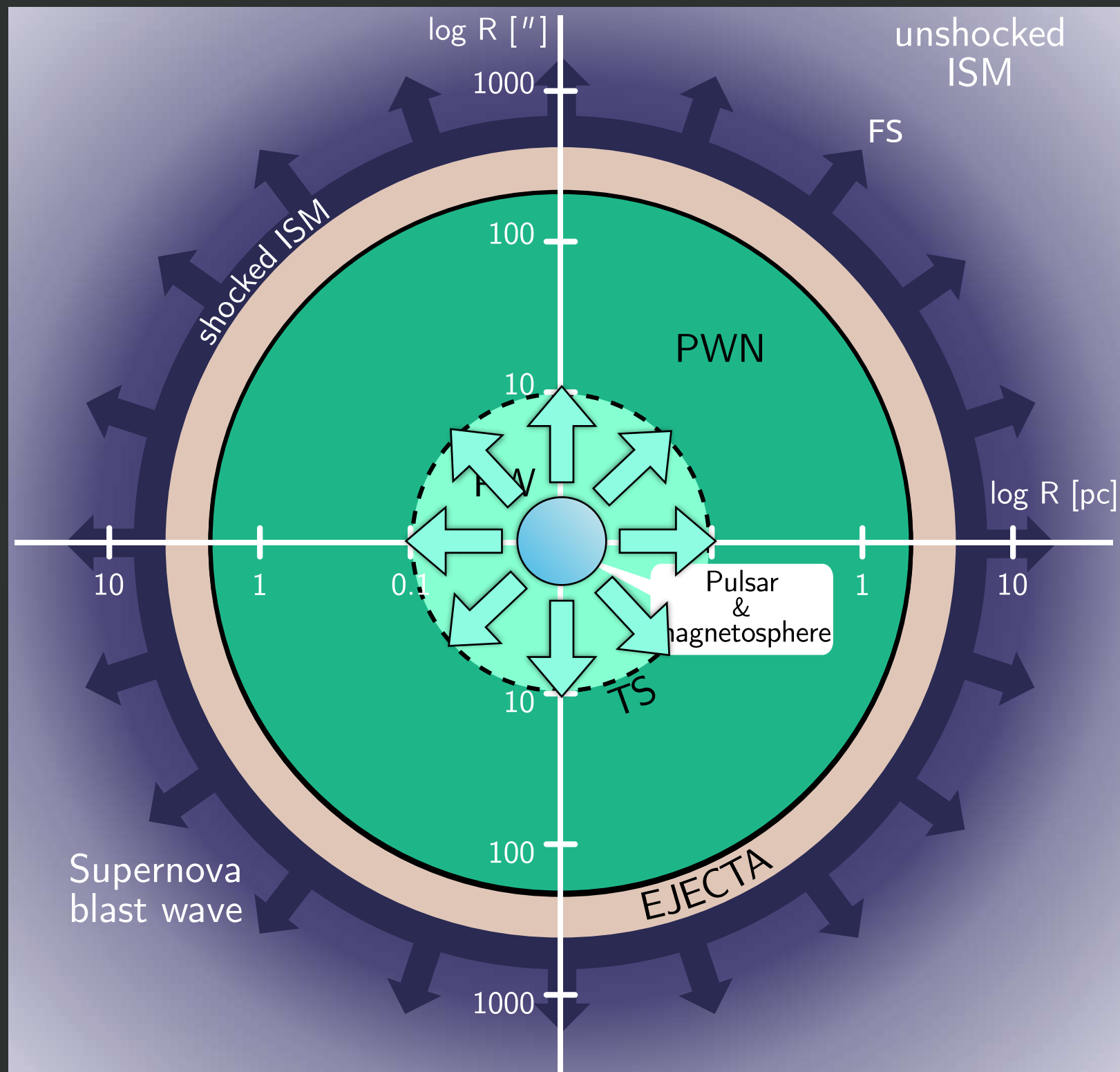
Escape of particles → ROLE OF PULSARS AS GALACTIC ANTIMATTER FACTORIES  
(SOURCE OF CR POSITRON EXCESS?)

# BASIC PICTURE FOR YOUNG SYSTEMS



Adapted from Kennel & Coroniti 1984  
[Del Zanna & Olmi 2017]

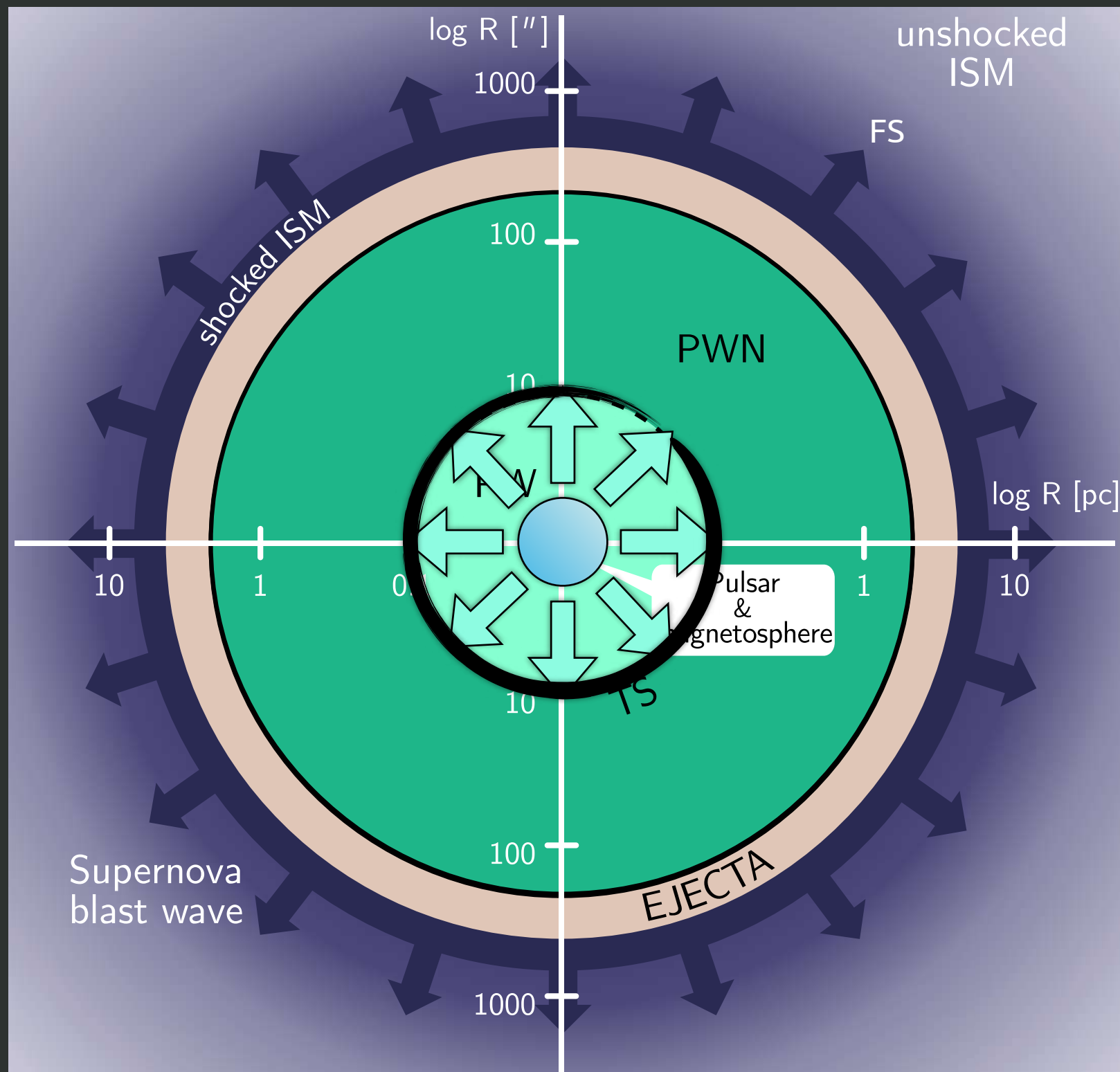
# BASIC PICTURE FOR YOUNG SYSTEMS



The central pulsar is both source of magnetic field and particles: it fills the remnant with a magnetized, relativistic and cold plasma (mainly or fully leptonic)

Adapted from Kennel & Coroniti 1984  
[Del Zanna & Olmi 2017]

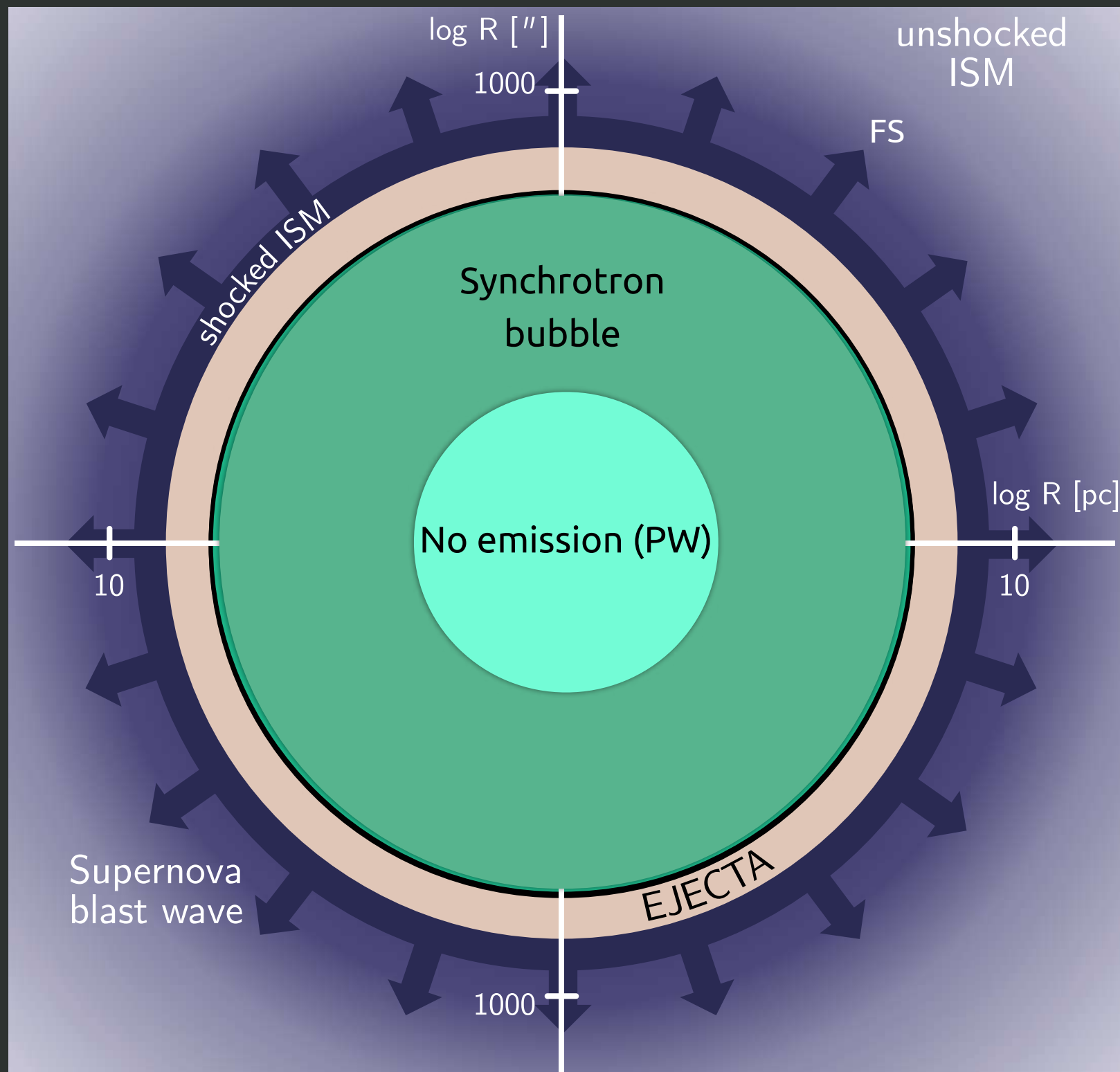
# BASIC PICTURE FOR YOUNG SYSTEMS



Interaction of the pulsar wind with the SNR induces the formation of a Termination shock

Adapted from Kennel & Coroniti 1984  
[Del Zanna & Olmi 2017]

# BASIC PICTURE FOR YOUNG SYSTEMS



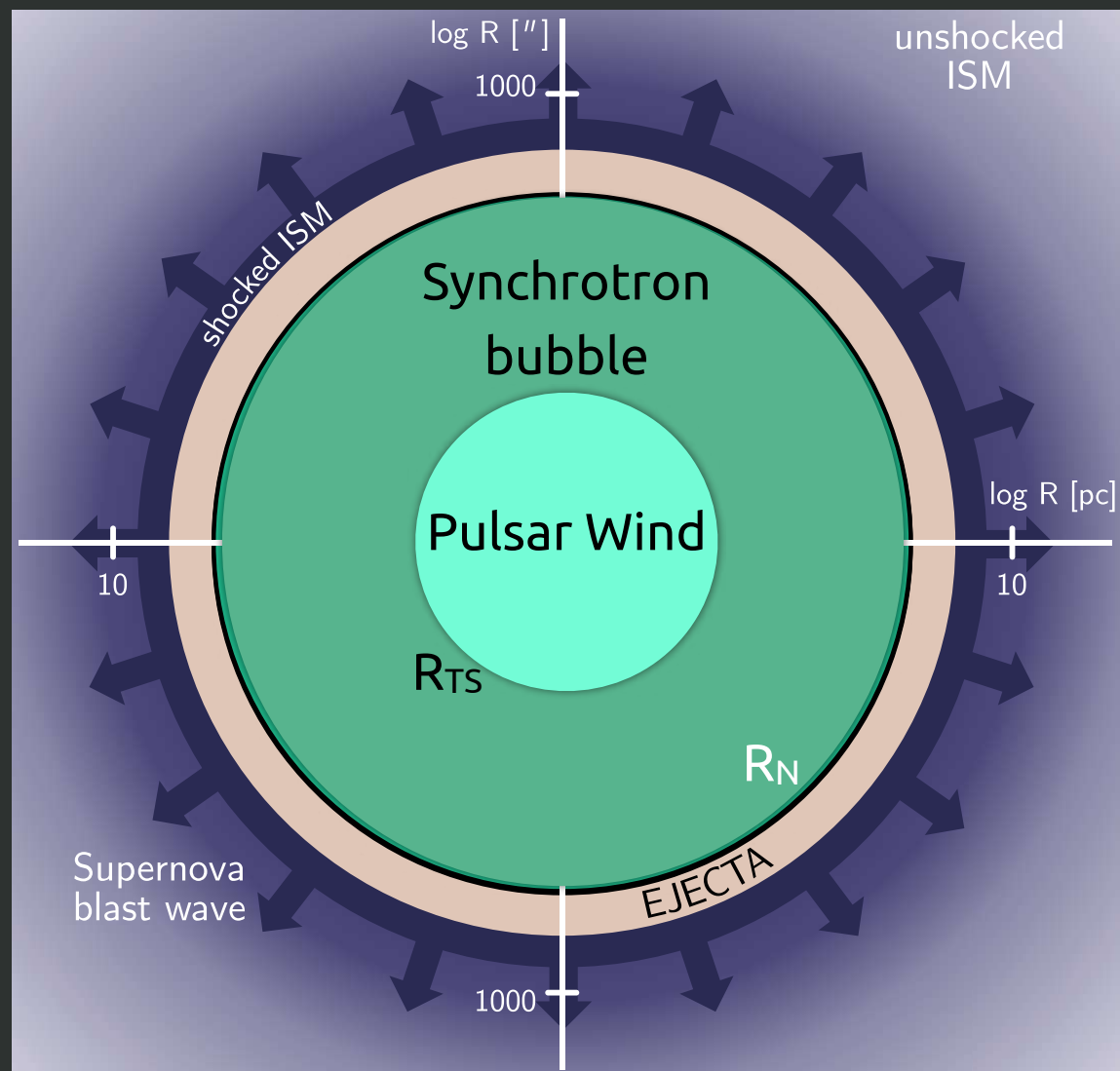
The visible nebula corresponds to the shocked wind beyond the TS.

The PWN bubble is formed by a hot plasma and intense magnetic field (50-200  $\mu\text{G}$ )

Adapted from Kennel & Coroniti 1984  
[Del Zanna & Olmi 2017]

# 1D/2D STATIC MODELS OF PWNE

[Rees & Gunn 1974, Kennel & Coroniti 1984, Emmering & Chevalier 1987, Begelman & Li 1992]



## ASSUMPTIONS:

- the cold isotropic relativistic PW terminates in a strong perpendicular shock
- the flow in the nebula is subsonic
- particle acceleration at the shock
- synchrotron losses beyond the shock

## MAIN FREE PARAMETERS:

- particle spectral indices
- wind Lorentz factor  $\rightarrow \Gamma$
- wind magnetization  $\rightarrow \sigma = B^2 / (4\pi n m_e c^2 \Gamma^2)$

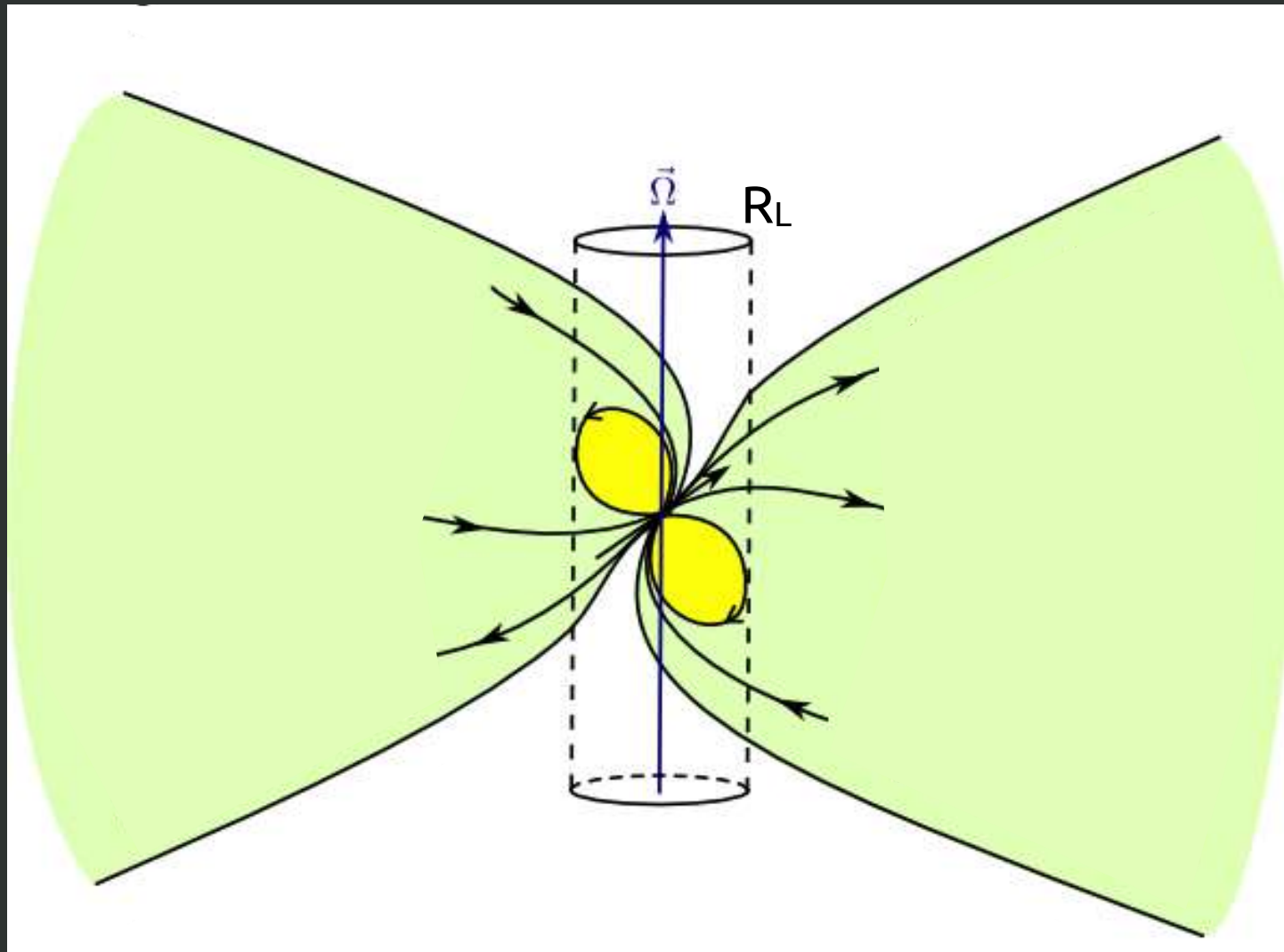
## PREDICTIONS:

- position of TS  $\rightarrow R_{TS} \sim R_N (V_N/c)^{1/2} \sim 0.1 \text{ pc}$
- Optical / X-ray spectrum [de Jager & Harding 1992, Atoyan & Aharonian 1996]
- size shrinkage with increasing energy

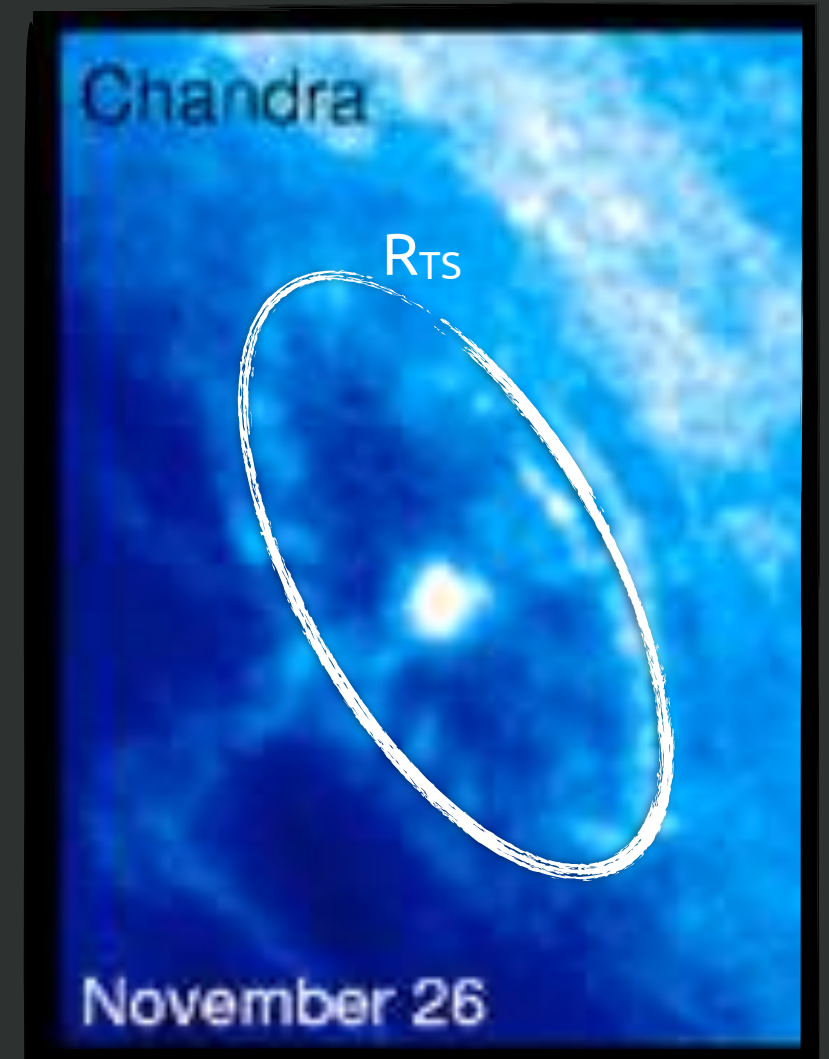
$\Gamma \simeq 10^6$   
 $\sigma \simeq V_N/c \simeq 10^{-3}$

# THE SIGMA PARADOX

From pulsar theories  $\rightarrow \sigma \sim 10^4$  @  $R_L$



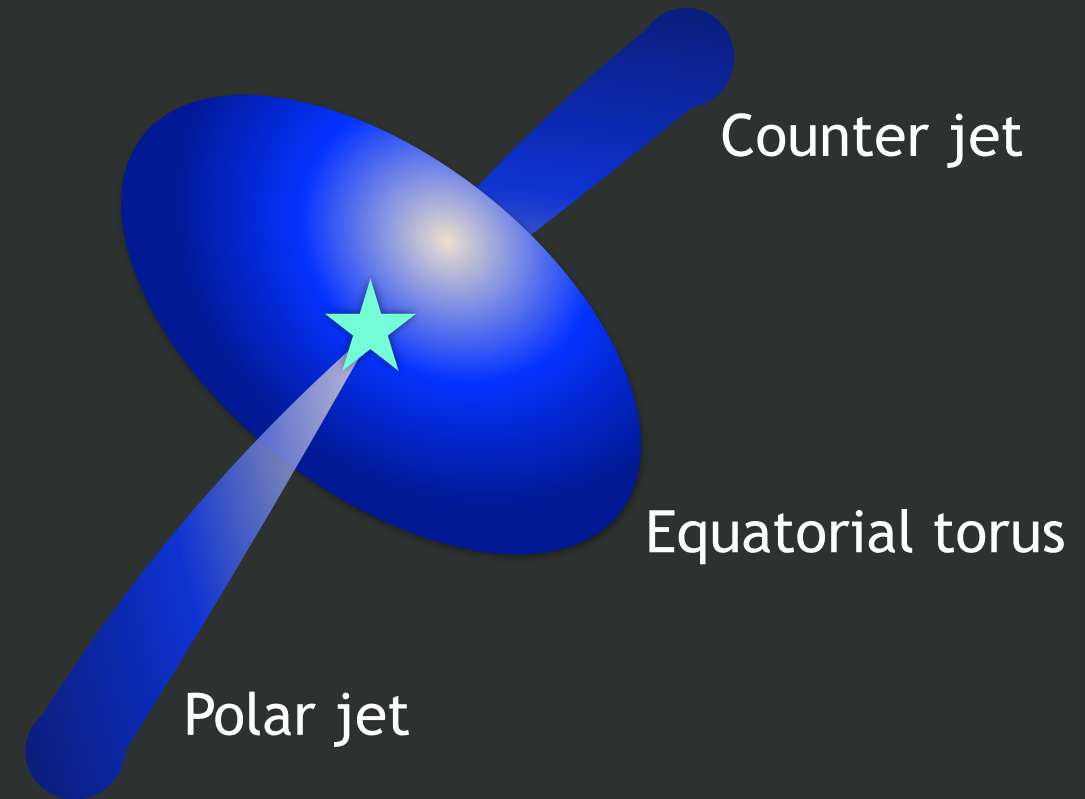
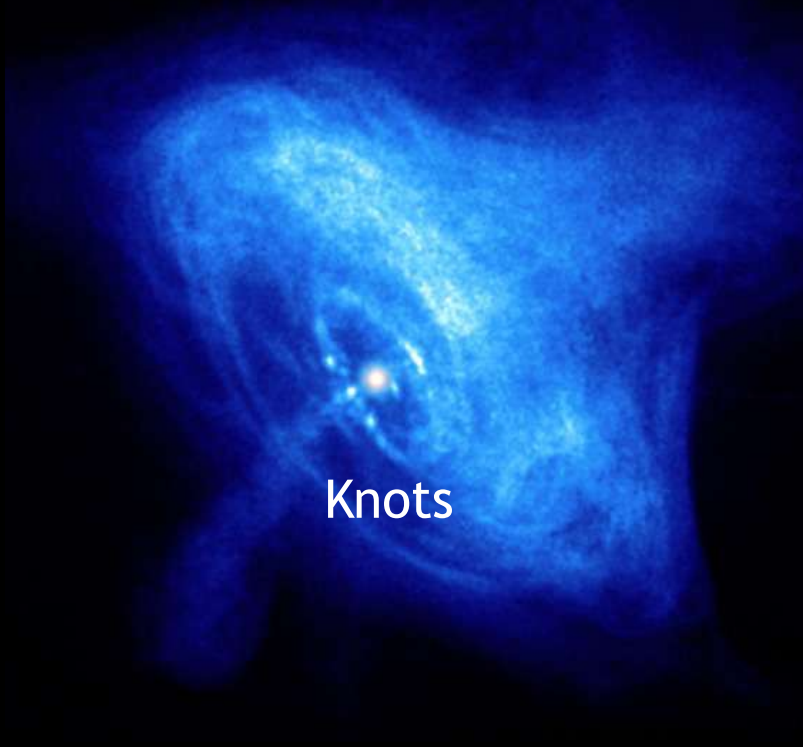
From 1D PWNe models  $\rightarrow \sigma \sim 10^{-3}$  @  $R_{TS}$



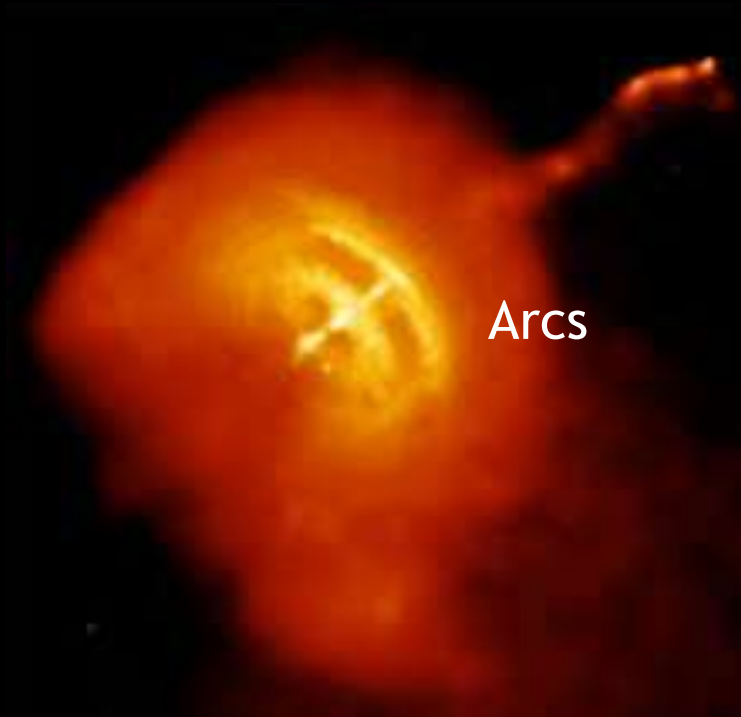
Even if  $R_{TS} \sim 10^9 R_L$  dissipation is not sufficient to explain this discrepancy!

# A DEEPER VIEW: THE INNER NEBULA HAS A JET-TORUS SHAPE

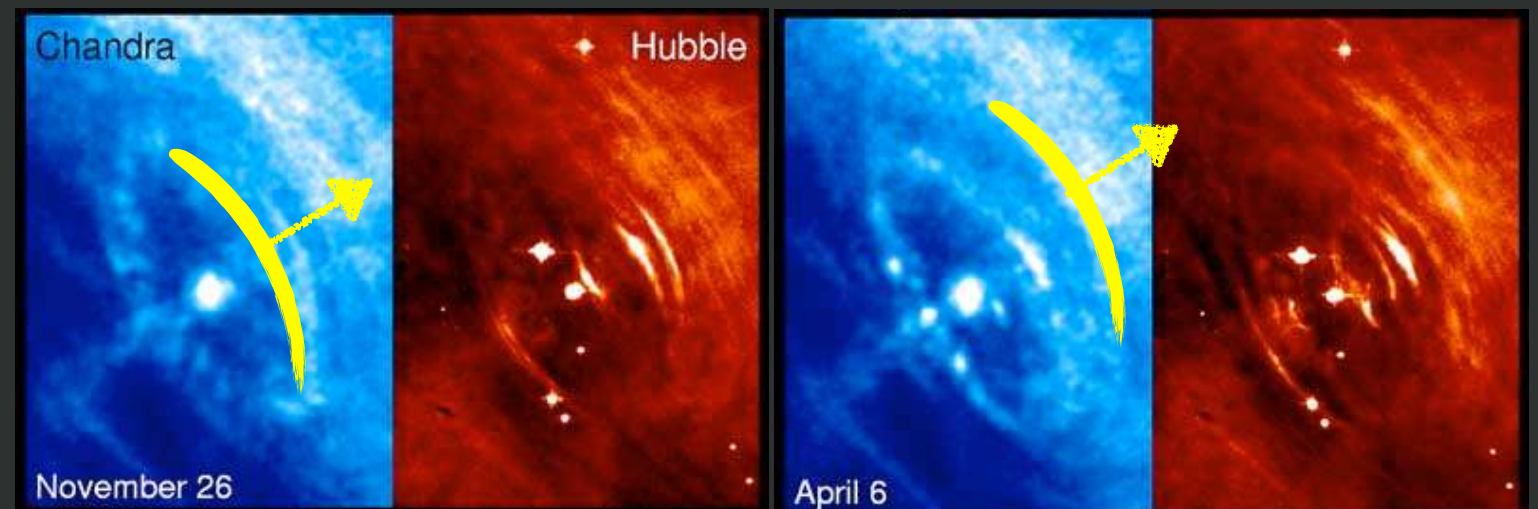
[Crab Nebula - Chandra]



AND SHOWS HIGH VARIABILITY

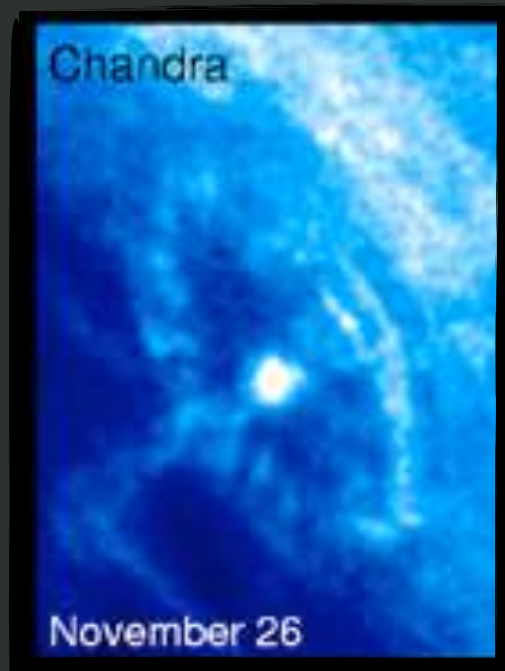


[Vela Nebula - Chandra]

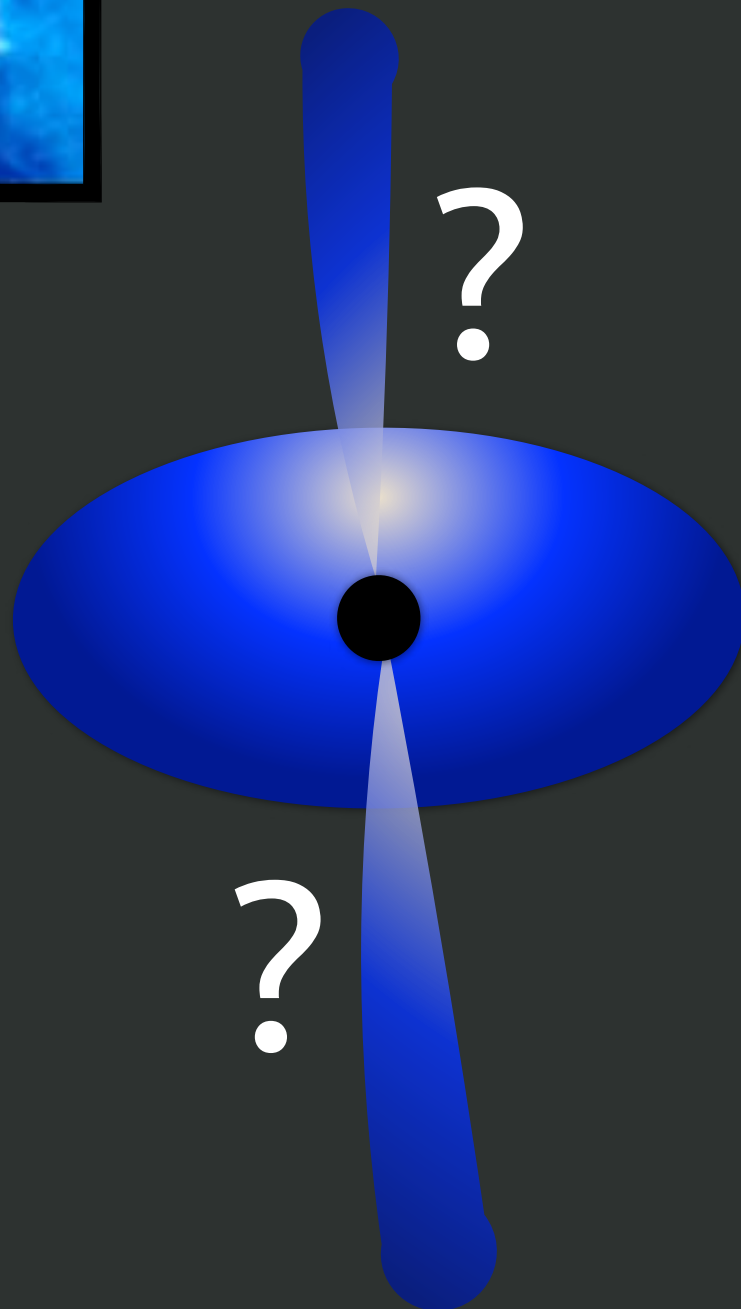


Outward moving wisps

# HOW POLAR JETS FORMS?



Jets appear to originate very close to the pulsar



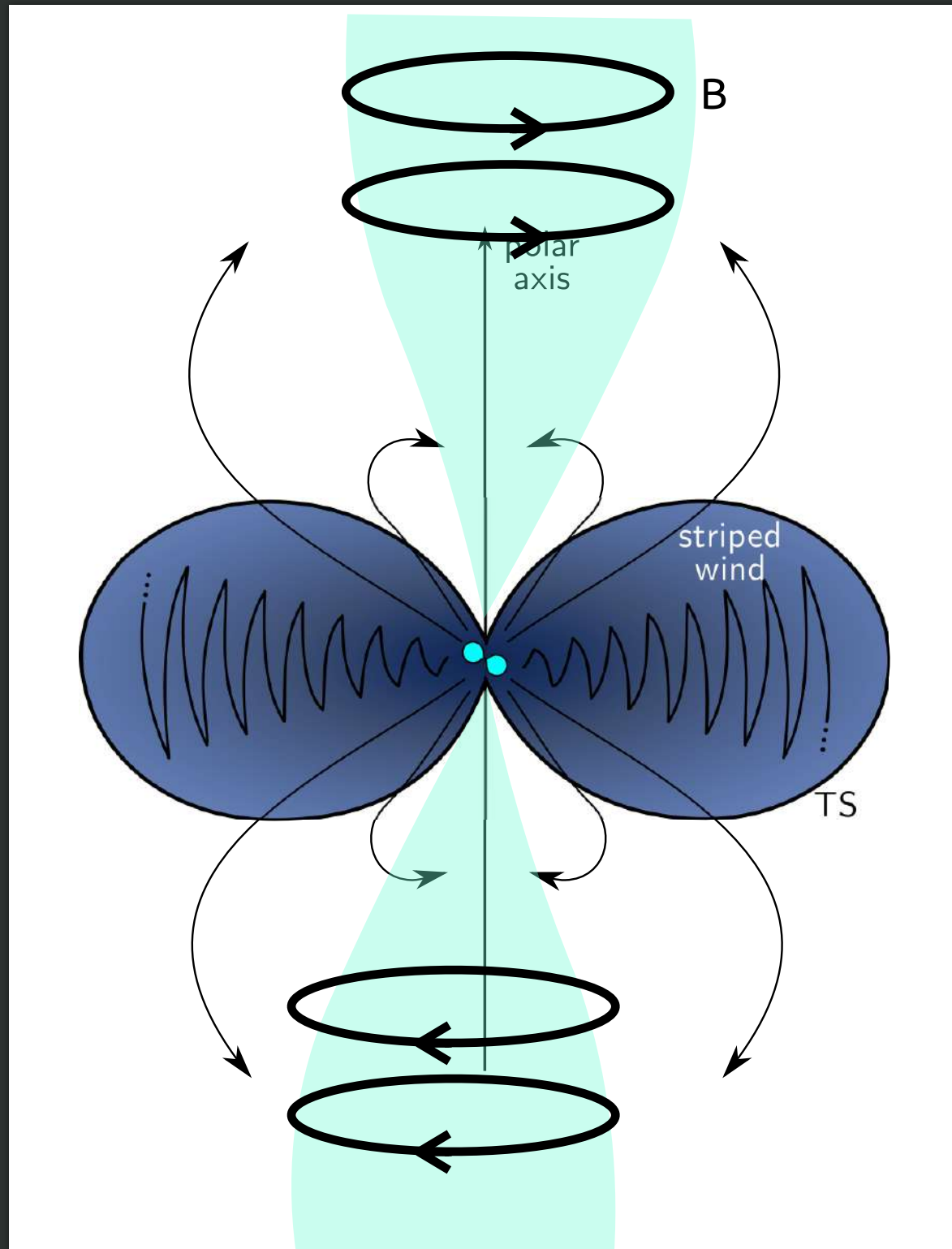
But magnetic **collimation** in the relativistic PW is **not efficient** [Lyubarsky & Eichler 2001]:

$$\Gamma \gg 1 \rightarrow \rho \vec{E} + \vec{J} \times \vec{B} \sim 0$$



Collimation must occur in the shocked plasma (in the nebula, NOT in the wind)

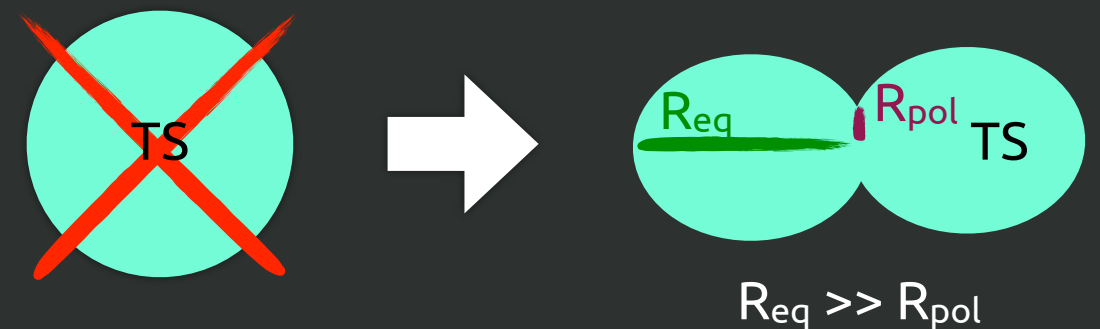
# FORMATION OF THE POLAR JETS: THE ANISOTROPIC WIND



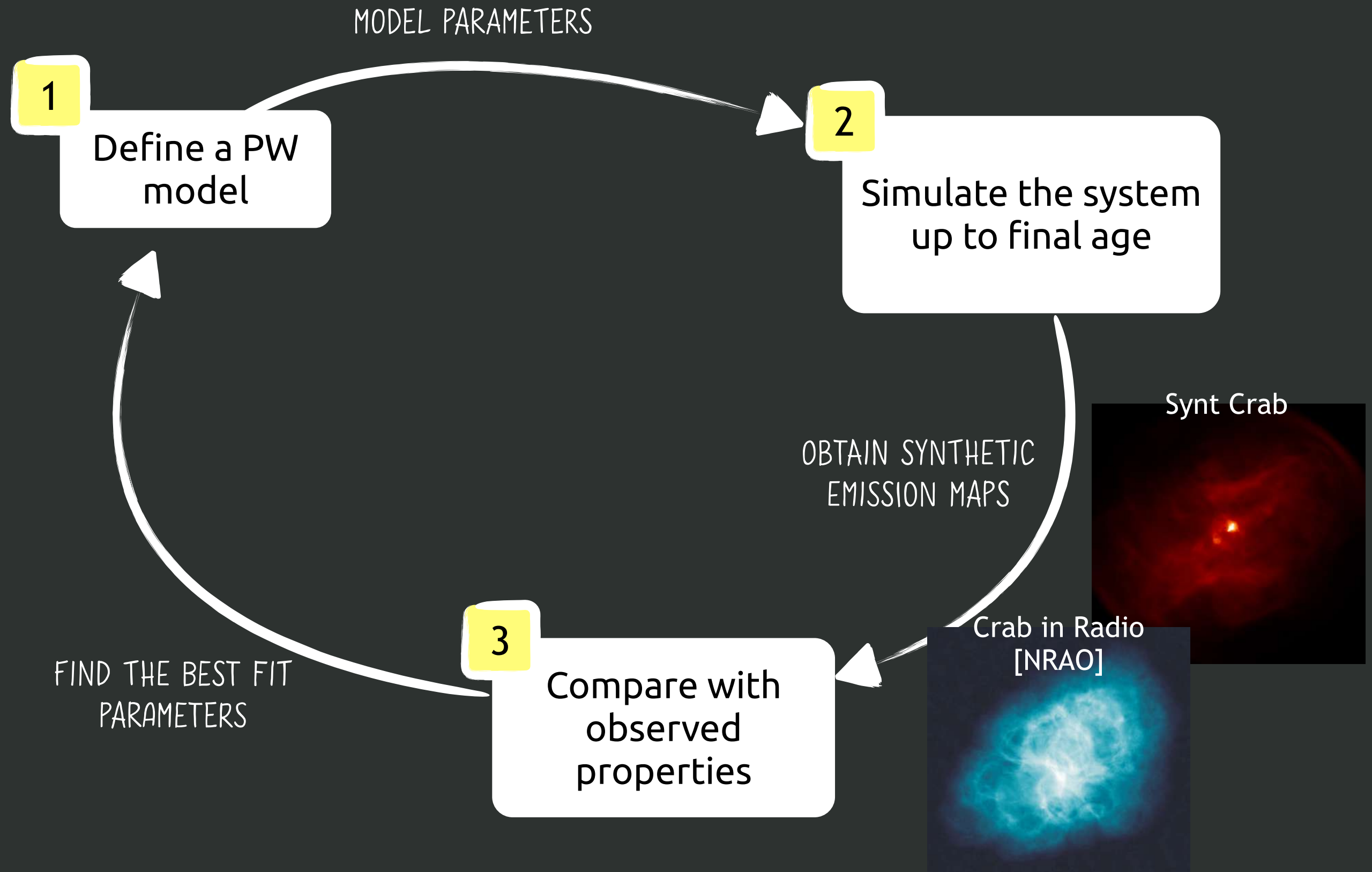
The energy flux in the nebula is anisotropic!  
[Bogovalov & Khangoulia 2002, Lyubarsky 2002]

$$F \propto \sin^2(\theta)$$

This account for the apparent vicinity of the jets to the pulsar: the TS is oblate!



# SCHEME OF A PWNE NUMERICAL MODEL



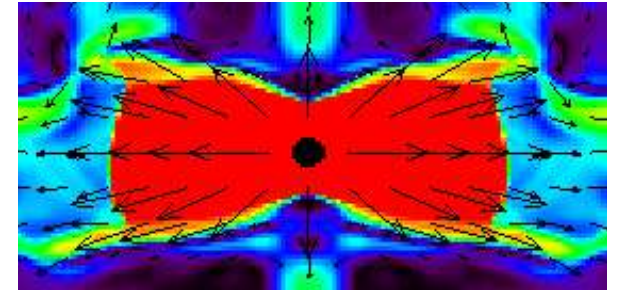
# MODELING THE PULSAR WIND

Anisotropic distribution of the energy flux  $F(r, \theta)$ :

$$F(r, \theta) \propto \frac{\alpha + (1 - \alpha) \sin^2 \theta}{(2 + \alpha) r^2} \rightarrow F(r, \pi/2) \gg F(r, 0) \rightarrow \alpha \ll 1$$

anisotropy parameter

Oblate TS, with  $R_{\text{eq}} \gg R_{\text{pol}}$

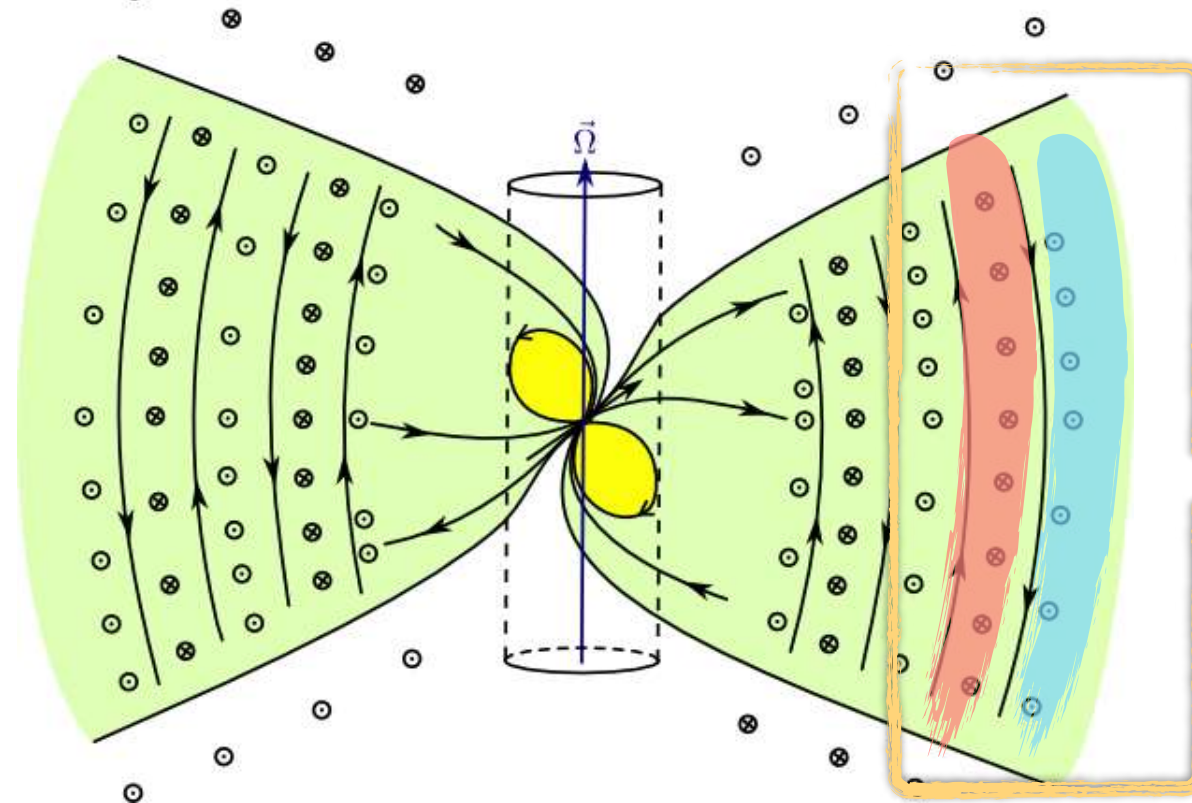


Striped morphology within an equatorial belt of extension  $\approx 2 \times \zeta$

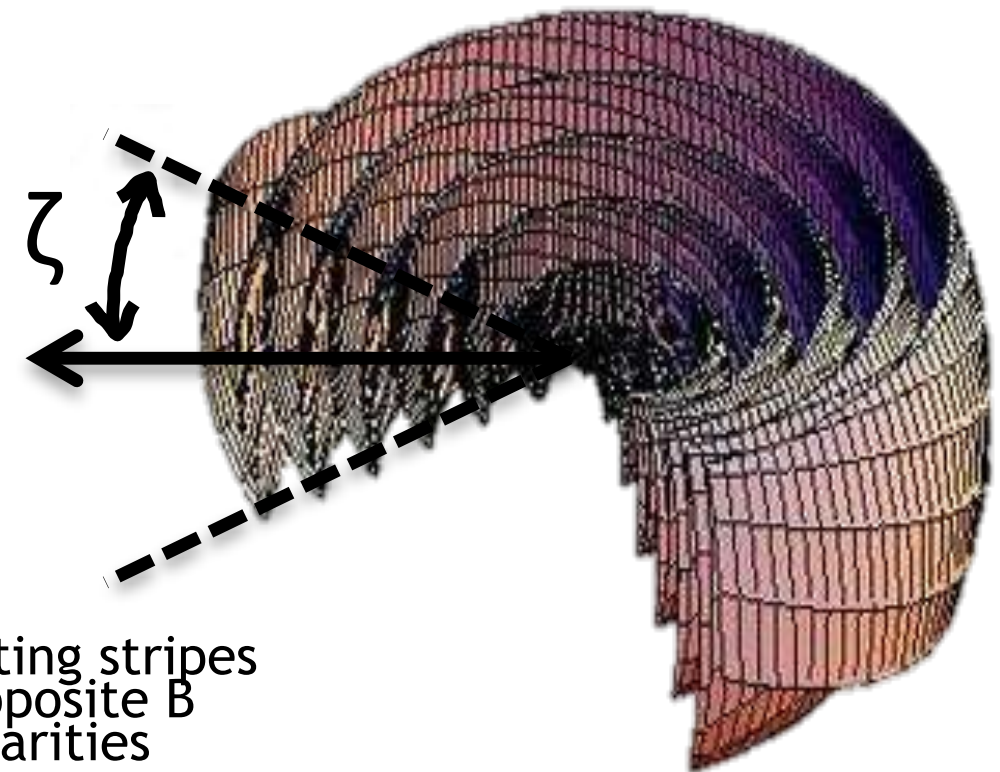
$$B(r, \theta) \propto \sqrt{\sigma} \mathcal{G}(\theta) \sin \theta$$

initial wind magnetization

striped wind



alternating stripes of opposite B polarities

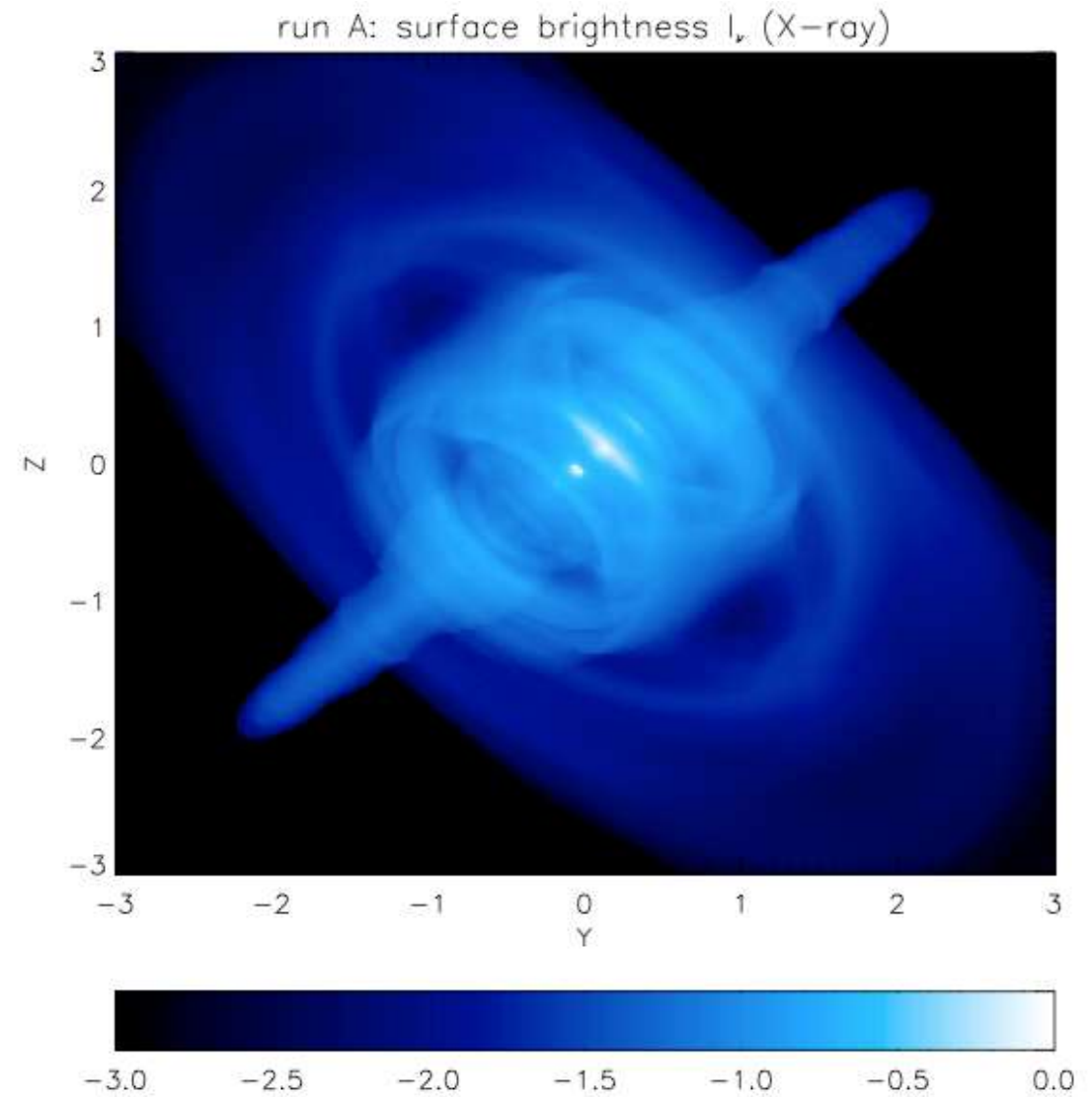
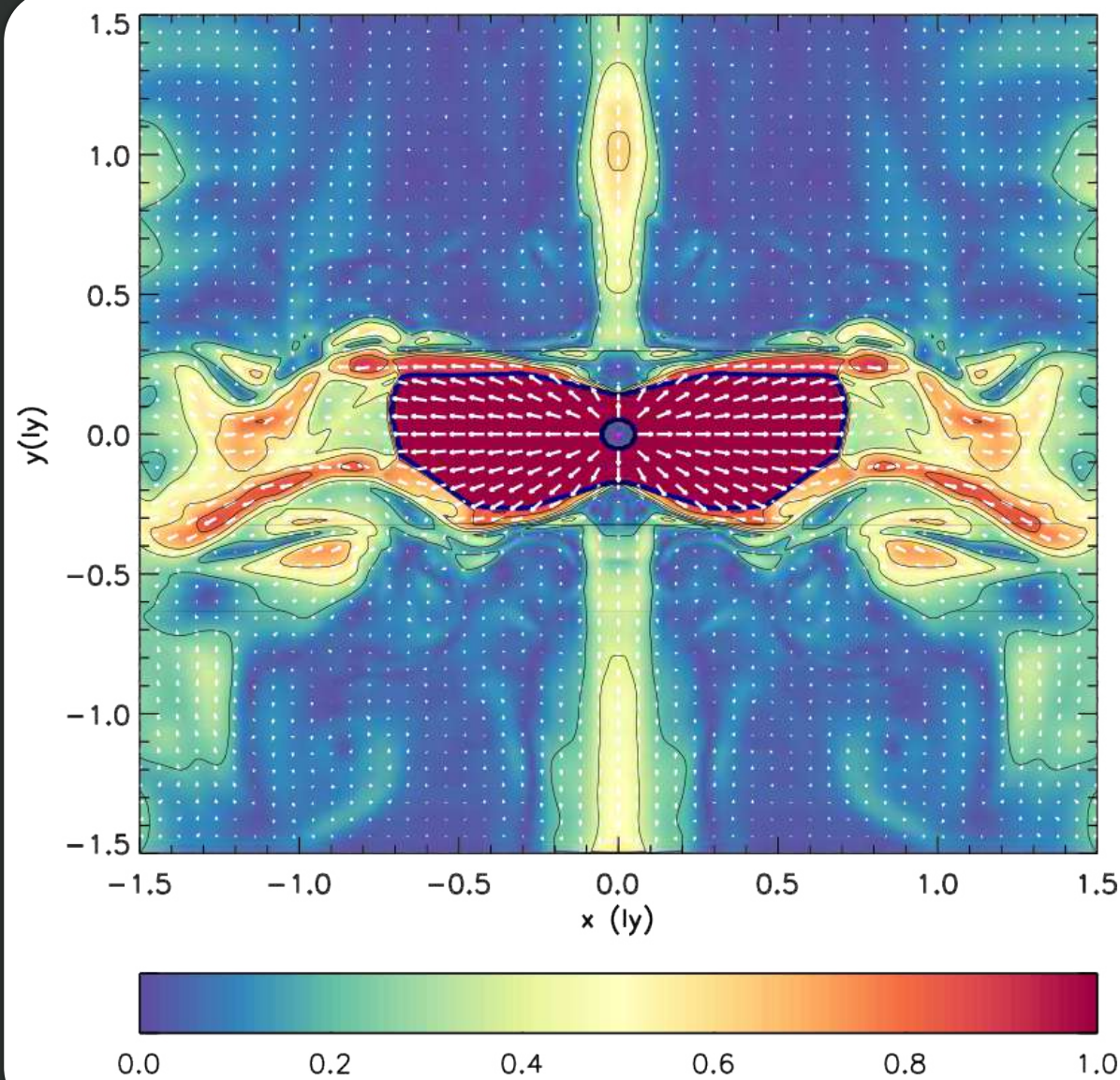


separated by a current sheet  $\rightarrow$  place for dissipation

# GOALS OF 2D MODELS: JET-TORUS

2D numerical models confirm the jet formation for values of magnetization  $\sigma \gtrsim 0.01$

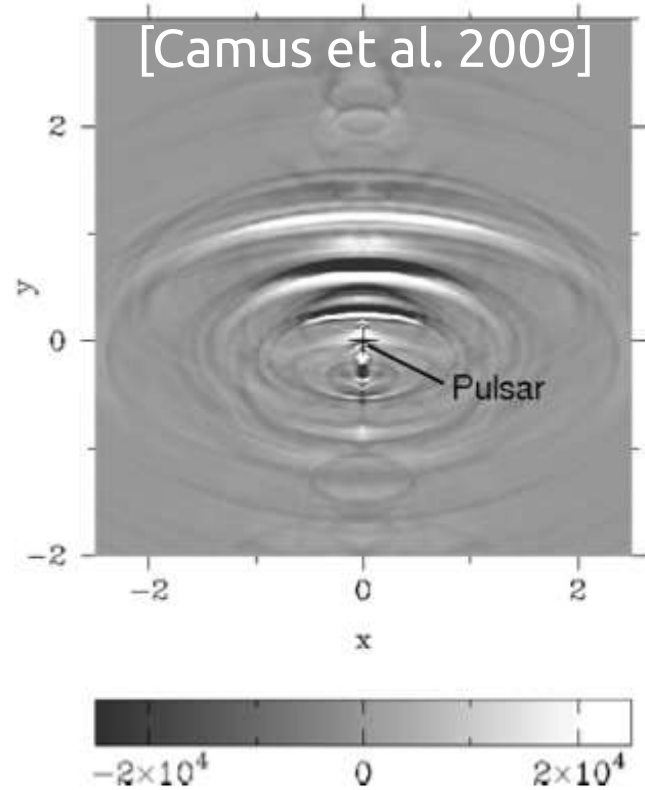
[Komissarov & Lyubarsky 2003-2004, Del Zanna et al. 2004]



# GOALS OF 2D MODELS: VARIABILITY OF THE INNER NEBULA

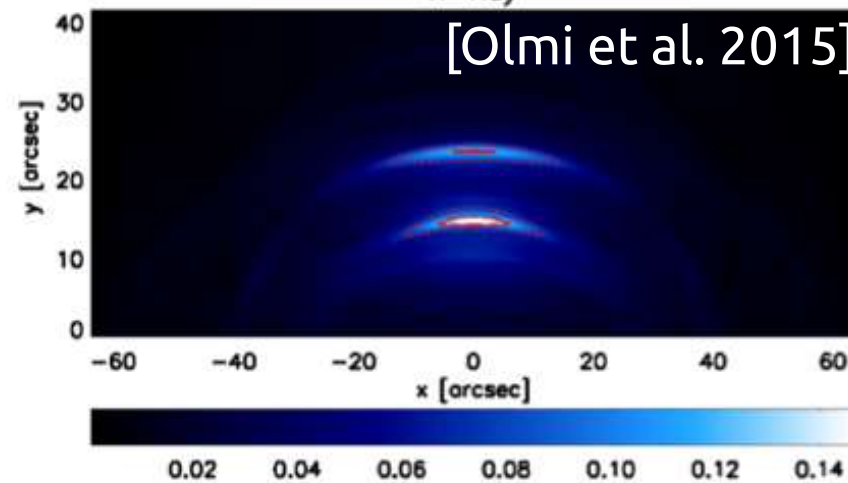
X-rays (105 days)

[Camus et al. 2009]

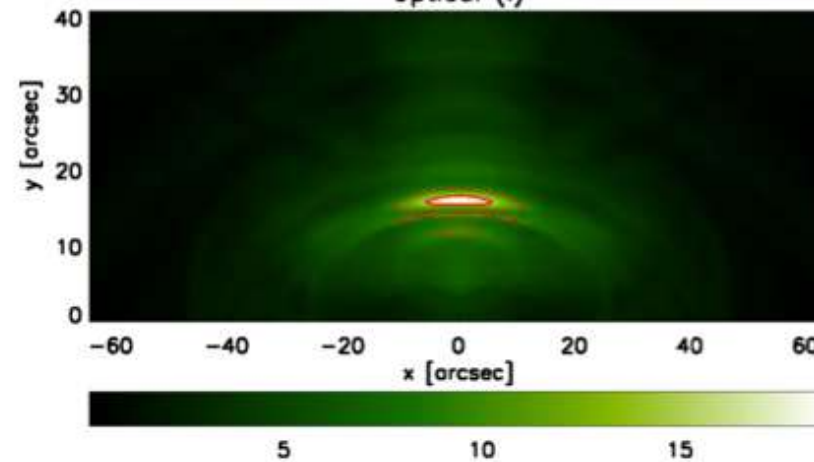


X-Ray

[Olmi et al. 2015]



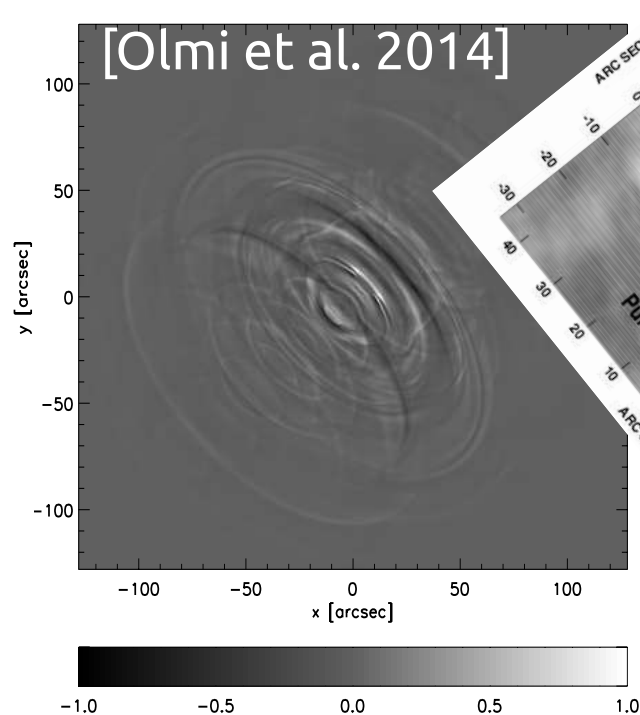
Optical (I)



Wisps variability reproduced  
at multi-wavelengths

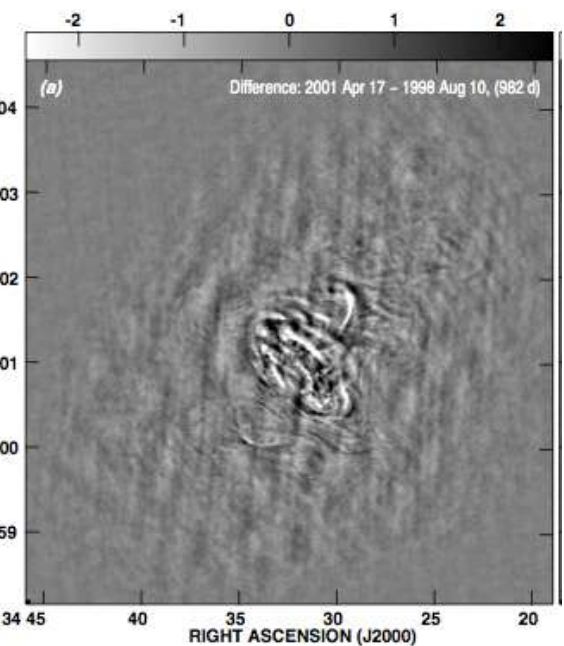
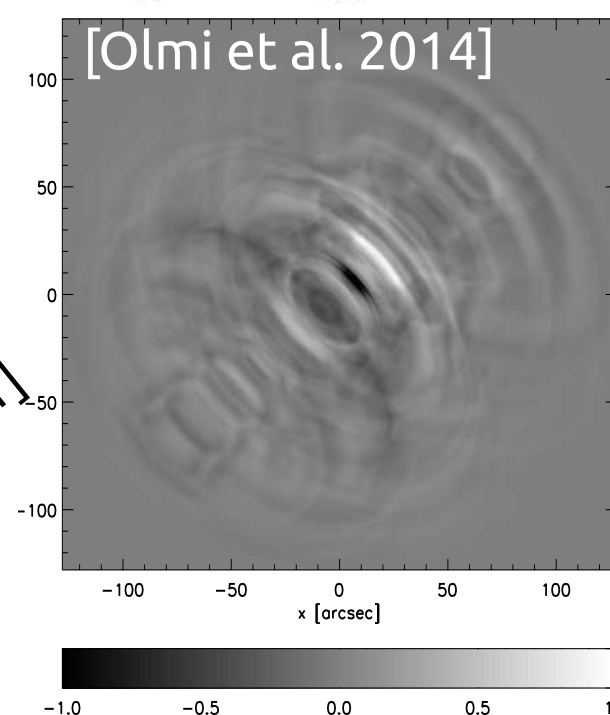
Radio (2 months)

[Olmi et al. 2014]



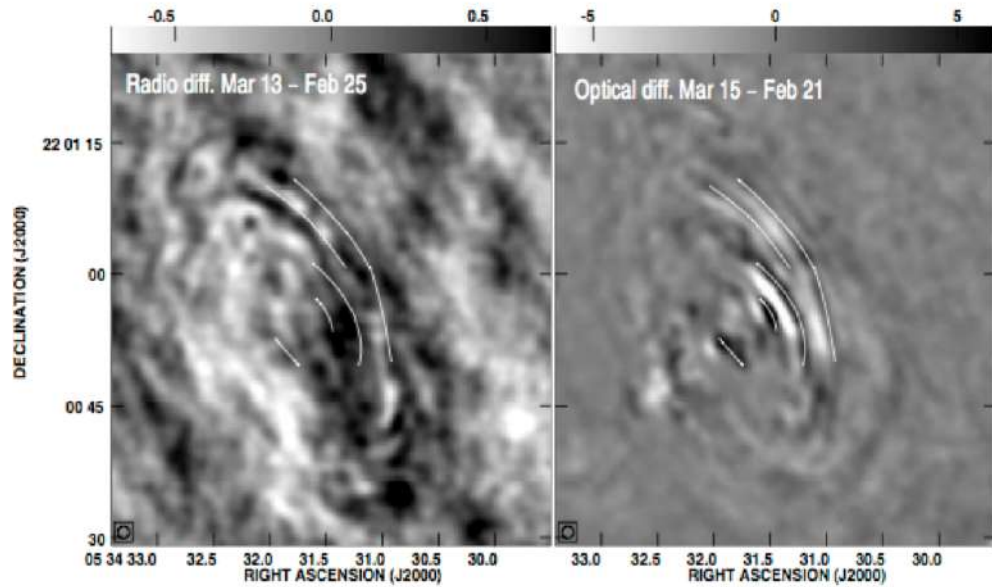
[Bietenholz et al. 01]

[Olmi et al. 2014]



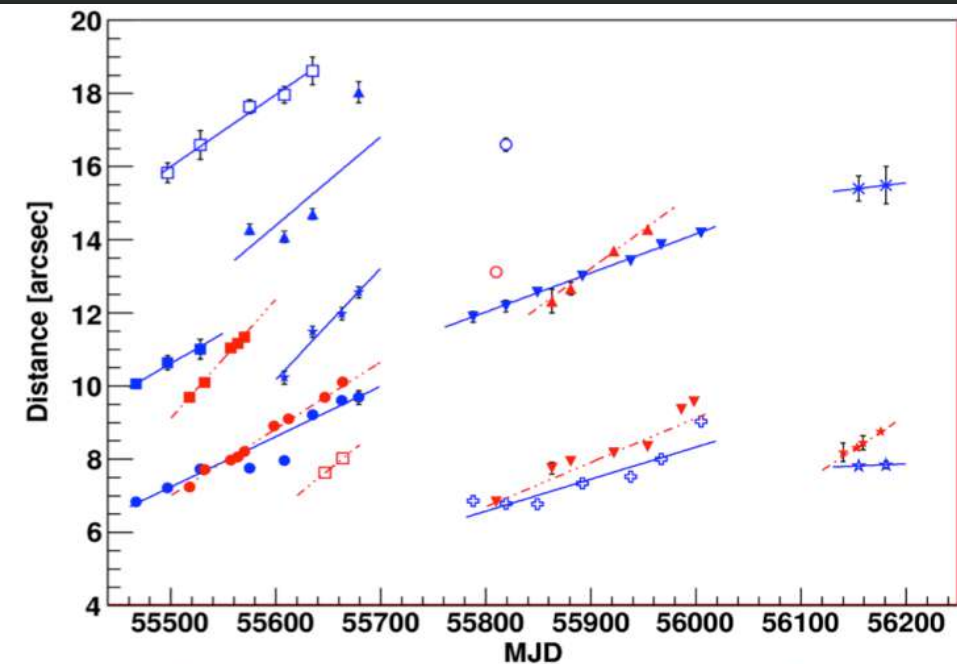
[Bietenholz et al. 04]

# GOALS OF 2D MODELS: MULTI-WAVELENGTHS WISP PROPERTIES



[Bietenholtz et al. 2004]

Radio vs Optical wisps

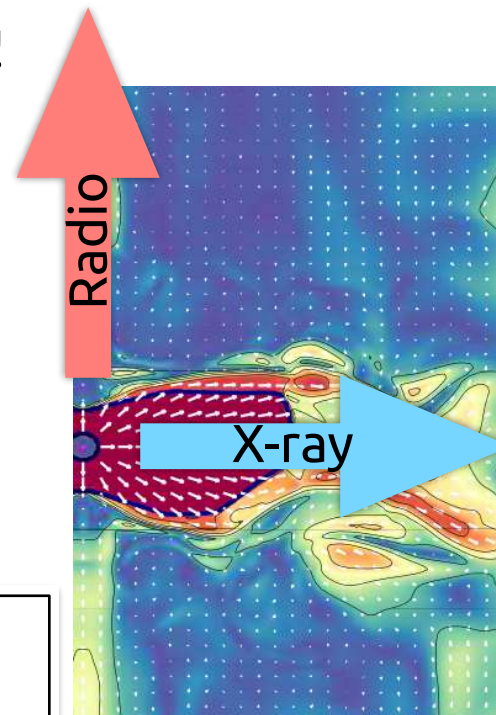
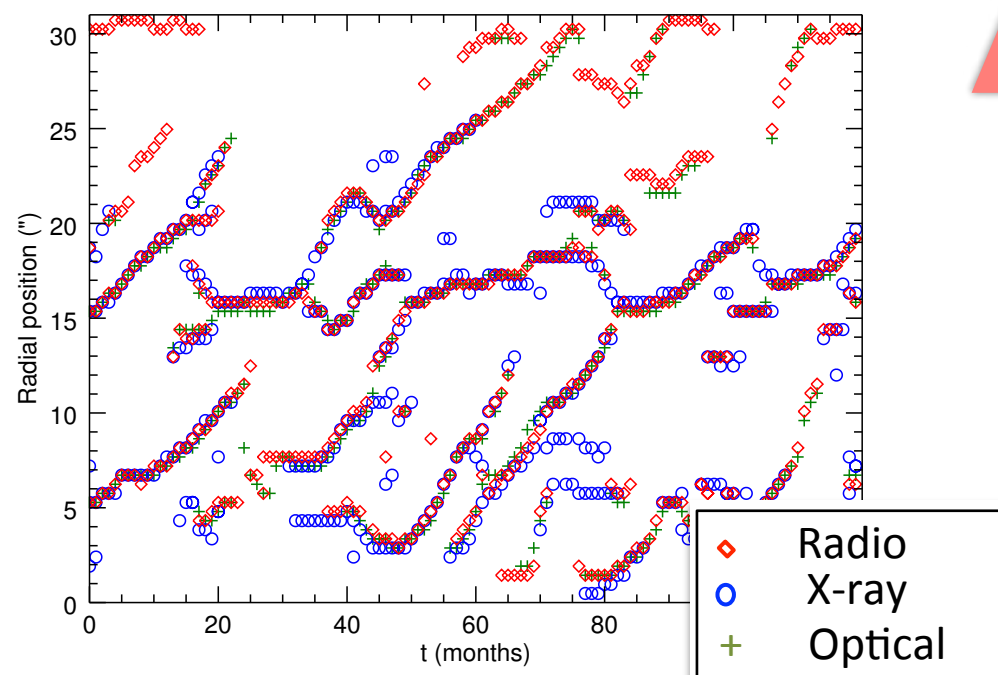


[Schweizer et al. 2013]

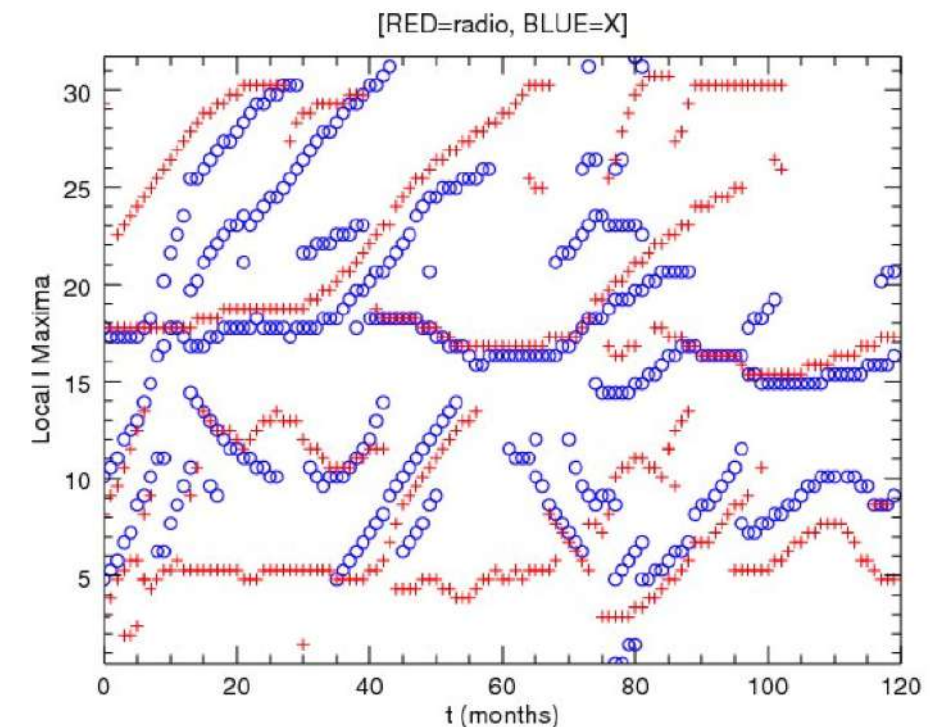
Optical vs X-ray wisps

Non-coincident locations and different outward velocities at different wavelengths explained with non uniform injection of emitting particles:

If injection is uniform wisps are coincident!



[Olmi et al. 2015]

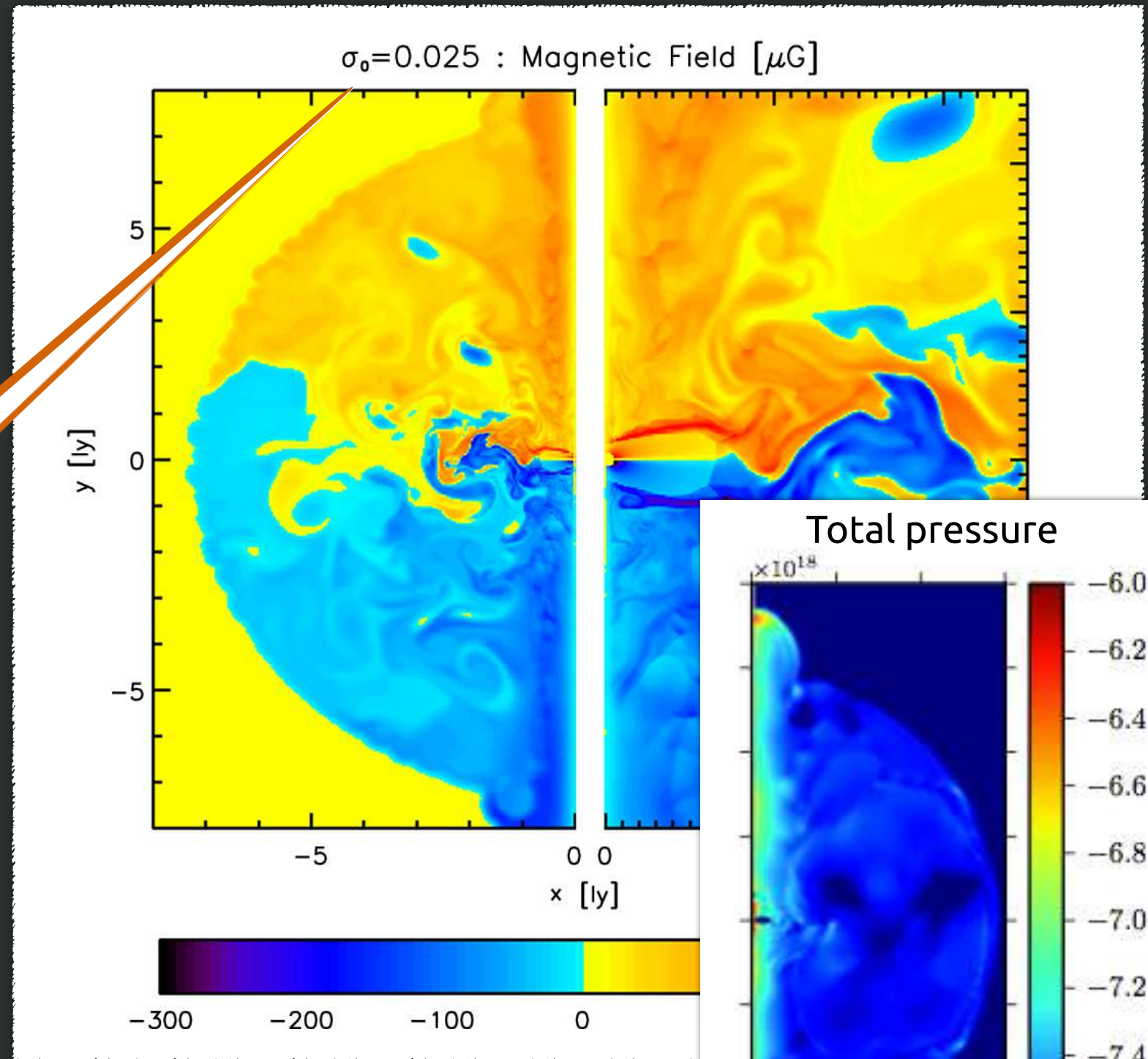


# LIMITS OF 2D MODELS

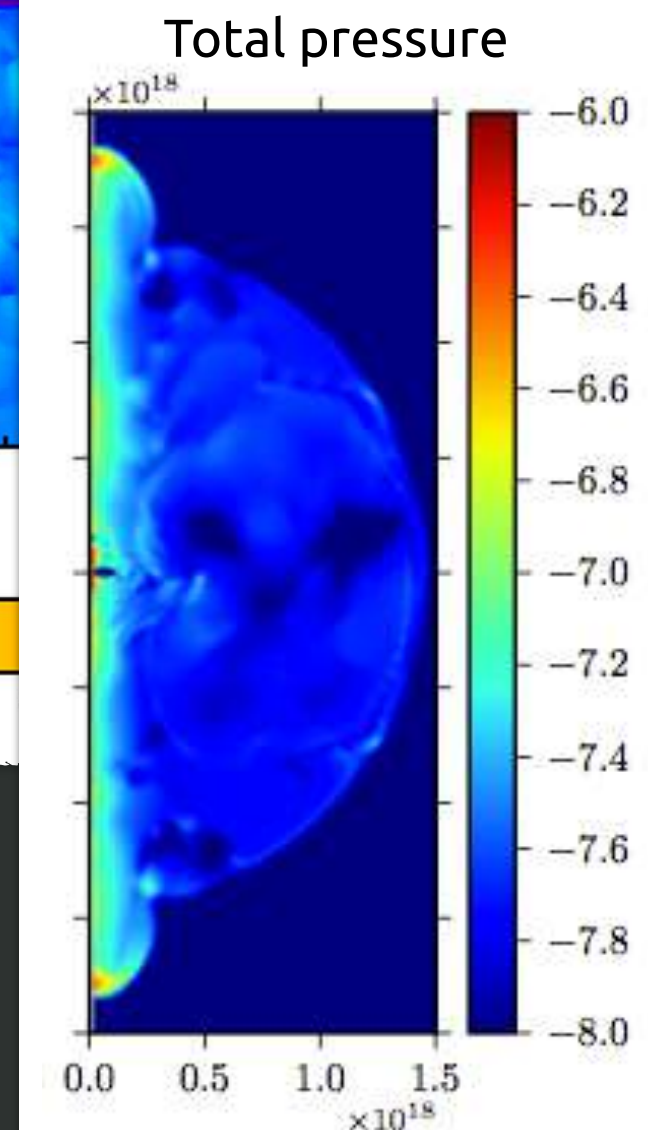
? MAGNETIC FIELD MORPHOLOGY ?  
? LEVEL OF MAGNETIZATION ?

2D simulations can only  
work with  $\sigma < 1$ .

Averaged field  
underestimated:  
 $\langle B \rangle_{\text{SYM}} \approx 10^{-5} \text{ G}$   
 $\langle B \rangle_{\text{OBS}} \approx 10^{-4} \text{ G}$



[Olmi et al. 2015]

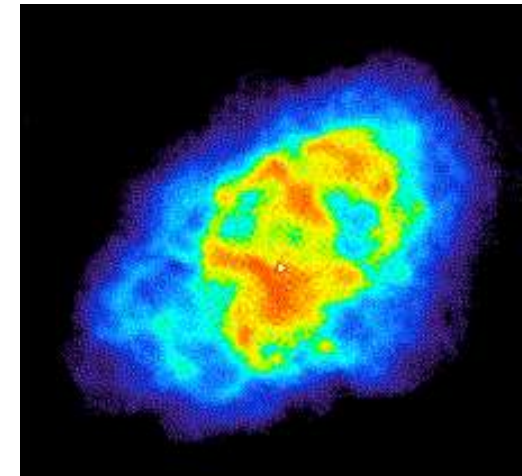
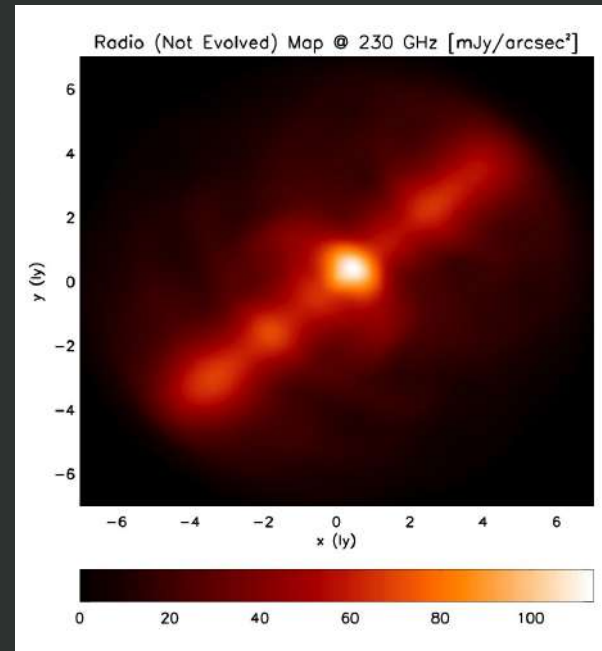
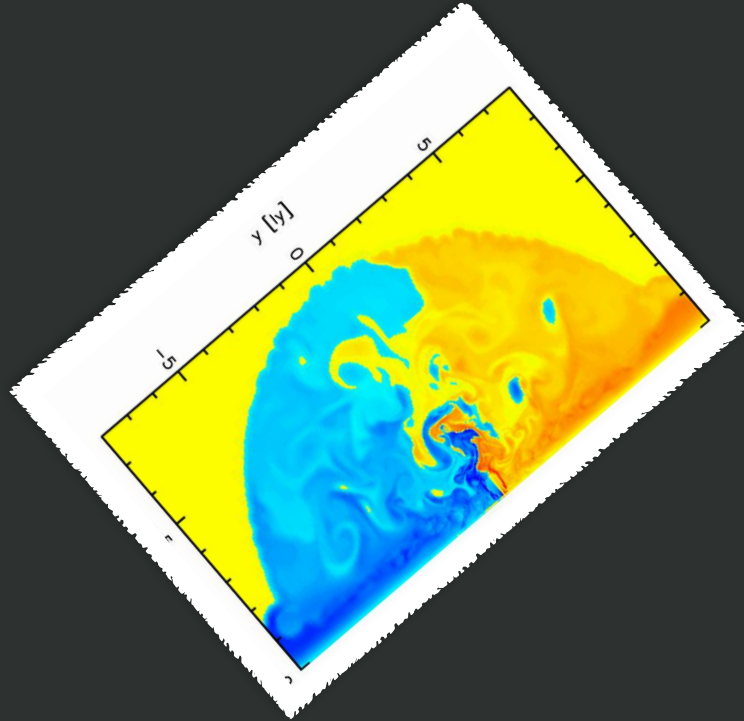


[Porth et al. 2014]

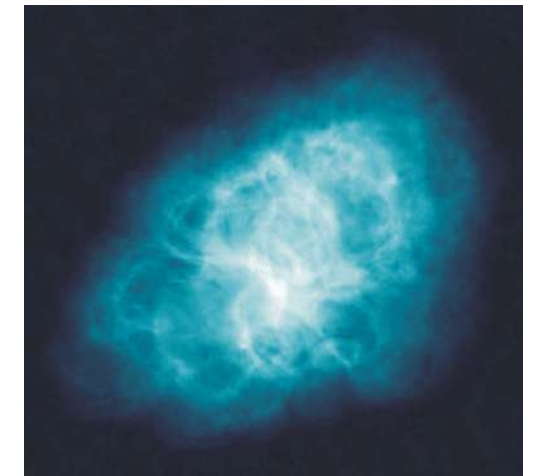
# LIMITS OF 2D MODELS

## THE MAGNETIC FIELD PROBLEMS AFFECT EMISSION

RADIO EMISSION IS NOT UNIFORM: TRACES THE FIELD COMPRESSION

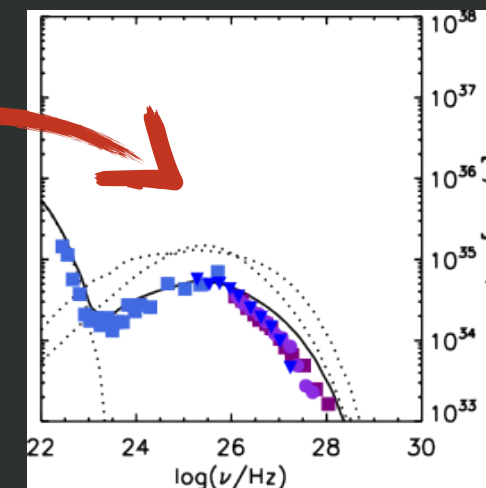
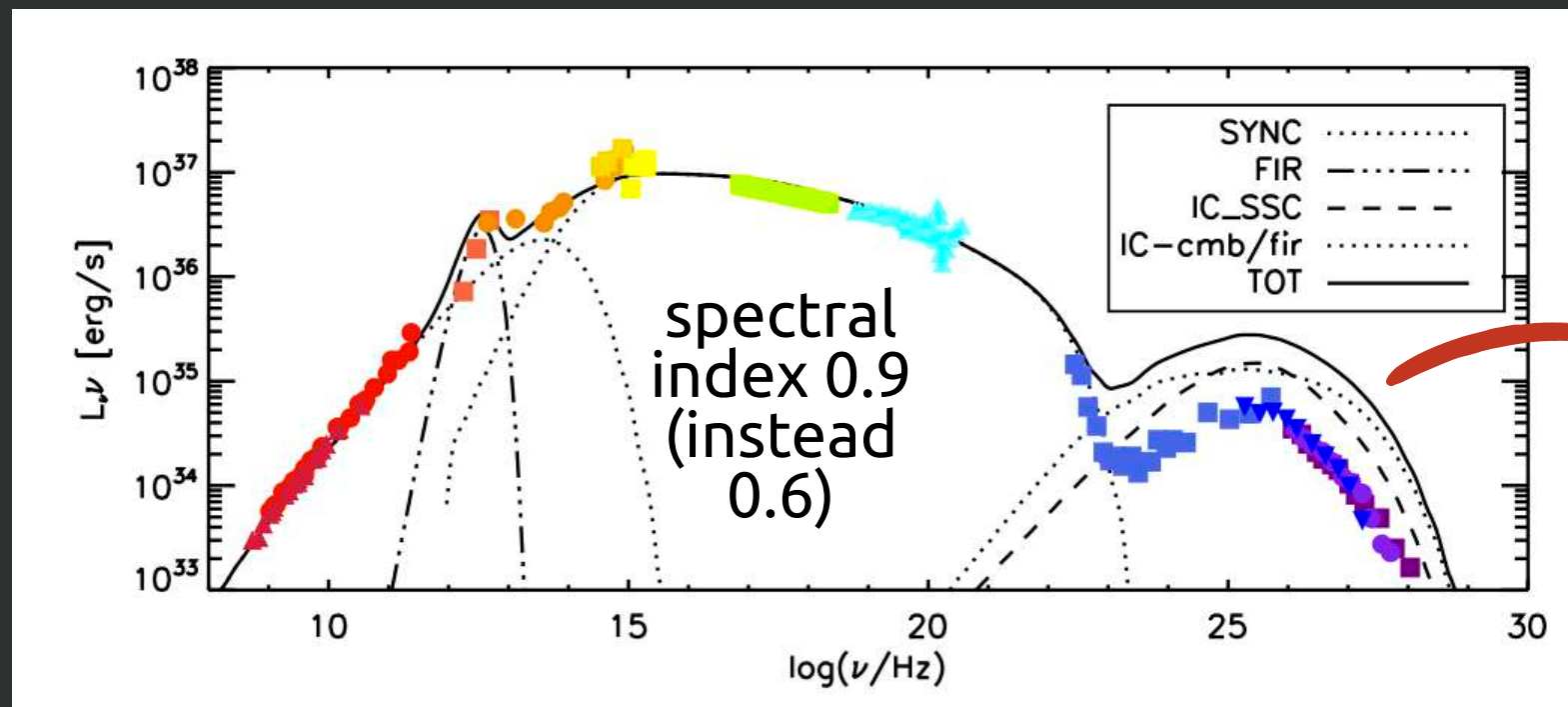


VLA



NRAO

HIGH-ENERGY SPECTRUM NEEDS ARTIFICIAL STEEPENING TO COMPENSATE LOWER ENERGY LOSSES  
IC OVERESTIMATED



IC corrected to  
equipartition  
field

# 3D SIMULATIONS

- ✓ 3D models allow for a more complex structure of the magnetic field
- ✓ In 3D the magnetic dissipation is stronger (Kink instability) and  $\sigma \geq 1$  can be reached!

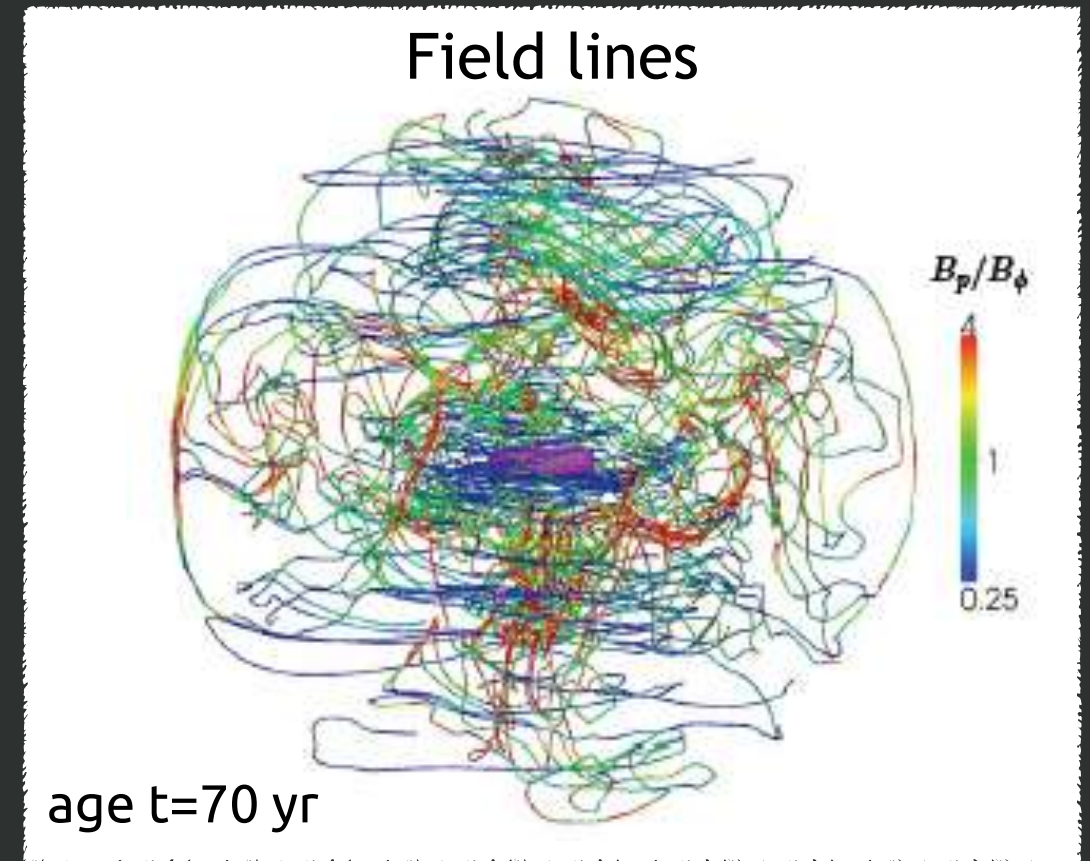
Possible solution to  $\sigma$ -paradox?



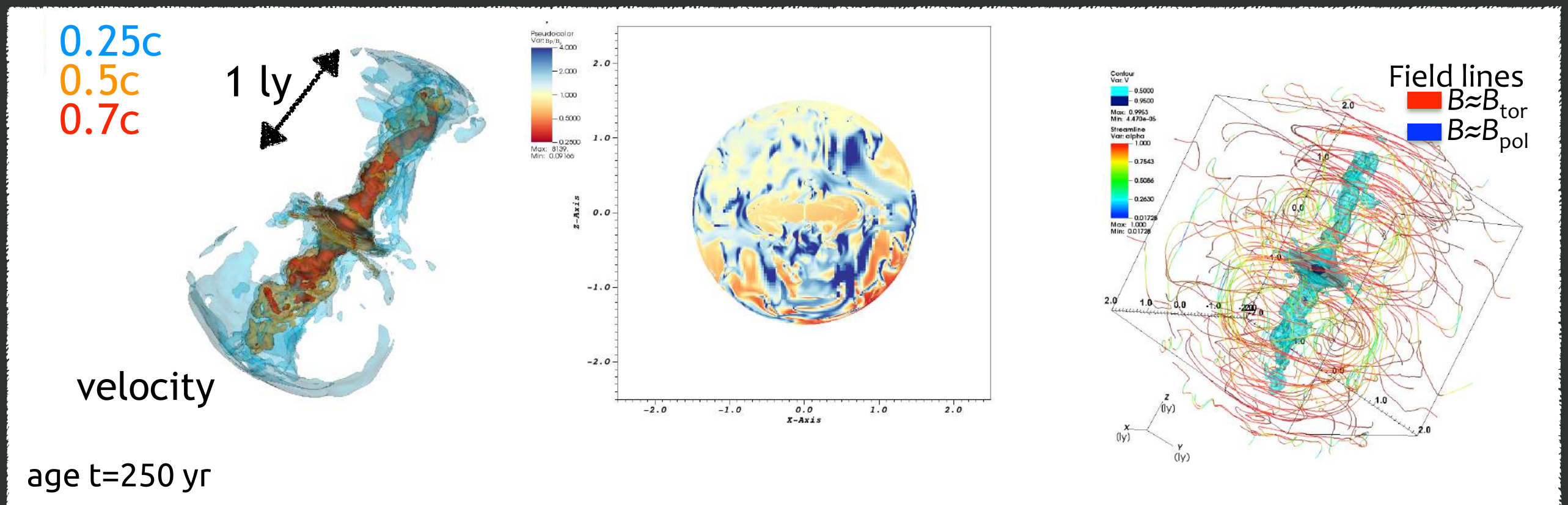
BUT 3D simulations are demanding in terms of resources and time, data are huge



> 1 Million CPU hours (ran @ CINECA with >2000 CPUs)



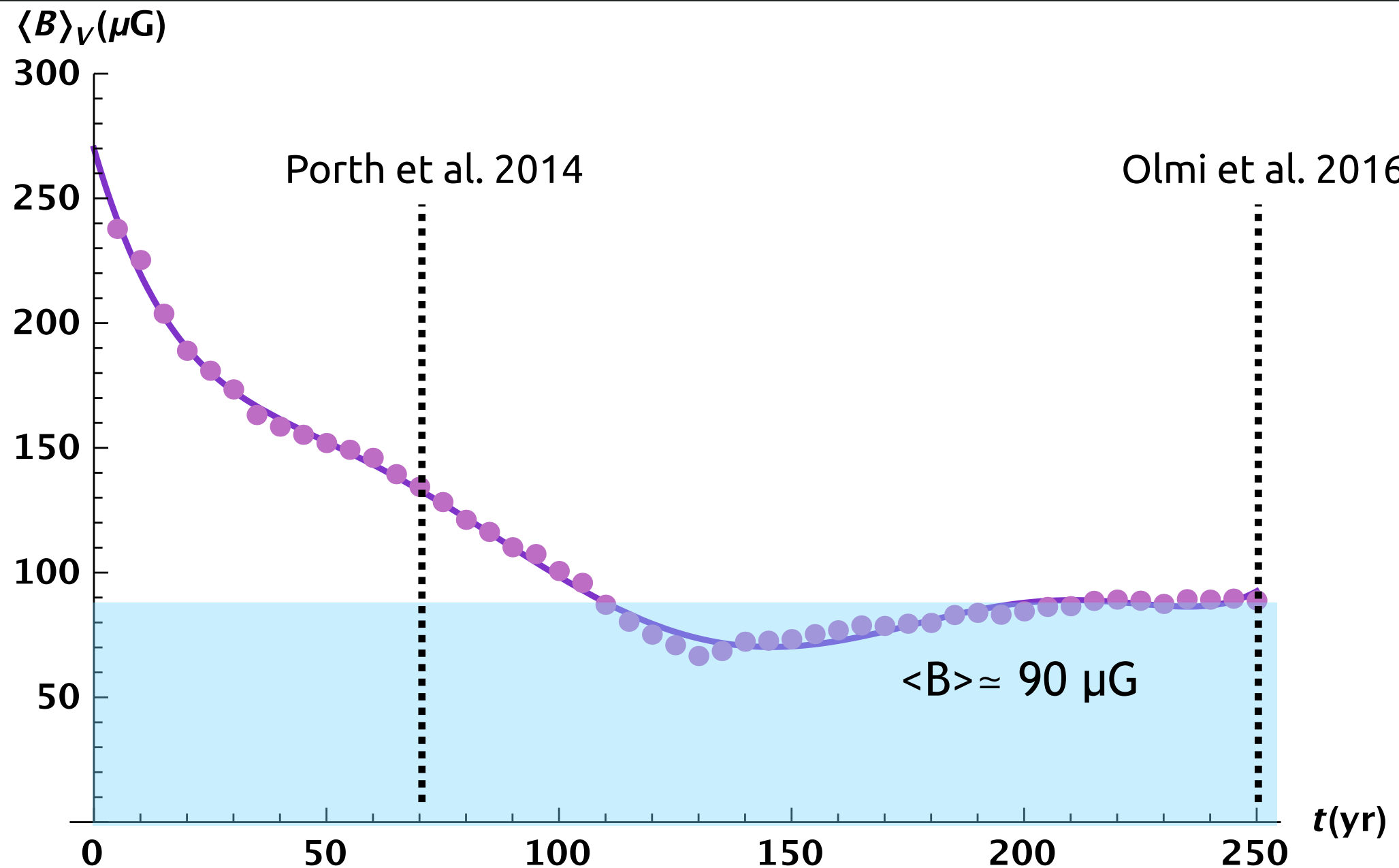
[Porth et al. 2013, 2014]



[Olmi et al. 2016]

# AND NOT ALL IS SOLVED...

The average field is again too low:  $\sigma=1$  not sufficient?

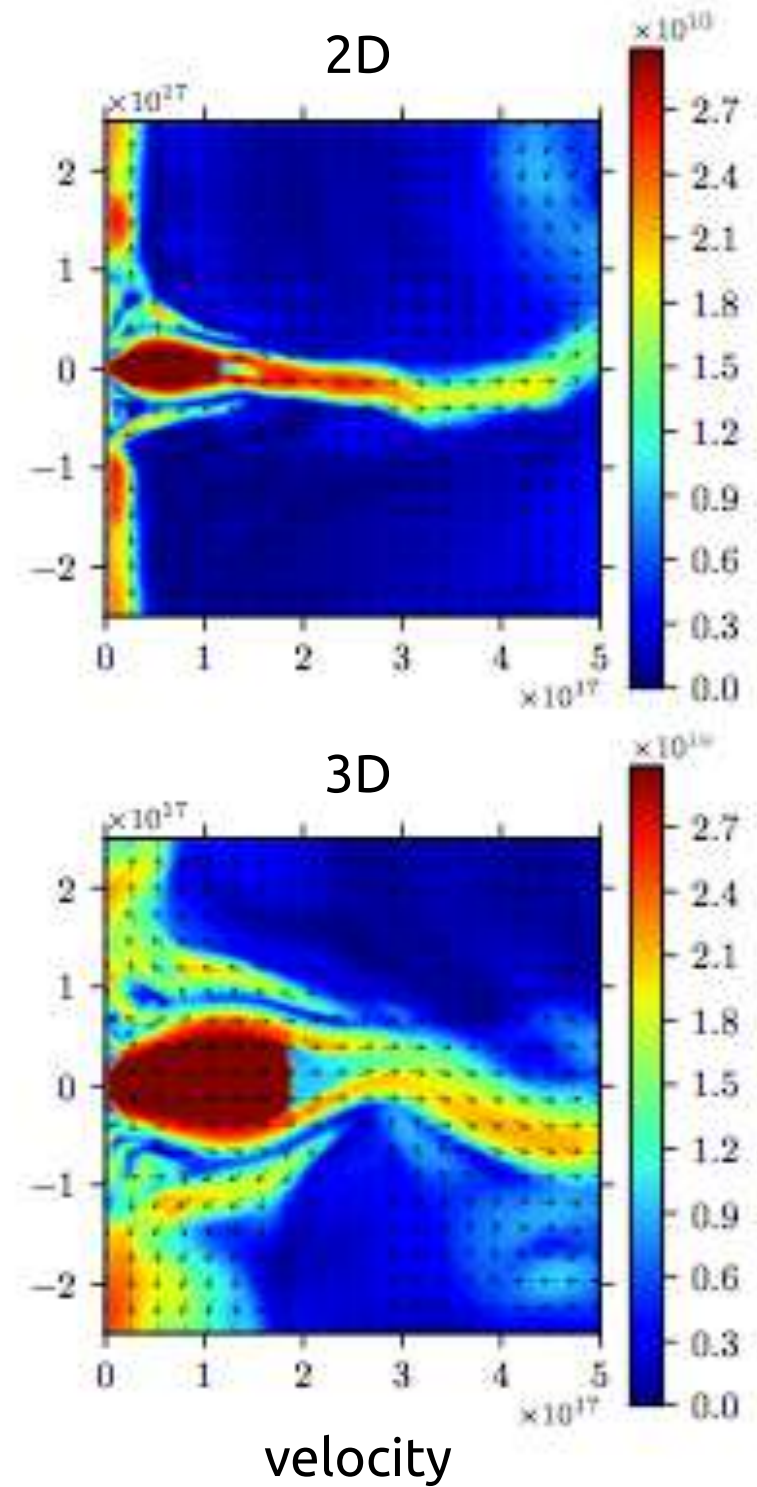
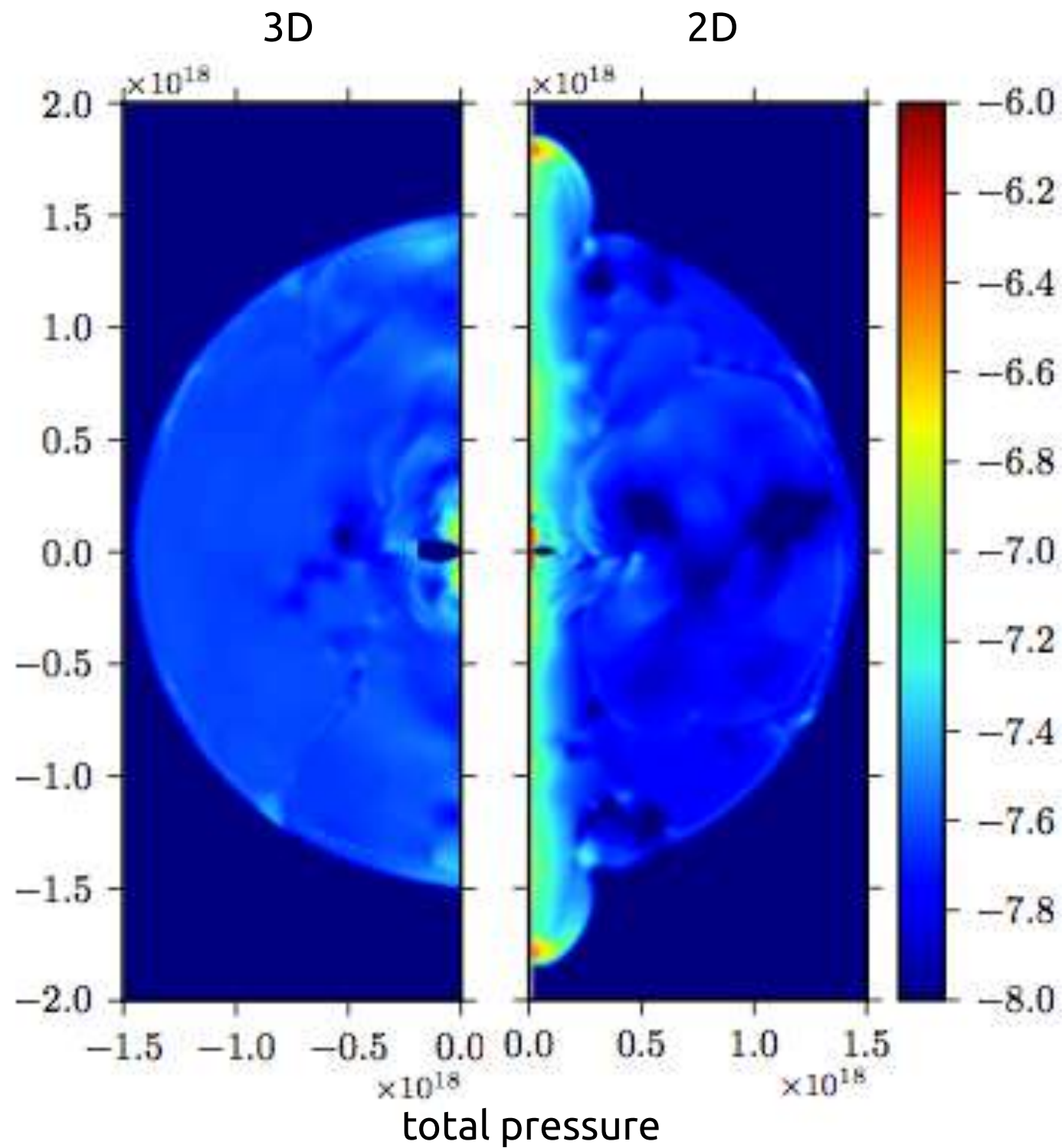


Same problems with the spectrum!

# 3D VS 2D

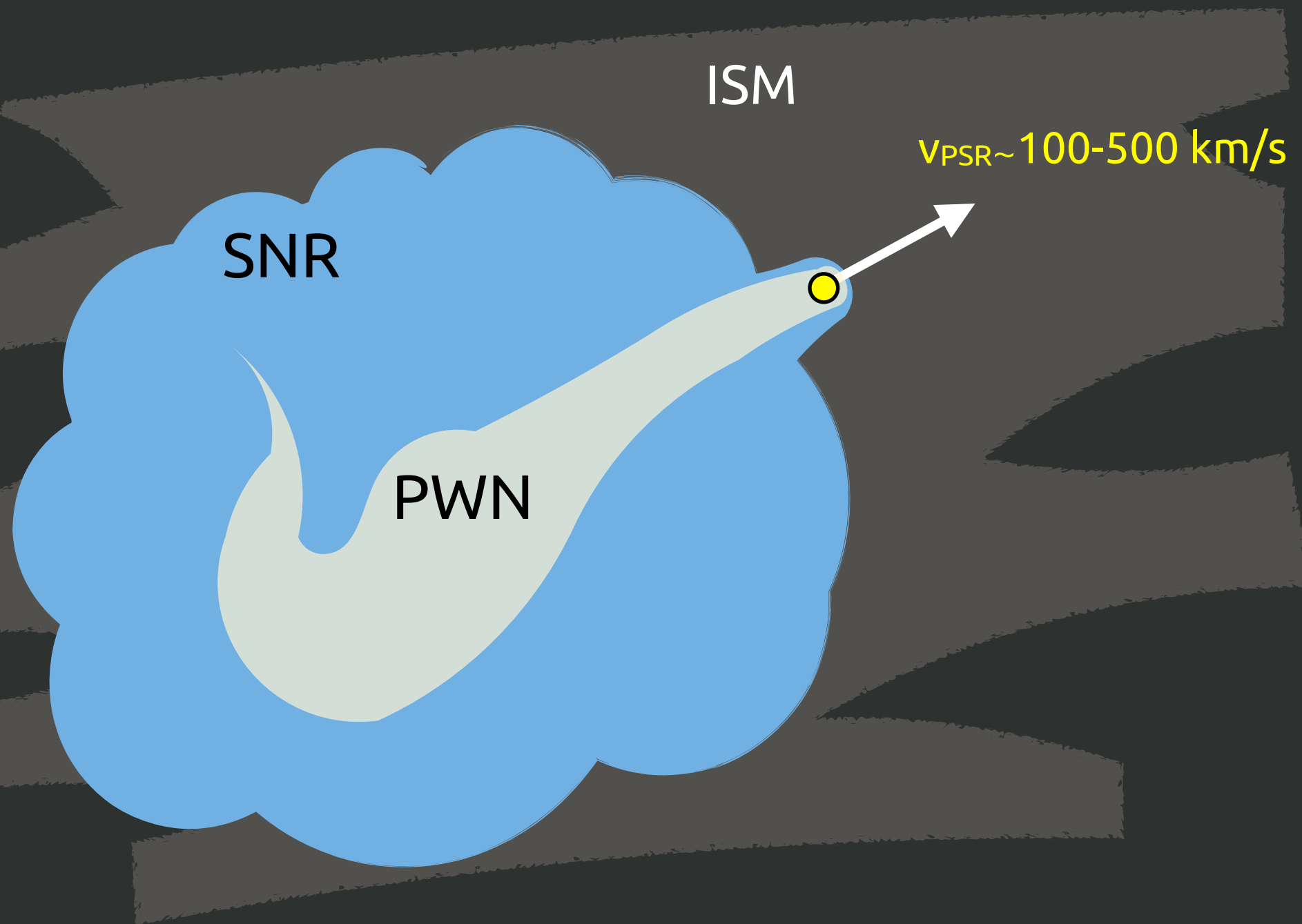
global dynamics completely different

inner dynamics comparable



[Porth et al. 2013, 2014]

# A DIFFERENT PROBLEM: EVOLVED PWNE

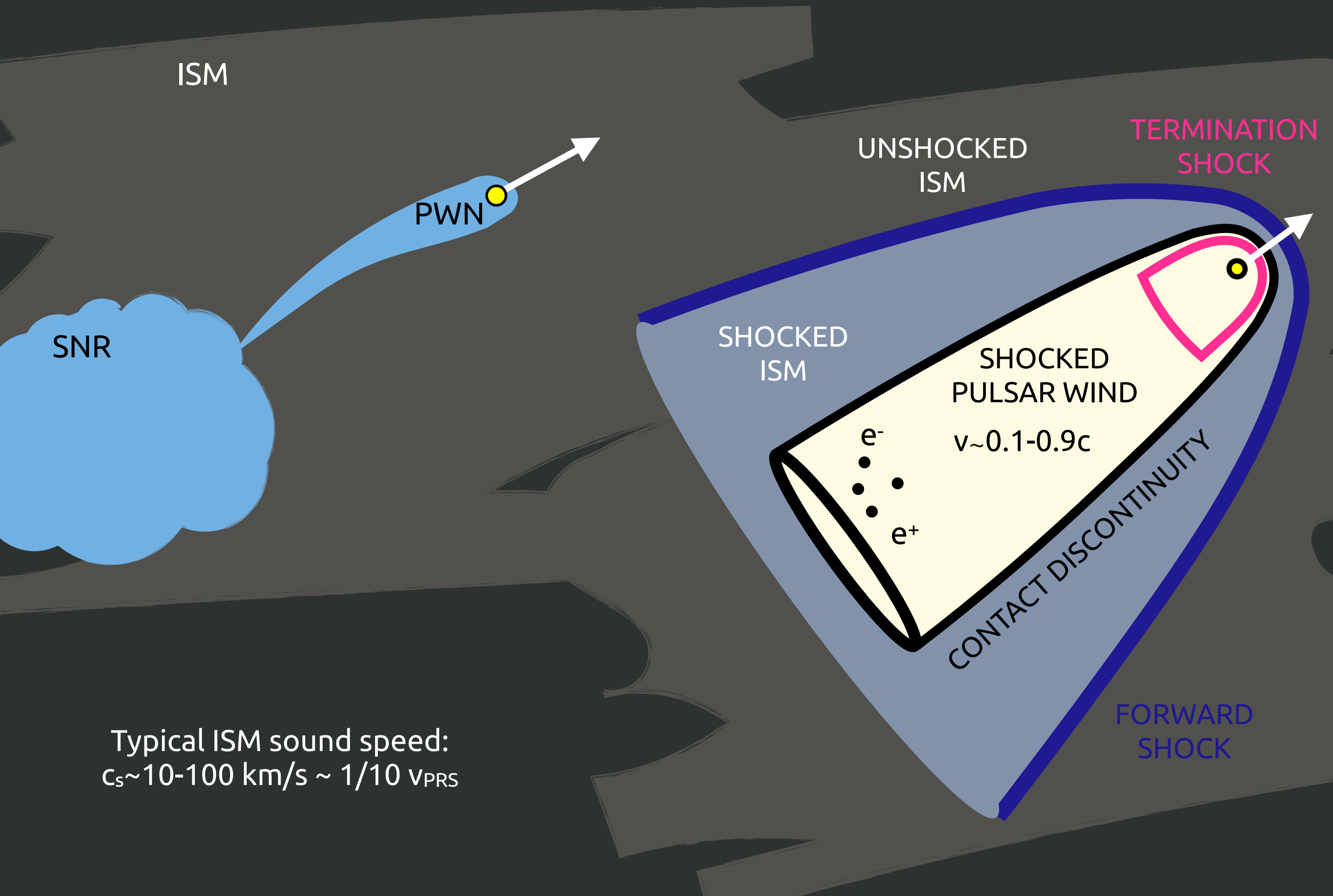


Large fraction of all  
the pulsars born  
with **high kick**  
velocity (**10%-50%**)

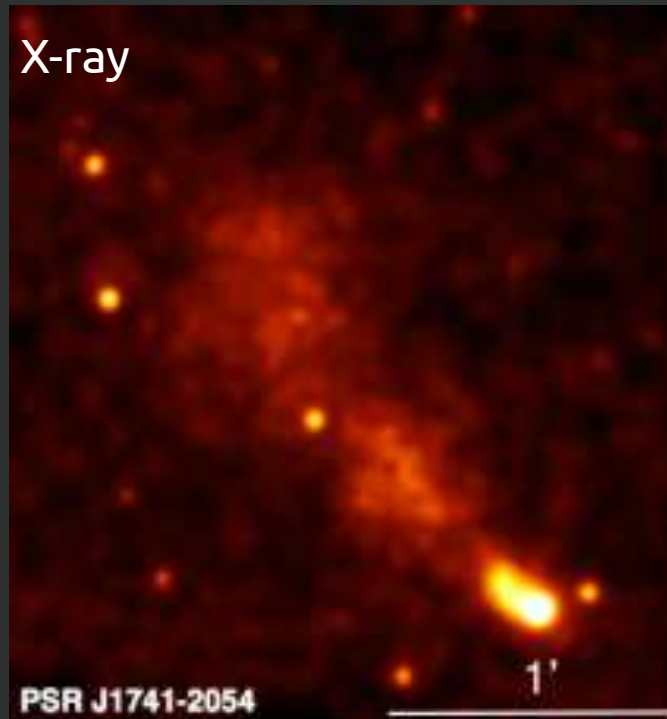


**fated to escape the**  
**SNR** on timescales  
<< than typical  
pulsar ages ( $\sim 10^6$   
yr)

# BOW SHOCK PWNe



# THE COMETARY SHAPE of BSPWNe



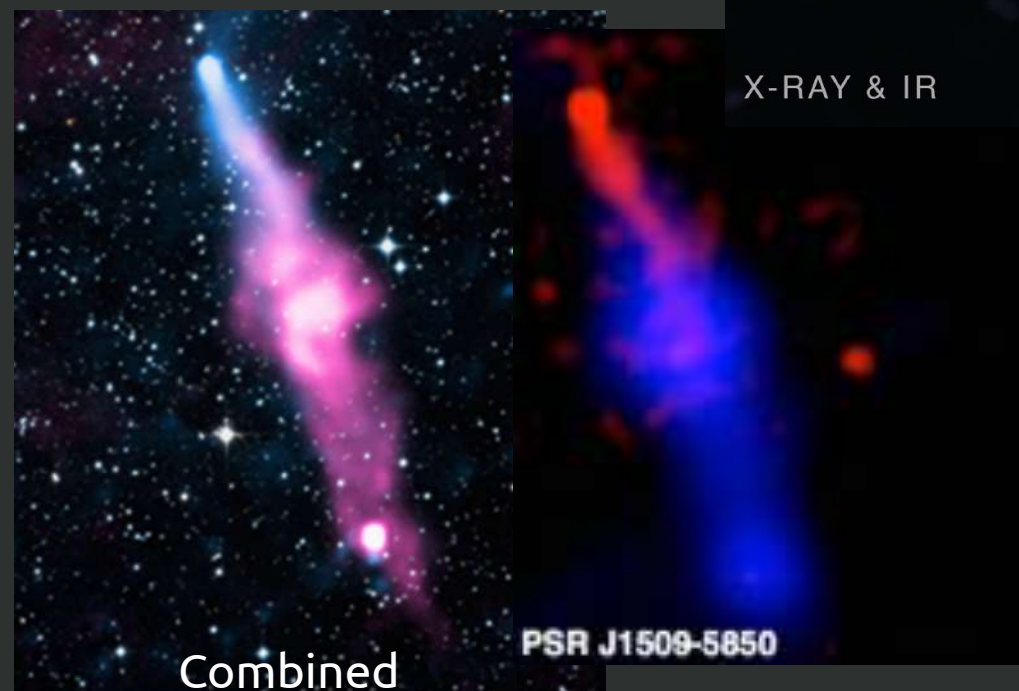
**PSR J1741-2054**

[Kargaltsev et al. 2016]



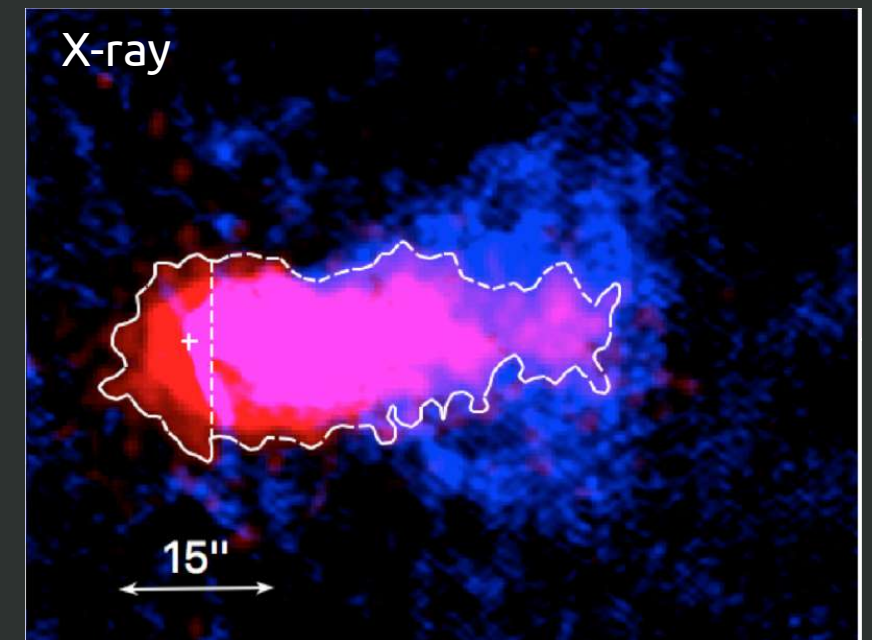
**B0355+54**

[Emre et al. 2005]



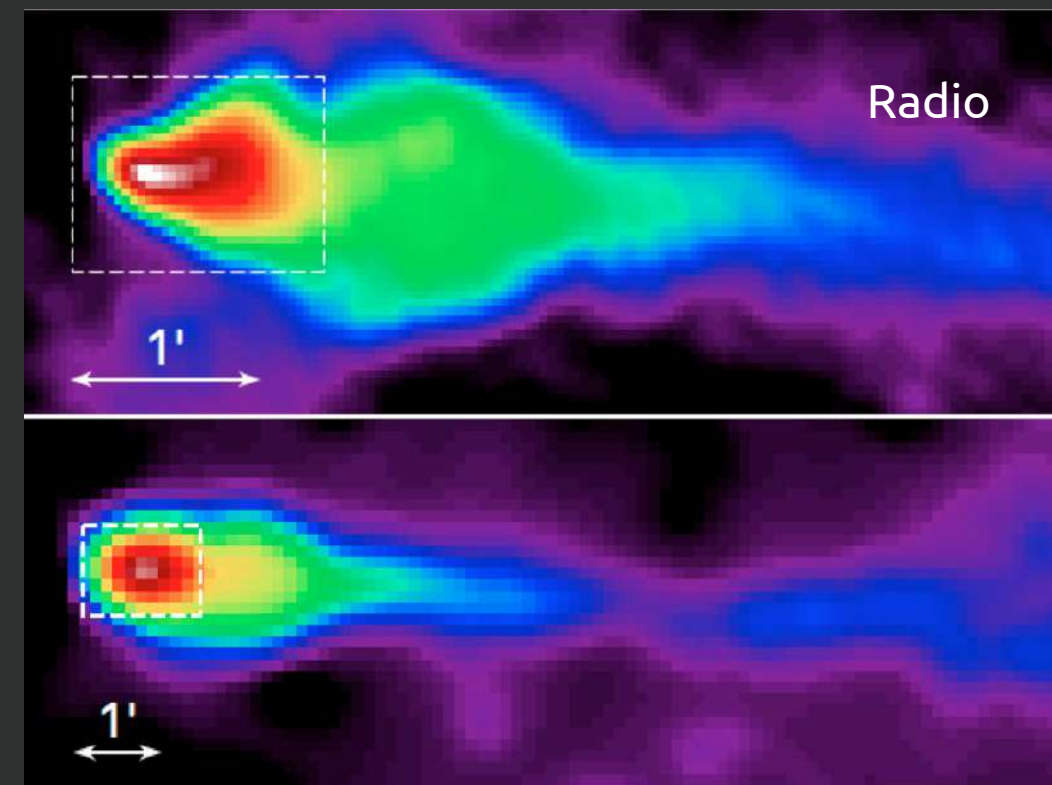
**PSR J1509-5850**

[Hui & Becker 2007, Klinger et al. 2016]



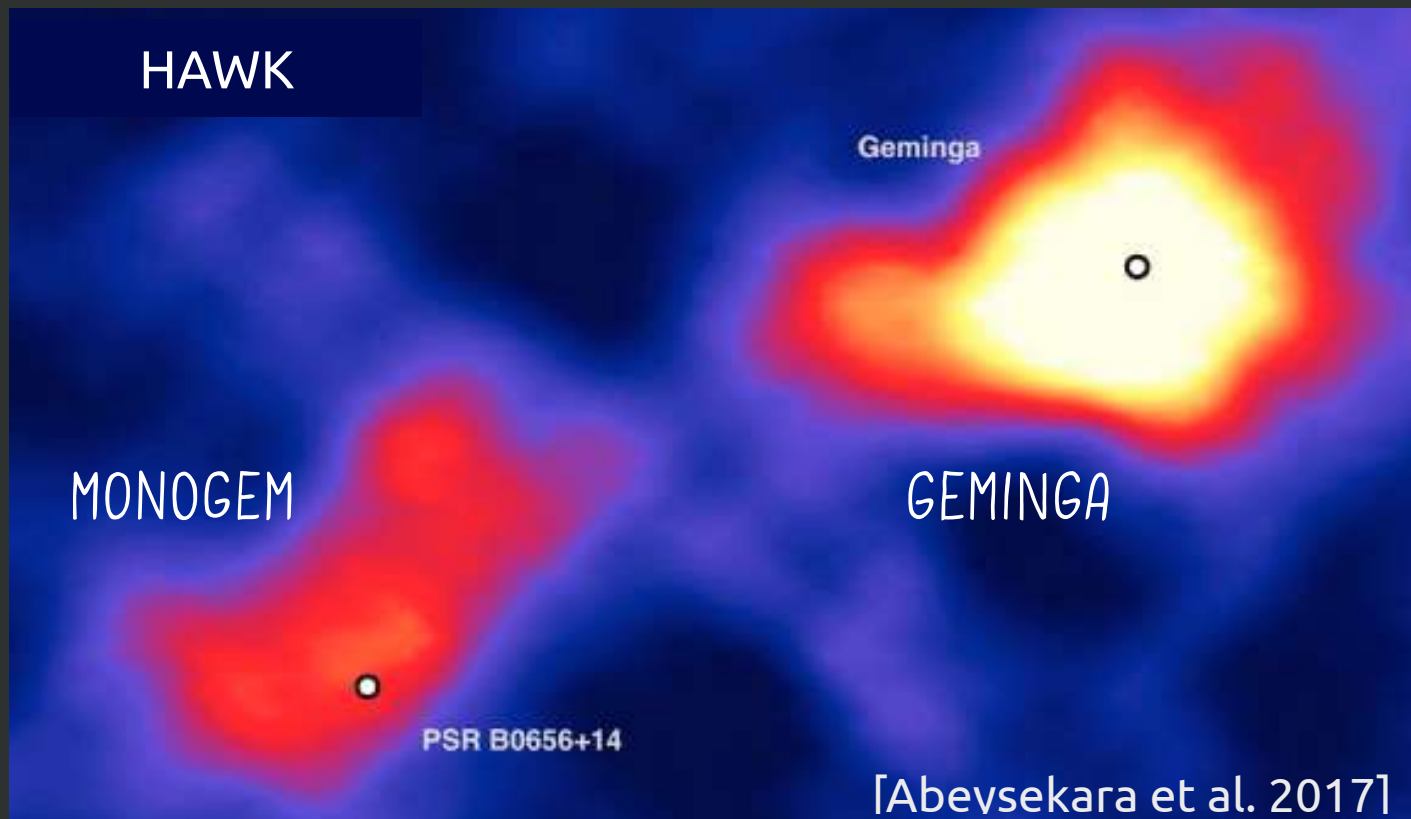
**Mouse PWN**

[Yusef-Zadeh & Bally 1987,  
Yusef-Zadeh & Gaensler 2005,  
Klinger et al. 2018]

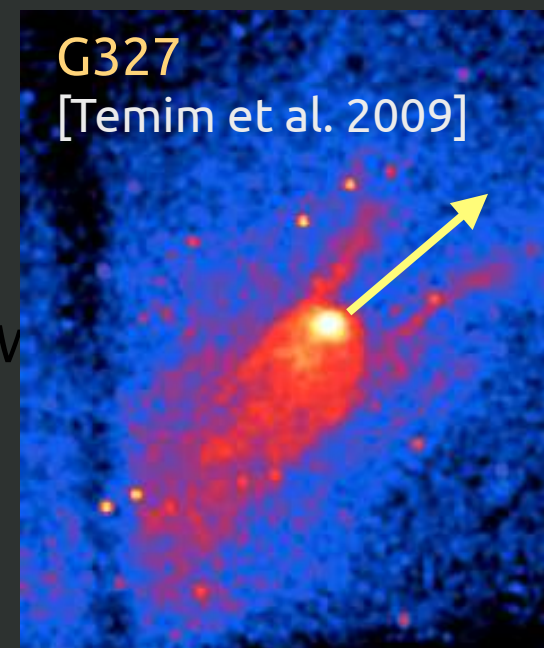


# BSPWNe as SOURCES of ENERGETIC PARTICLES?

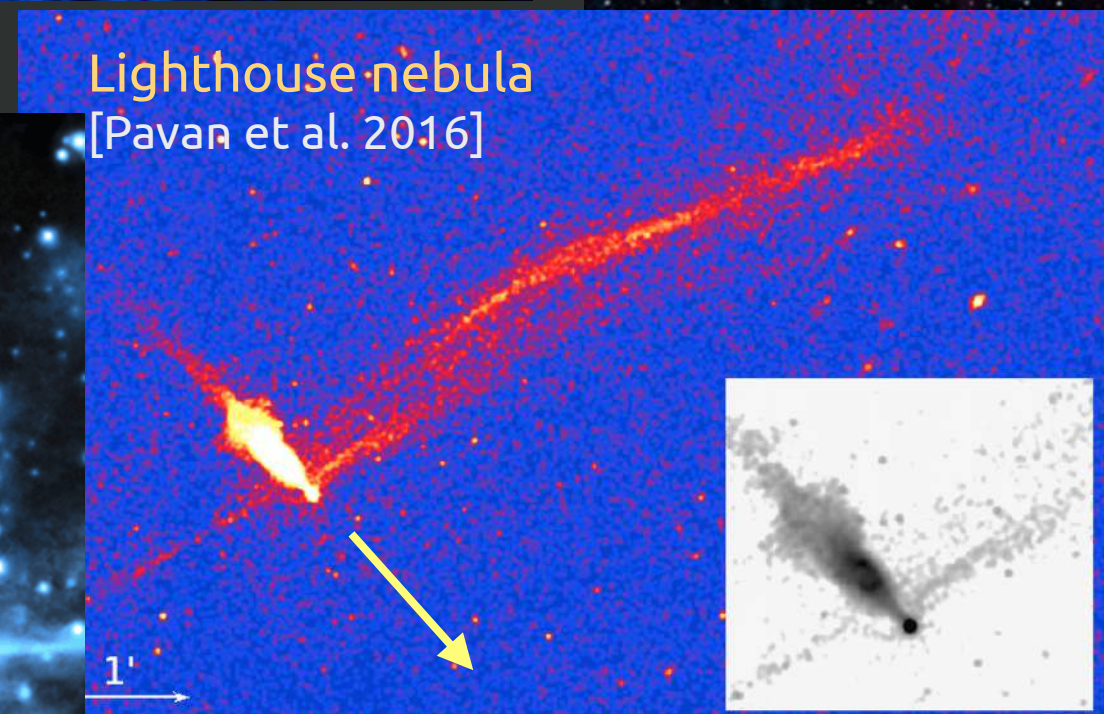
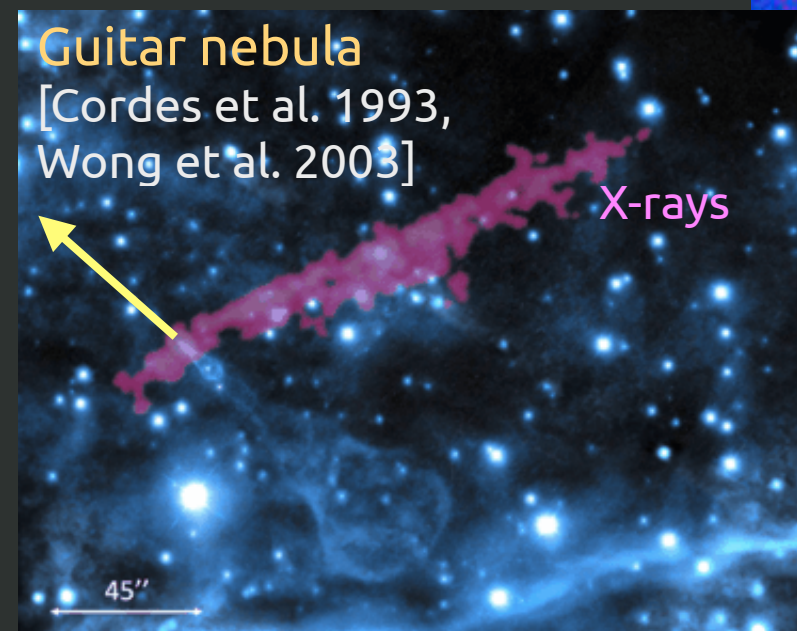
Extended TeV halos surrounding evolved pulsars



Asymmetric X-ray jets



Other recent observations in:  
J1809-1917 [Klinger et al. 2020]  
J2030+4415 [de Vries & Romani 2020]  
B1929+10 [Kim et al. 2020]

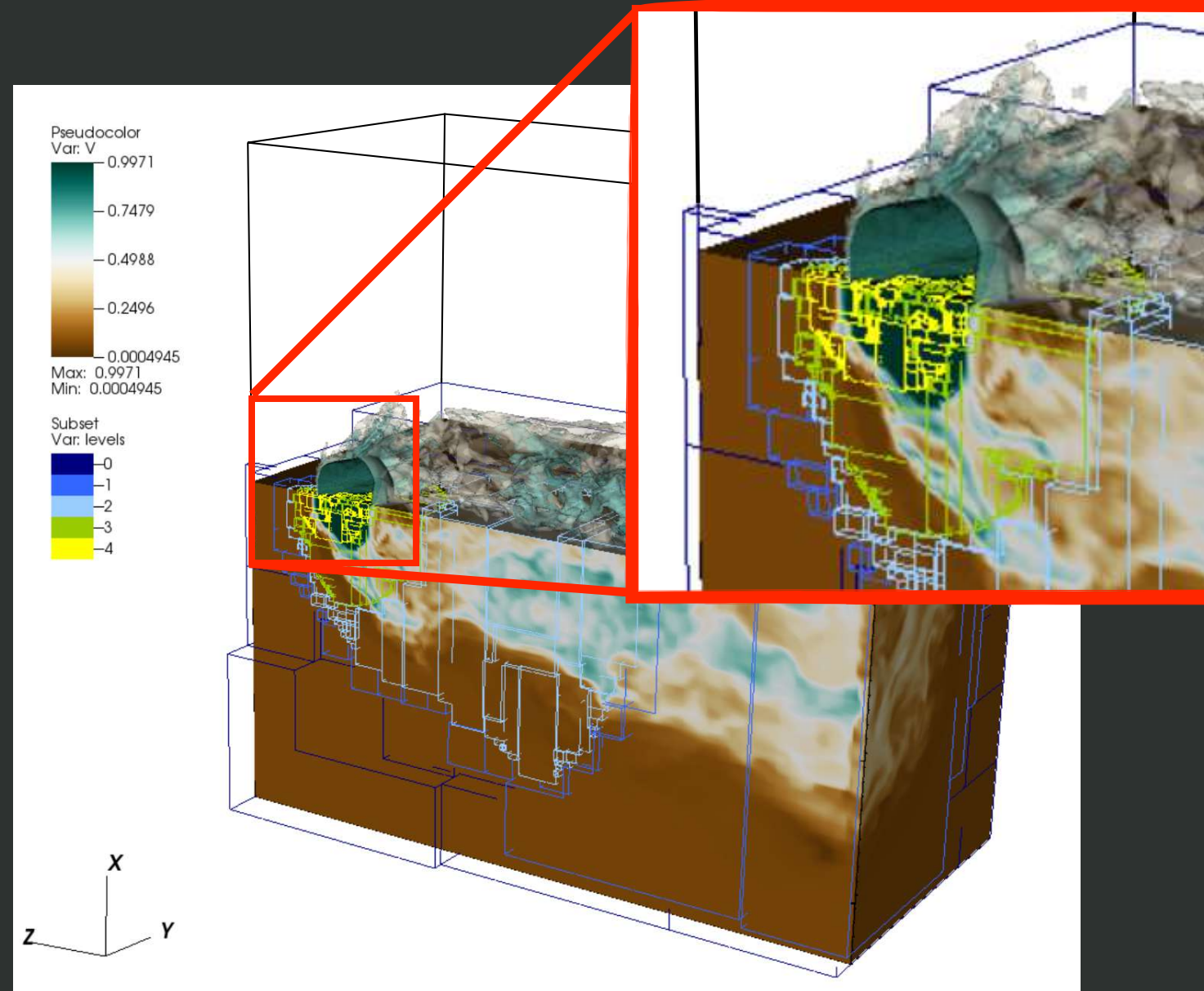
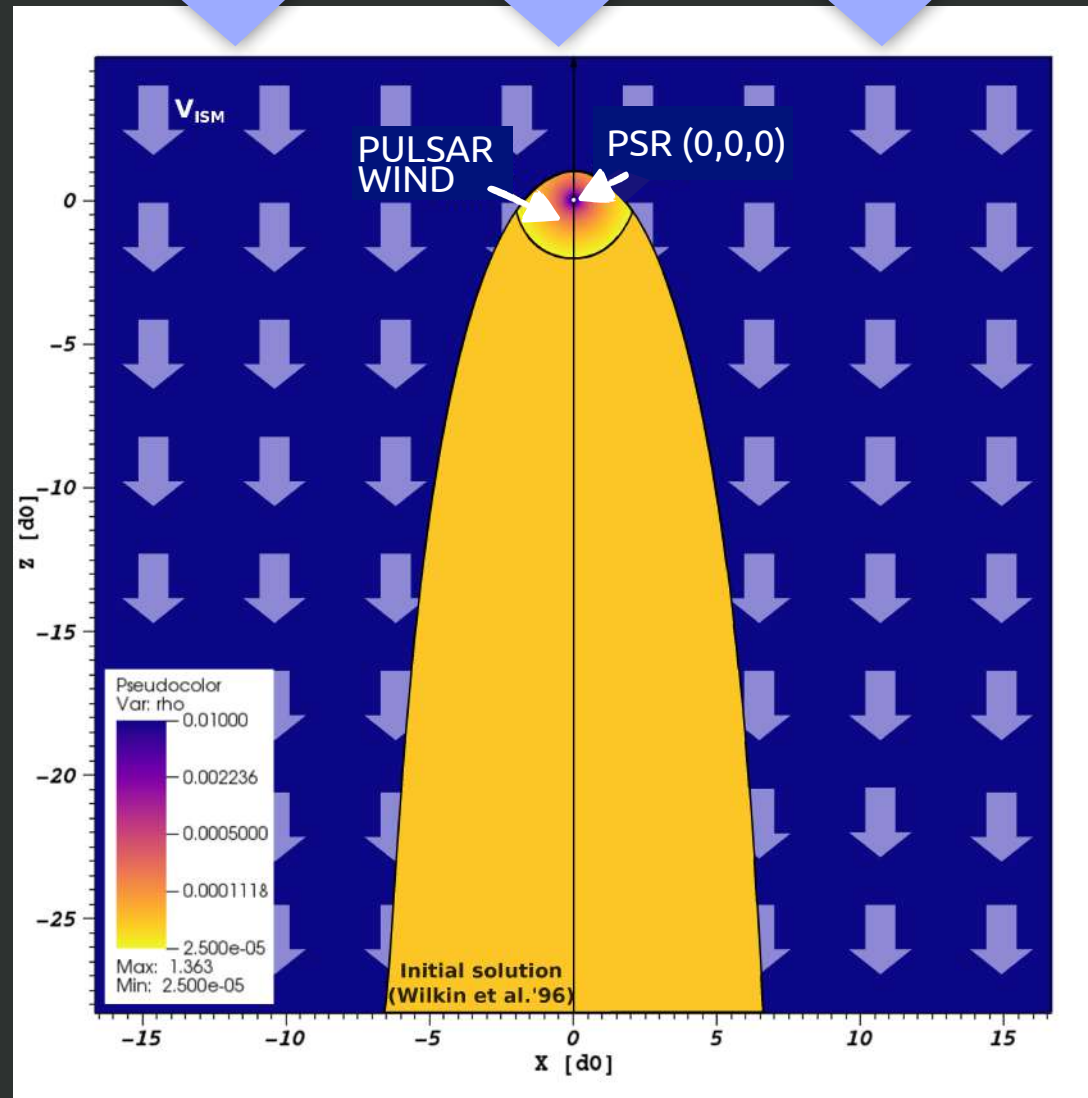


# 3D MHD SIMULATIONS of BSPWNe

Uniform unmagnetized

ISM  $V = -V_{\text{PSR}}$

High resolution required to resolve the PW injection region and allow the TS to correctly detach from the inner boundary (use of Adaptive Mesh Refinement - AMR)



The numerical tool is the **PLUTO** code [Mignone et al. 2007]

Simulations supported by  
MoU INAF-CINECA  
class A projects



# MODELING THE PULSAR WIND AND GEOMETRY

DISTRIBUTION  
OF ENERGY

Energy flux as function of the colatitude from the spin axis:

$$F(\psi) \propto 1 + \alpha \sin^2 \psi$$

$\alpha = 0 \implies$  ISOTROPIC

$\alpha \neq 0 \implies$  ANISOTROPIC

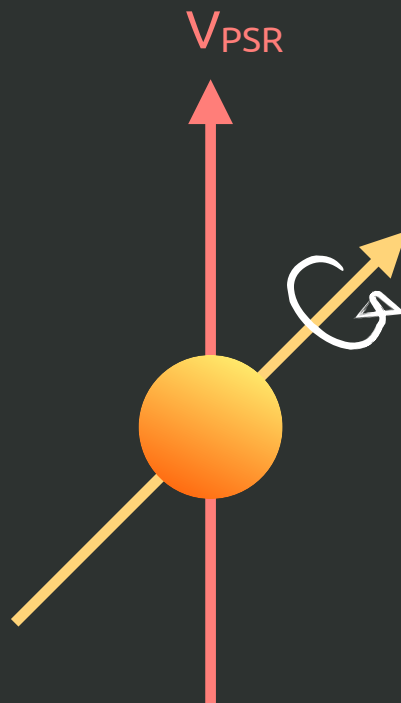
WIND  
MAGNETIZATION

$\sigma = \text{magnetic flux/kinetic flux} = 0.0, 0.01, 0.1, 1$

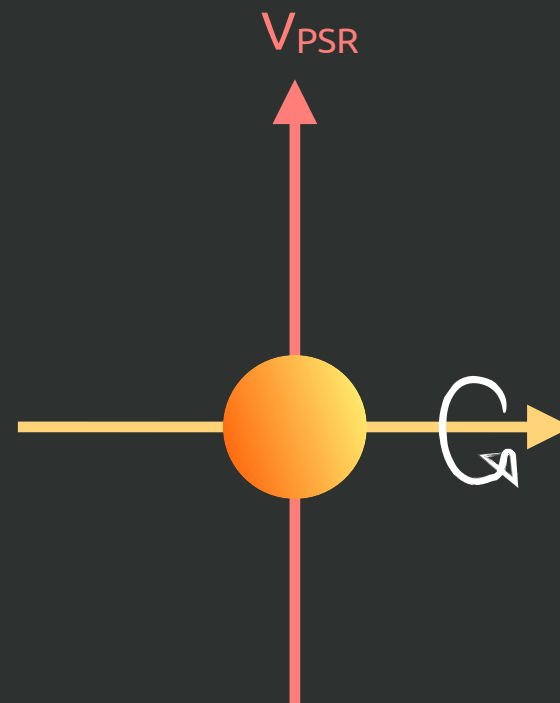
GEOMETRY



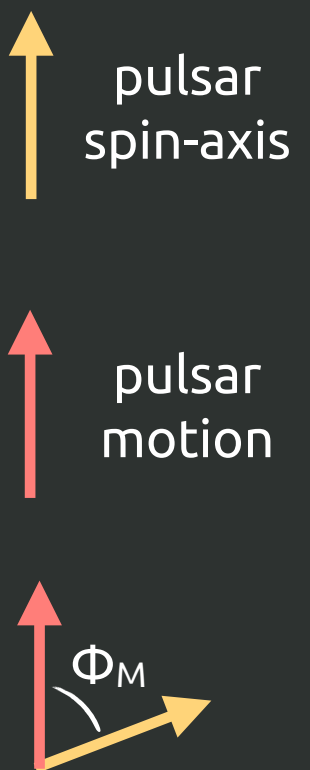
$\Phi_M = 0^\circ$



$\Phi_M = 45^\circ$

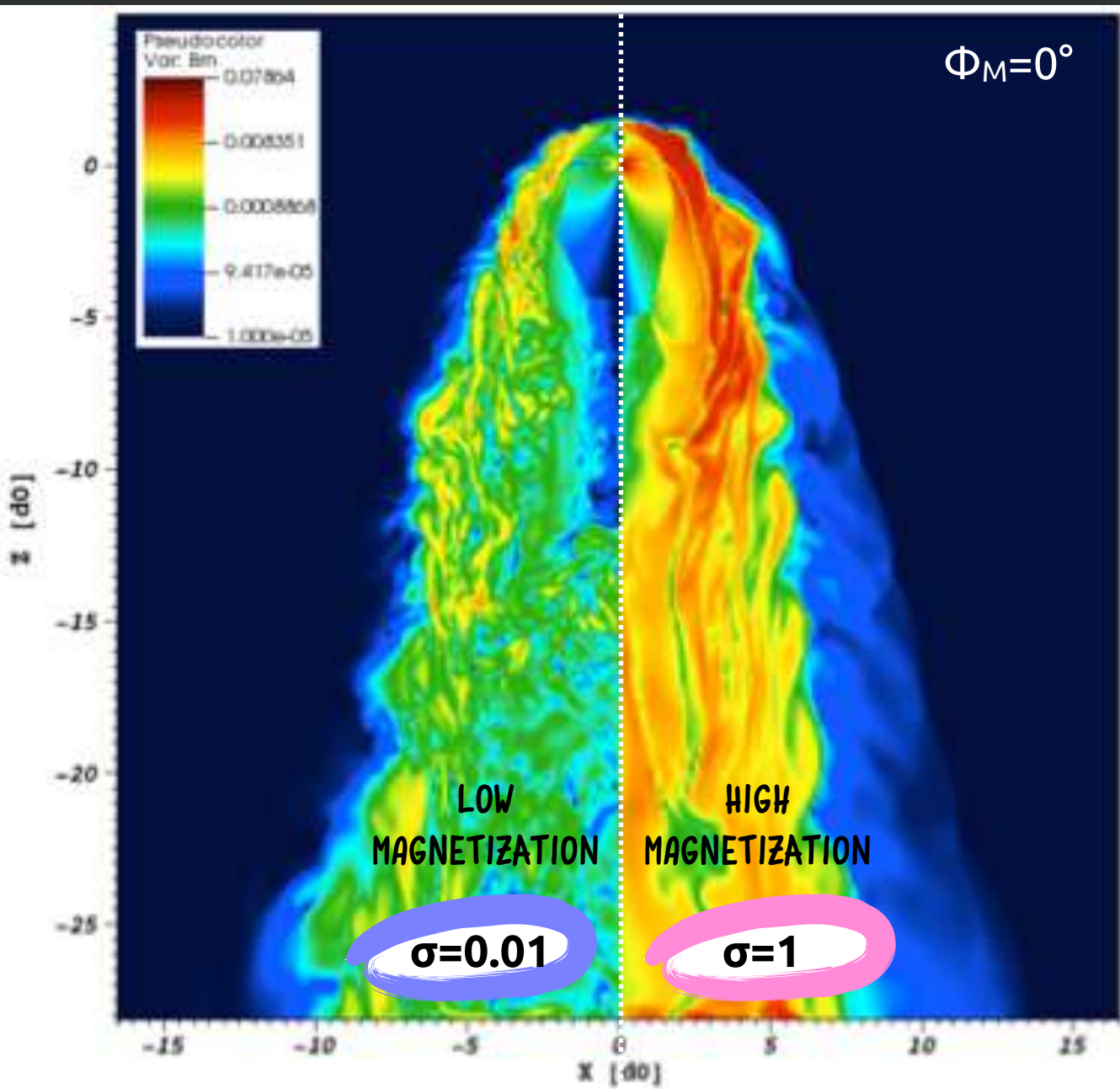


$\Phi_M = 90^\circ$



# DEVELOPMENT OF TURBULENCE IN TAILS

ISOTROPIC WIND

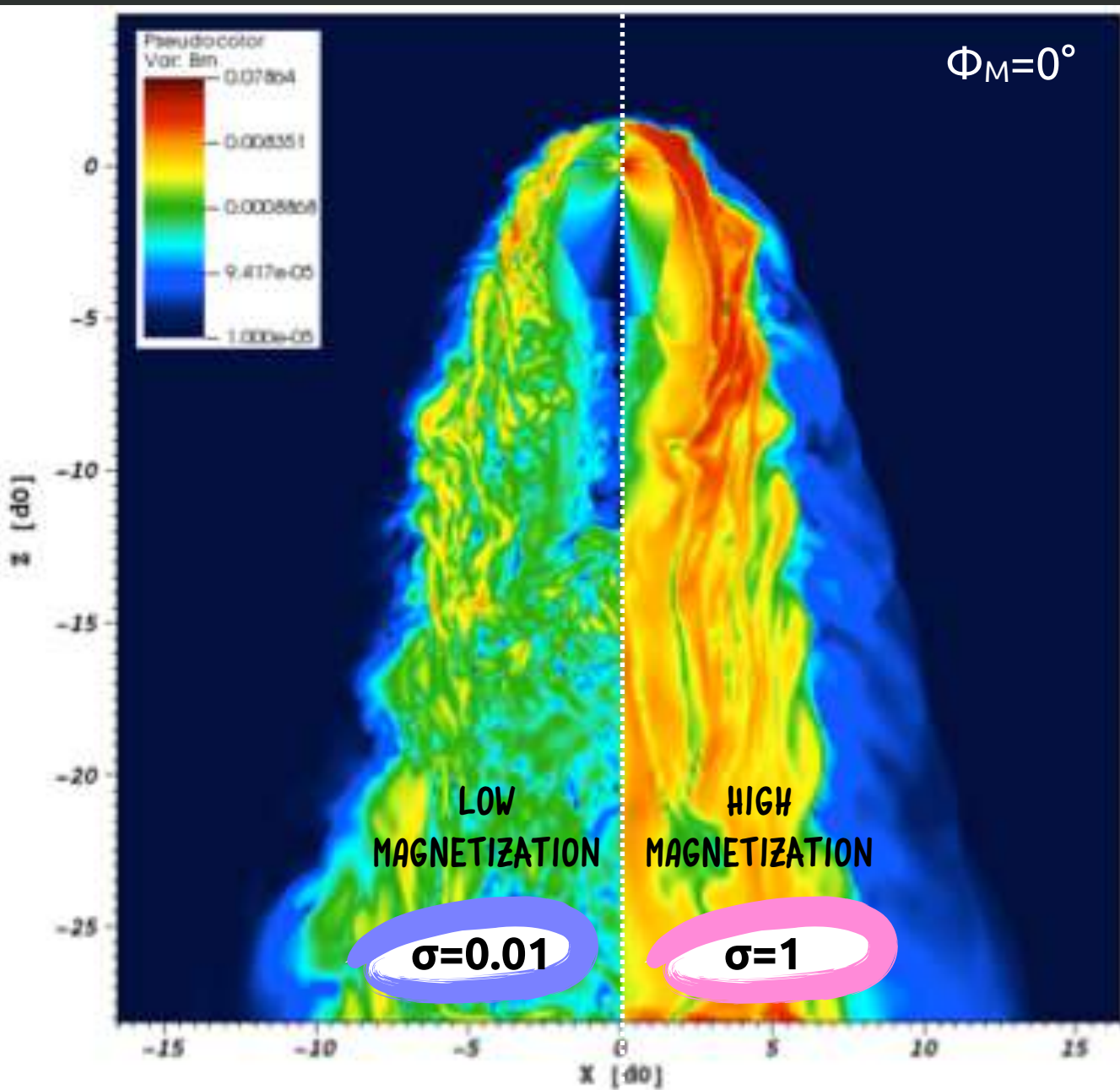


HIGH LEVEL OF TURBULENCE  
CHAOTIC FLOW

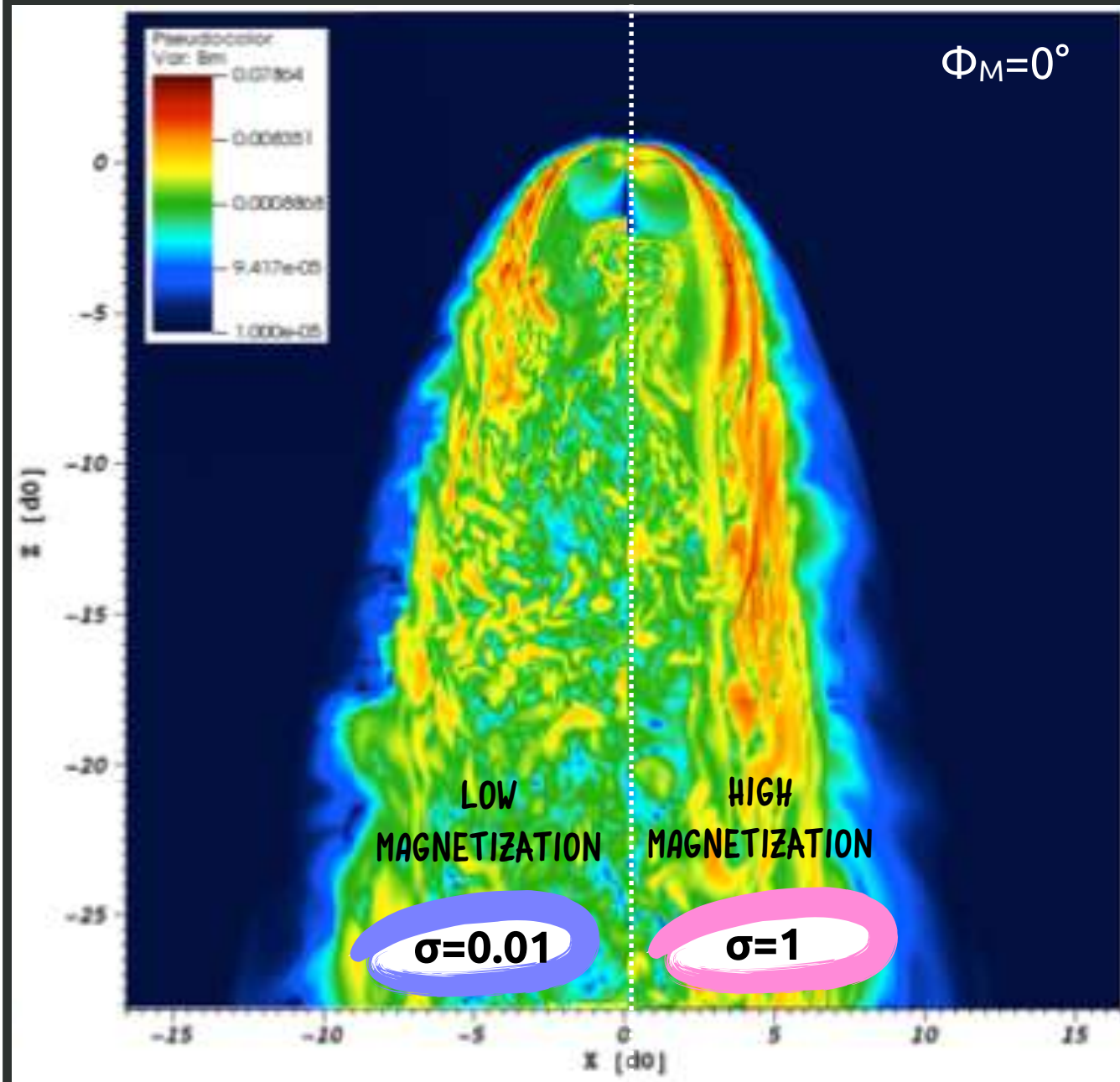
LOW LEVEL OF TURBULENCE  
LAMINAR FLOW

# DEVELOPMENT OF TURBULENCE IN TAILS

ISOTROPIC WIND



ANISOTROPIC WIND



HIGH LEVEL OF TURBULENCE  
CHAOTIC FLOW

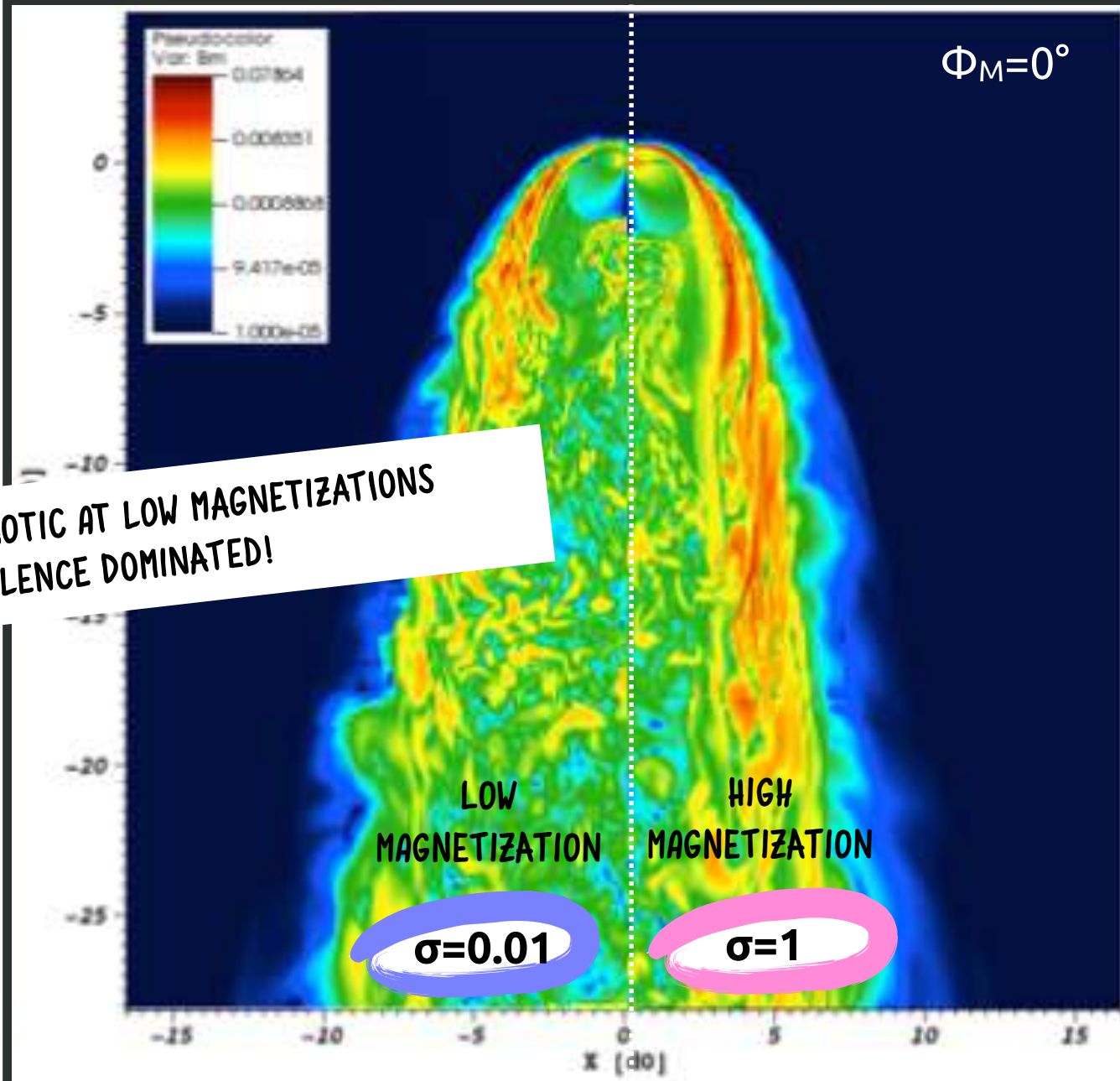
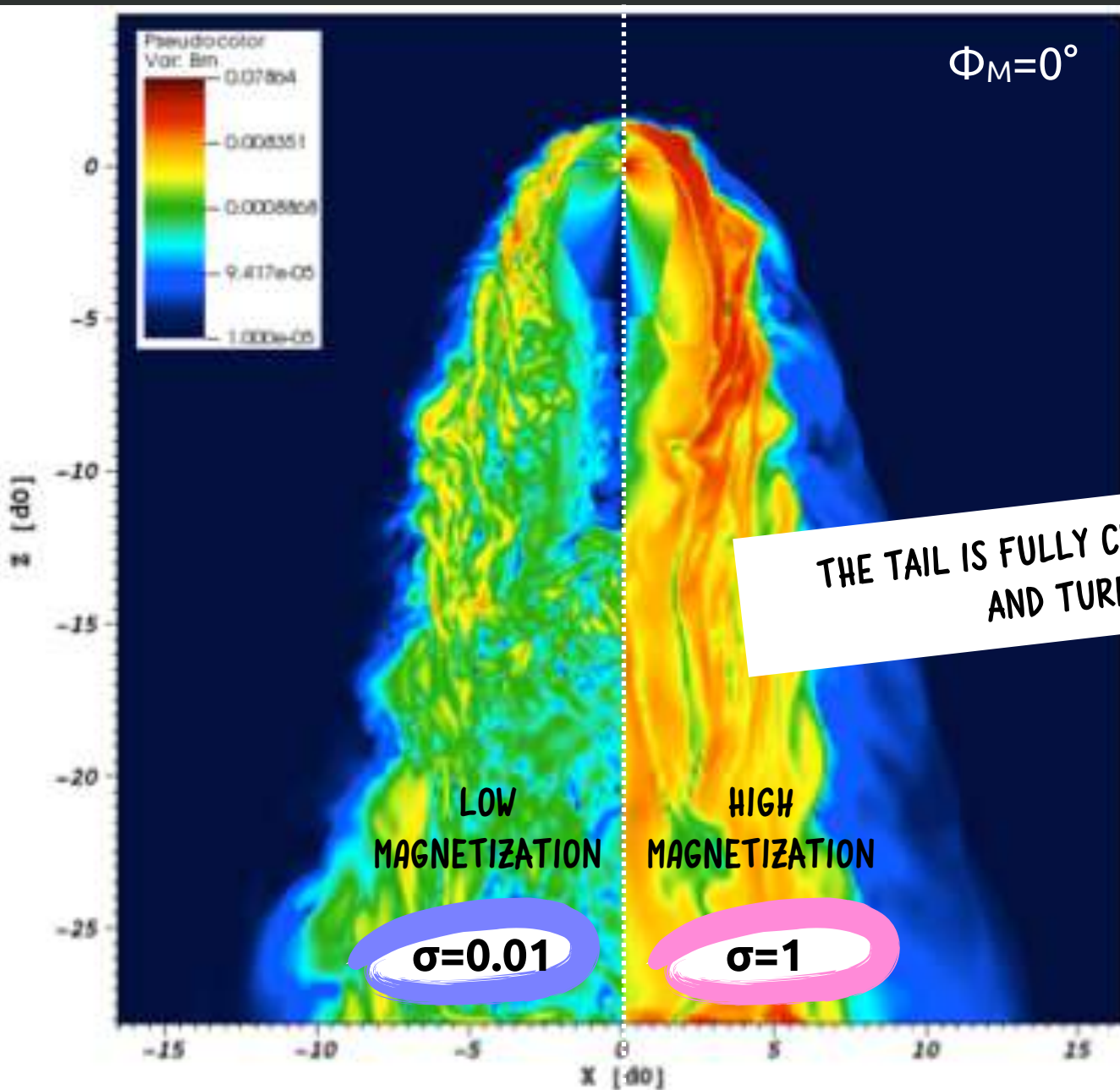
LOW LEVEL OF TURBULENCE  
LAMINAR FLOW

LESS MARKED DIFFERENCE IN ANISOTROPIC WINDS

# DEVELOPMENT OF TURBULENCE IN TAILS

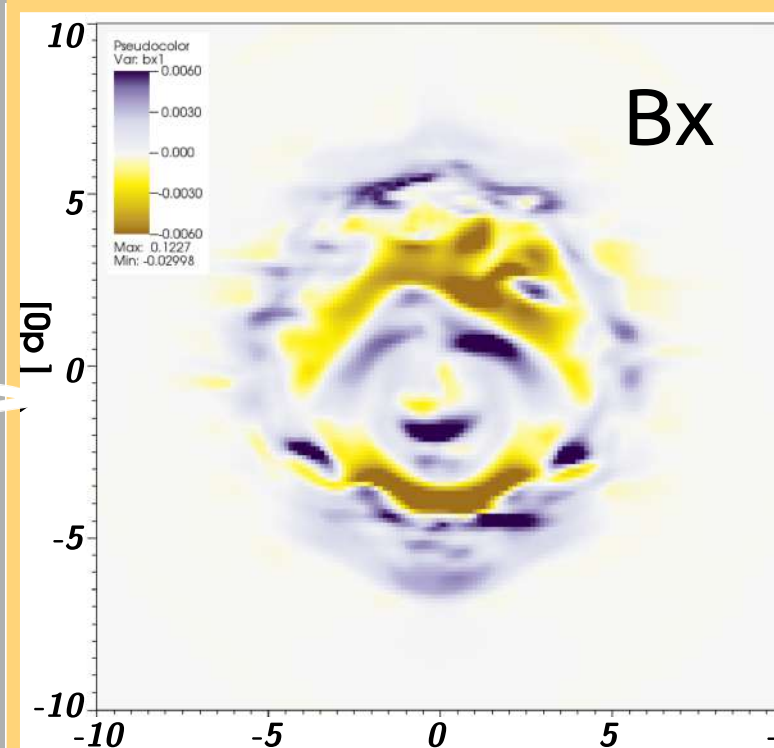
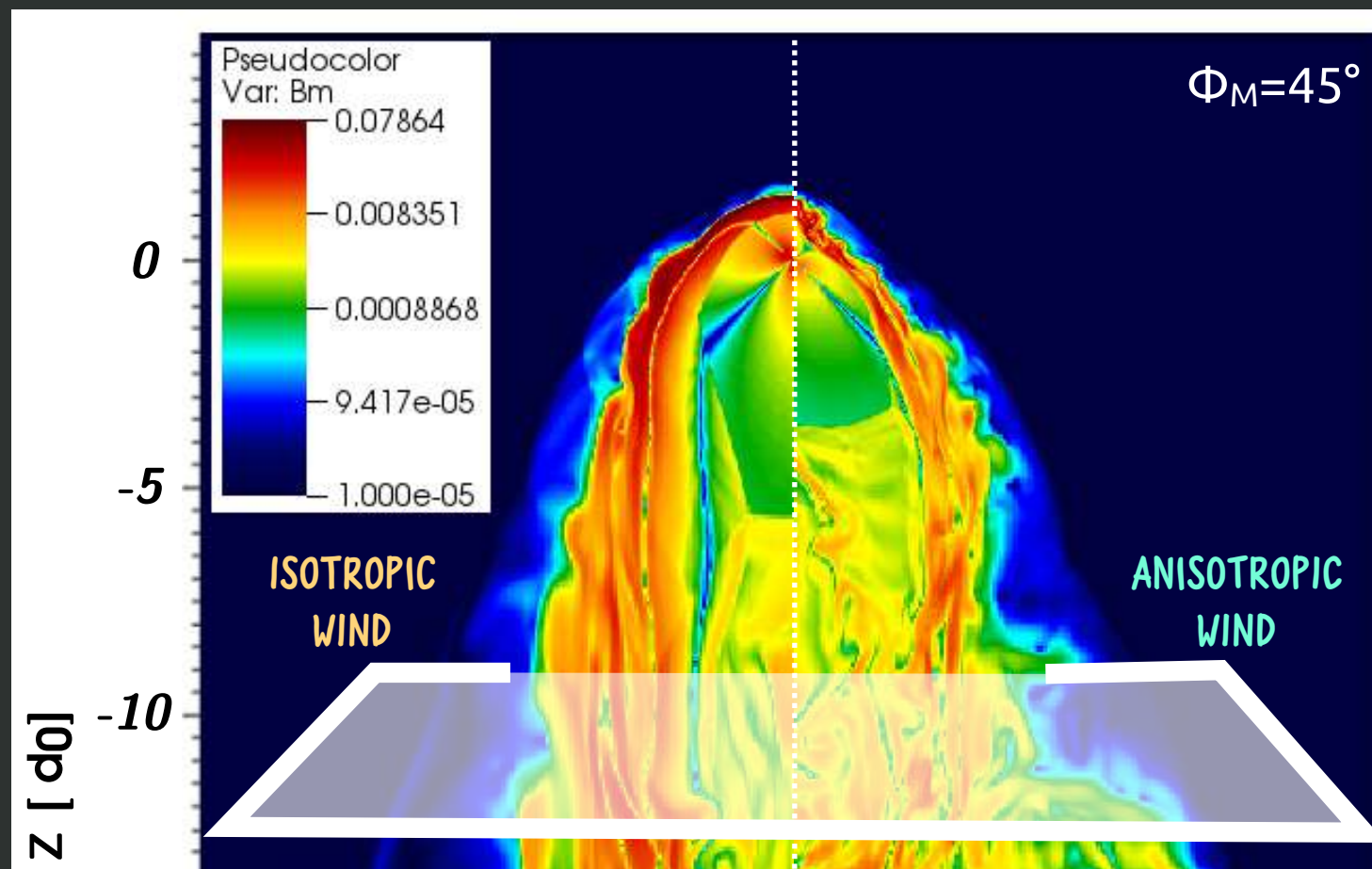
ISOTROPIC WIND

ANISOTROPIC WIND

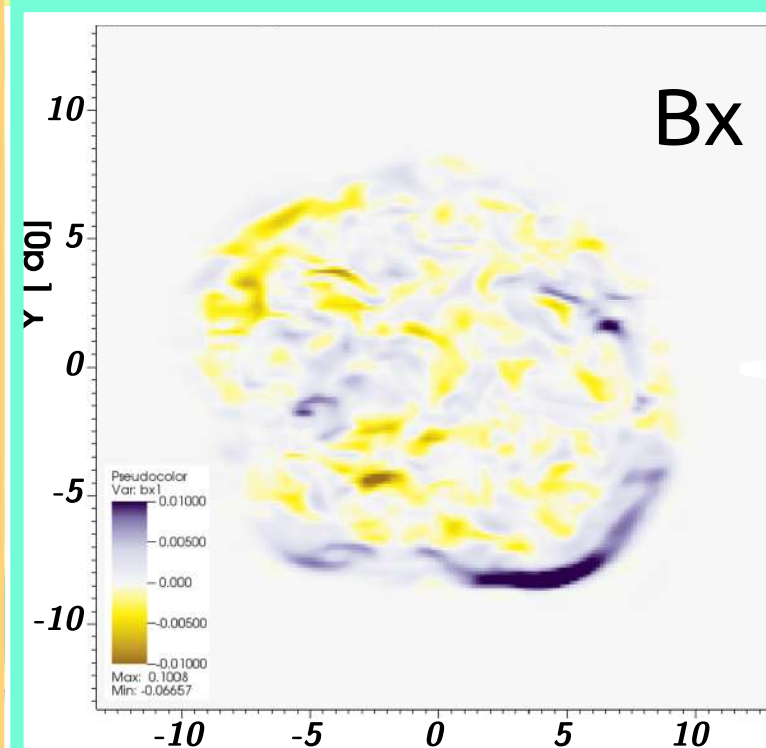


THE TAIL IS FULLY CHAOTIC AT LOW MAGNETIZATIONS AND TURBULENCE DOMINATED!

# TAIL DYNAMICS FOR HIGH MAGNETIZATION ( $\sigma=1$ )



DIFFERENT B  
POLARITIES  
MAINTAINED



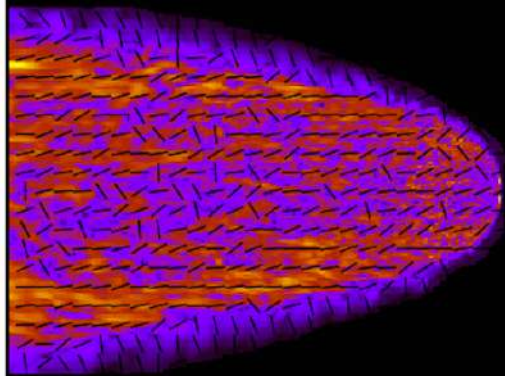
DIFFERENT B  
POLARITIES  
MIXED UP

$y$  [dn]

# CONSEQUENCES FOR EMISSION

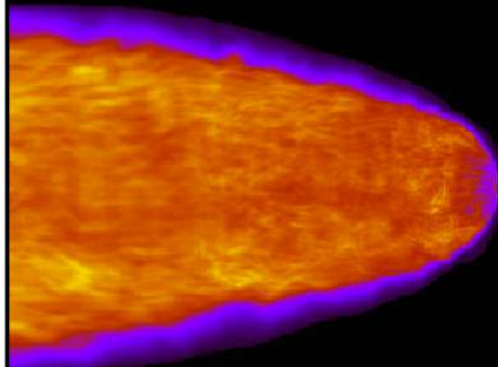
ANISOTROPIC  $\sigma=0.01$

polarization vector

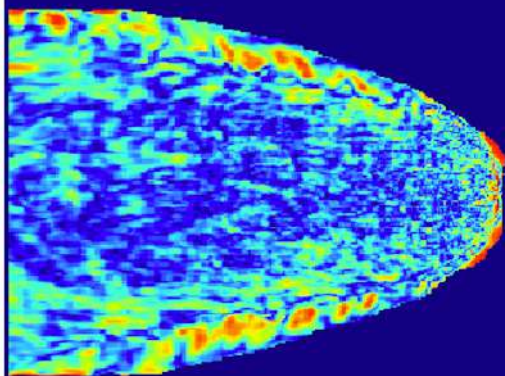


High level of  
turbulence

surface brightness



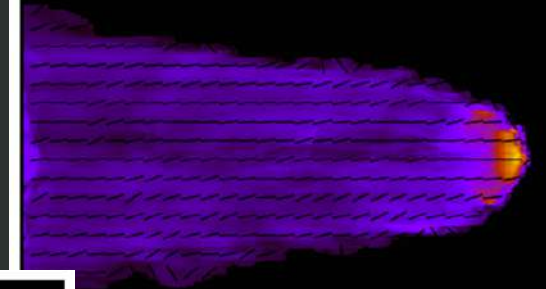
polarization level



Uniform emissivity.  
Unpolarized

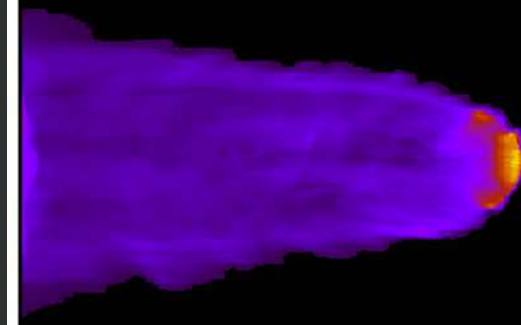
ISOTROPIC  $\sigma=1$

polarization vector

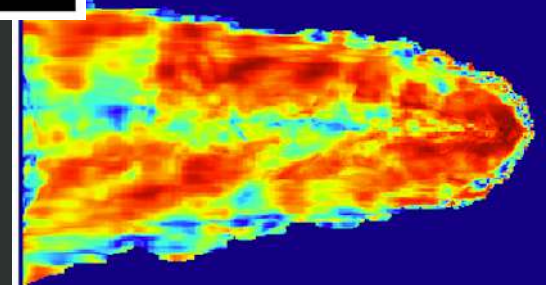


Low level of  
turbulence

surface brightness

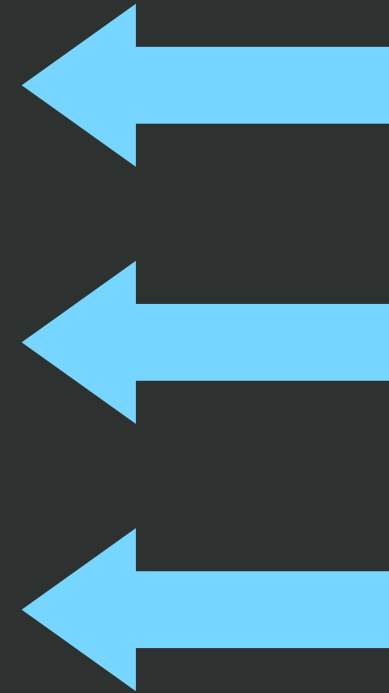
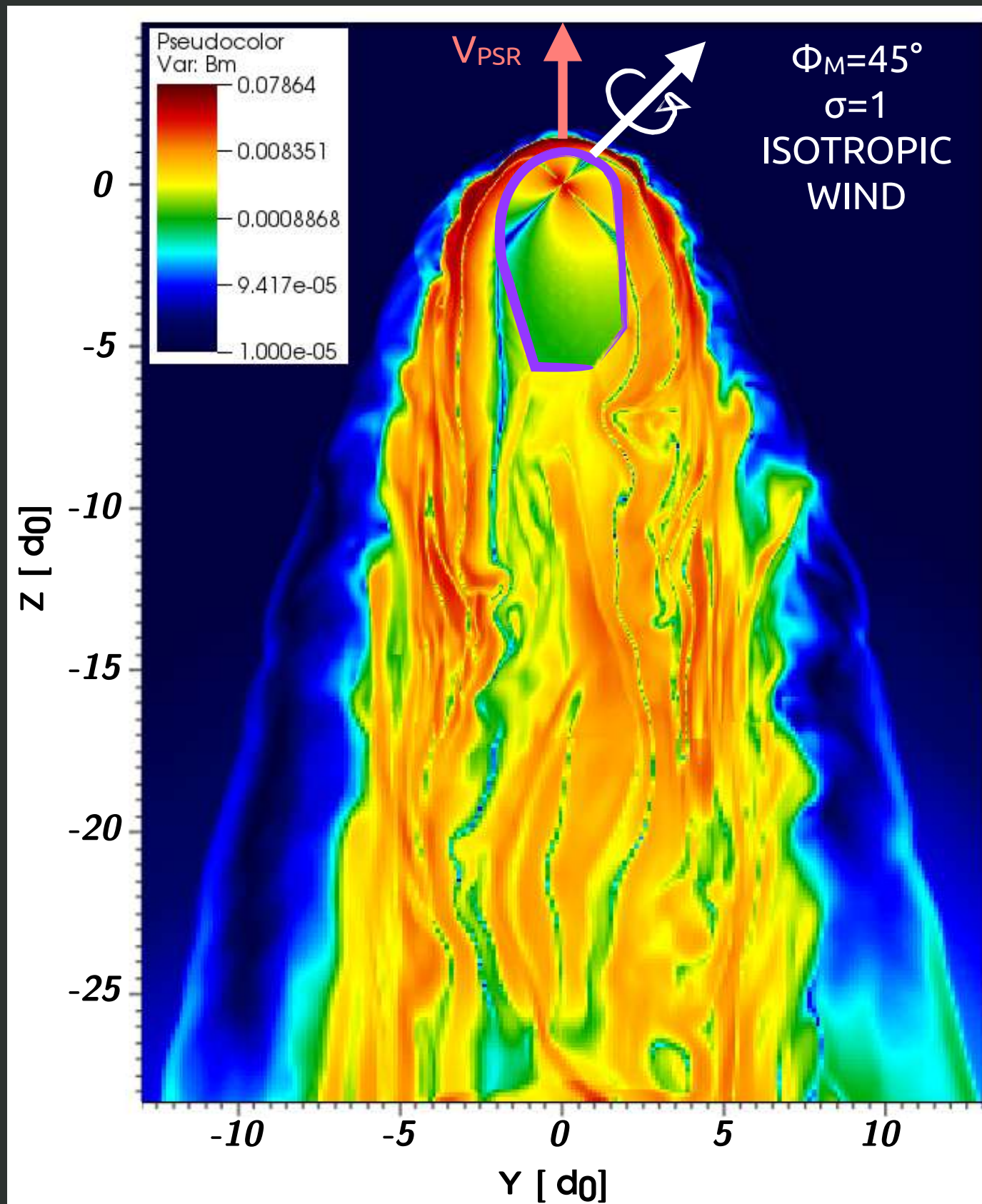


polarization level



Emission dominated  
by the head.  
Strong polarization.

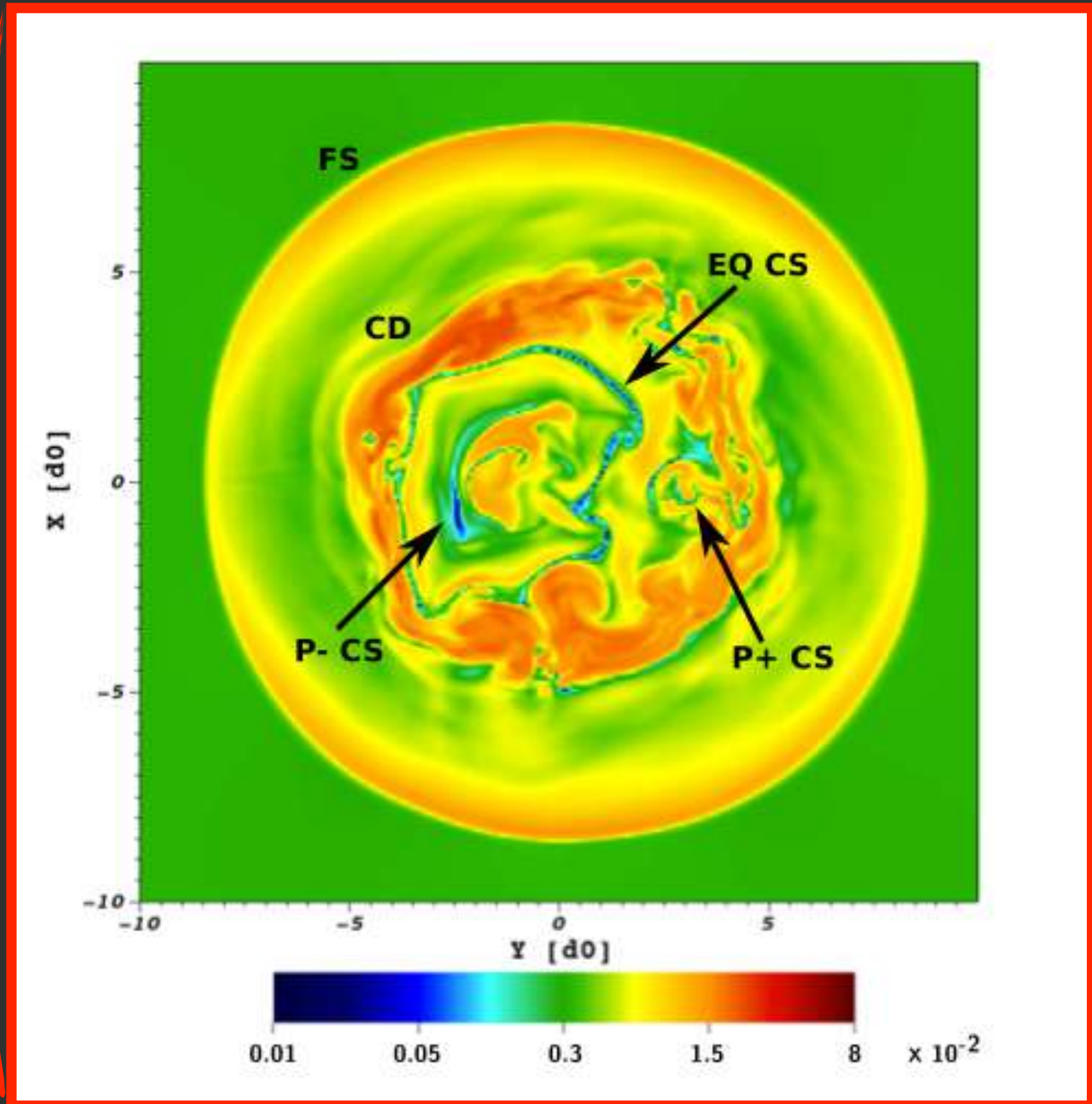
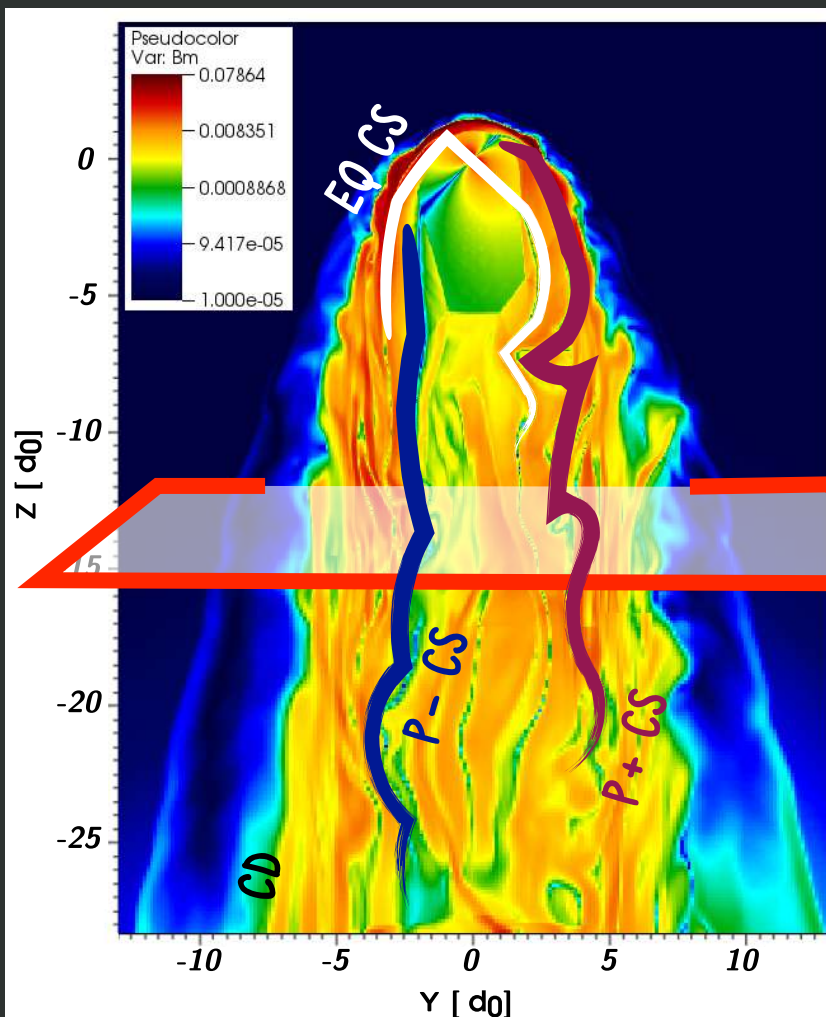
# EFFECTS OF OUTER MAGNETIC FIELD



$B_{ISM}$

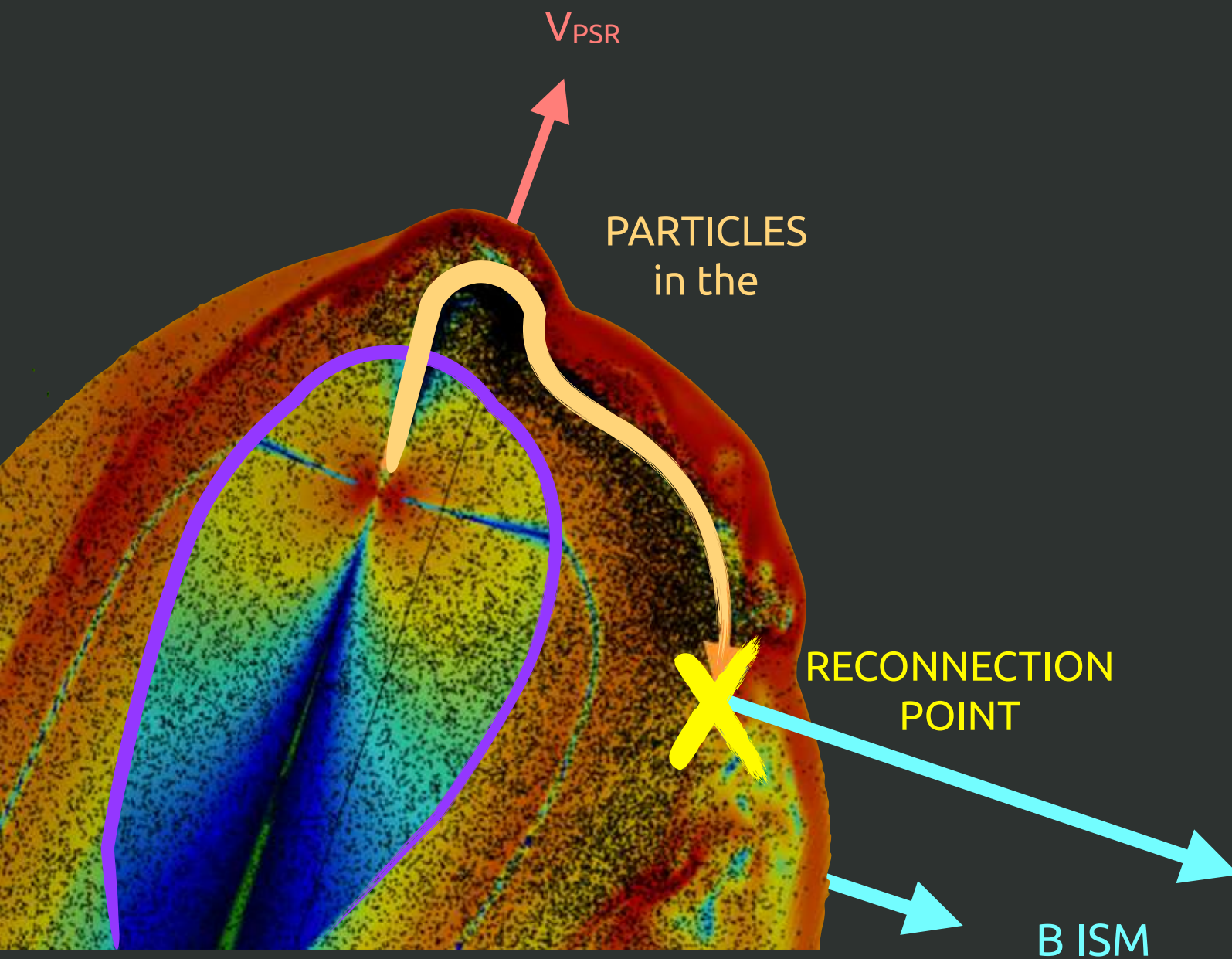
$$|B| = 0.01 \rho_{ISM} V_{PSR} \sim 3-5 \mu G$$

# SURVIVAL OF CURRENT SHEETS IN THE TAIL



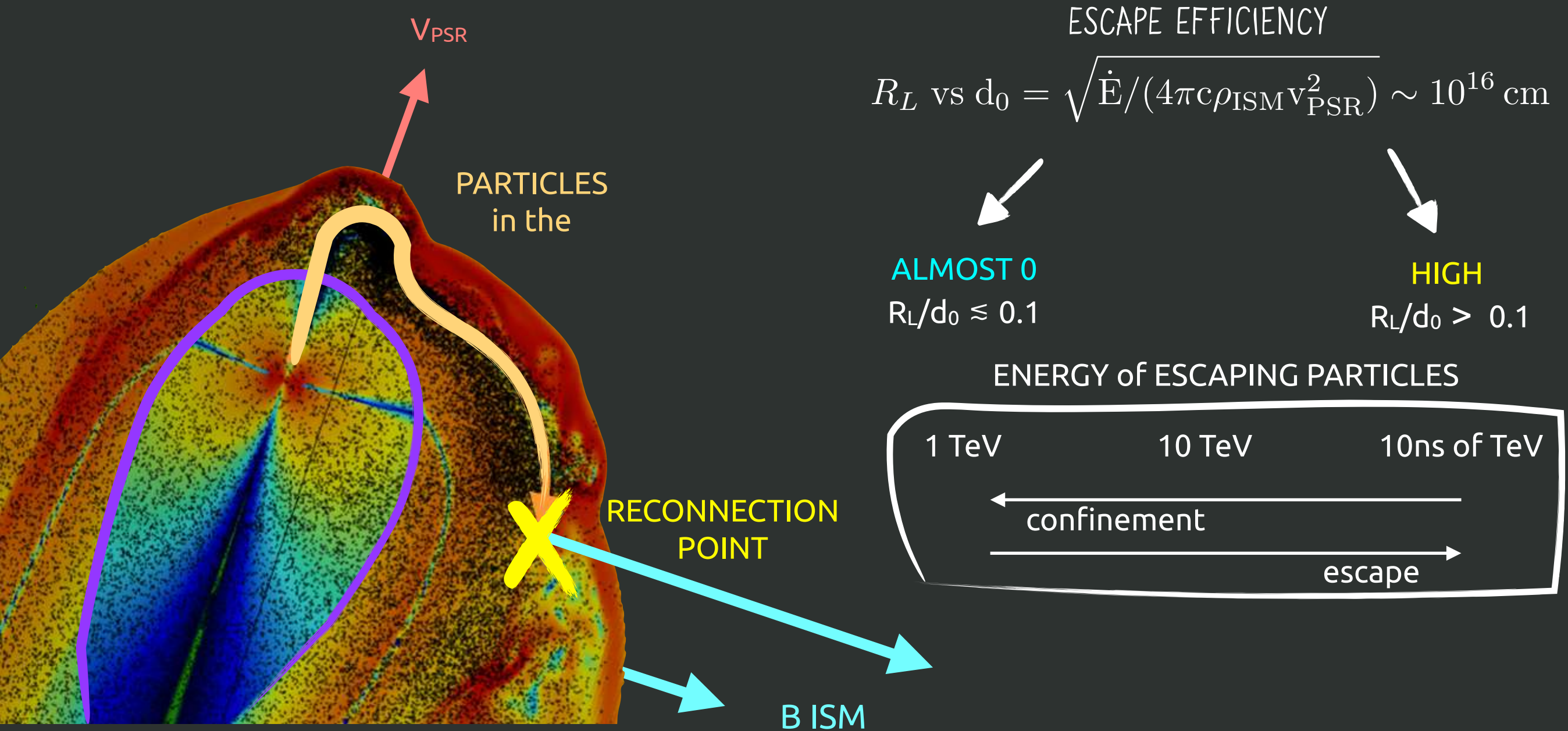
# PARTICLES LEACKAGE

Particles remain confined in current sheets: those injected in the polar flow can escape at reconnecting points at the magnetopause, efficiently jumping on external field lines.



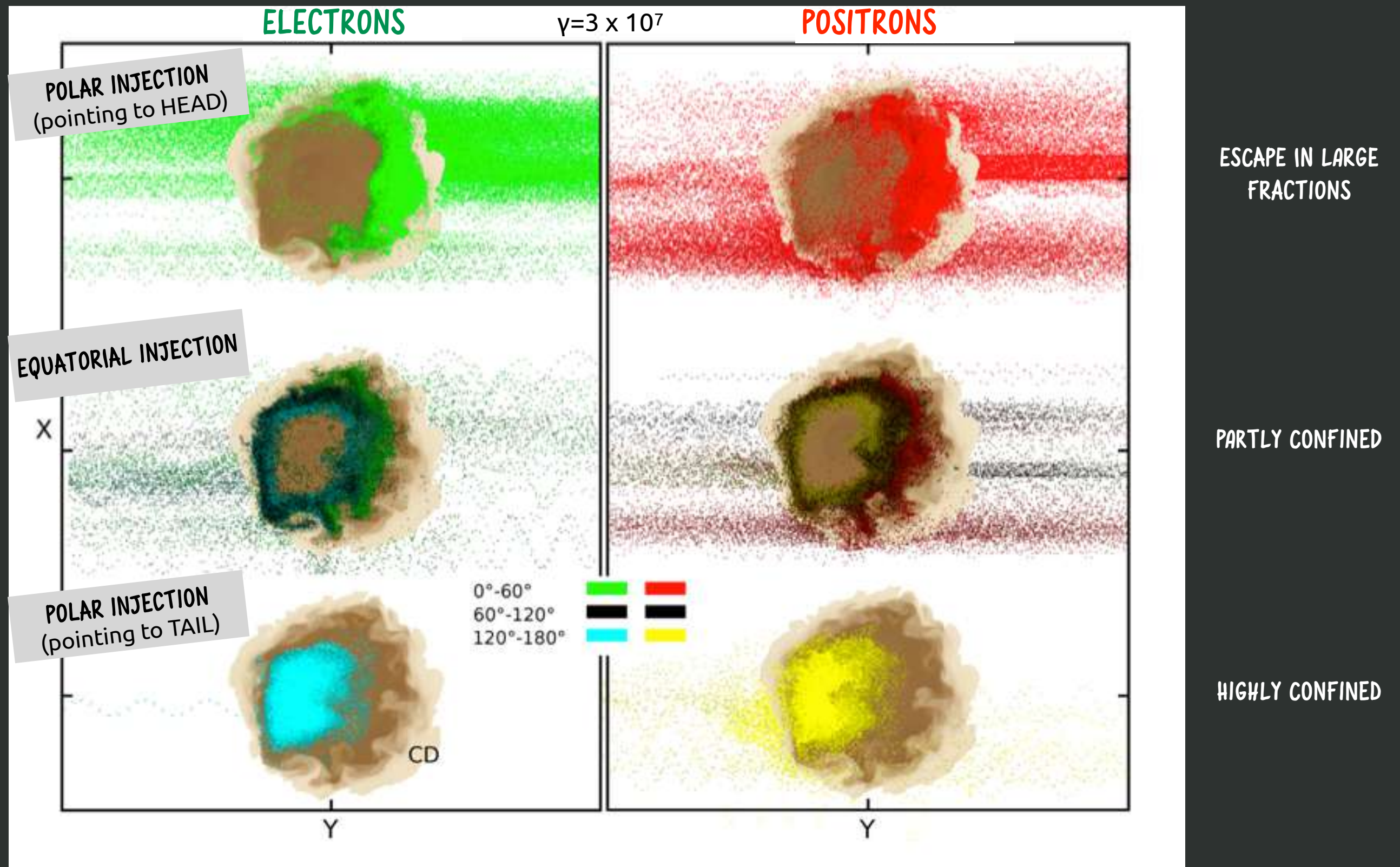
# PARTICLES LEAKAGE

Particles remain confined in current sheets: those injected in the polar flow can escape at reconnecting points at the magnetopause, efficiently jumping on external field lines.

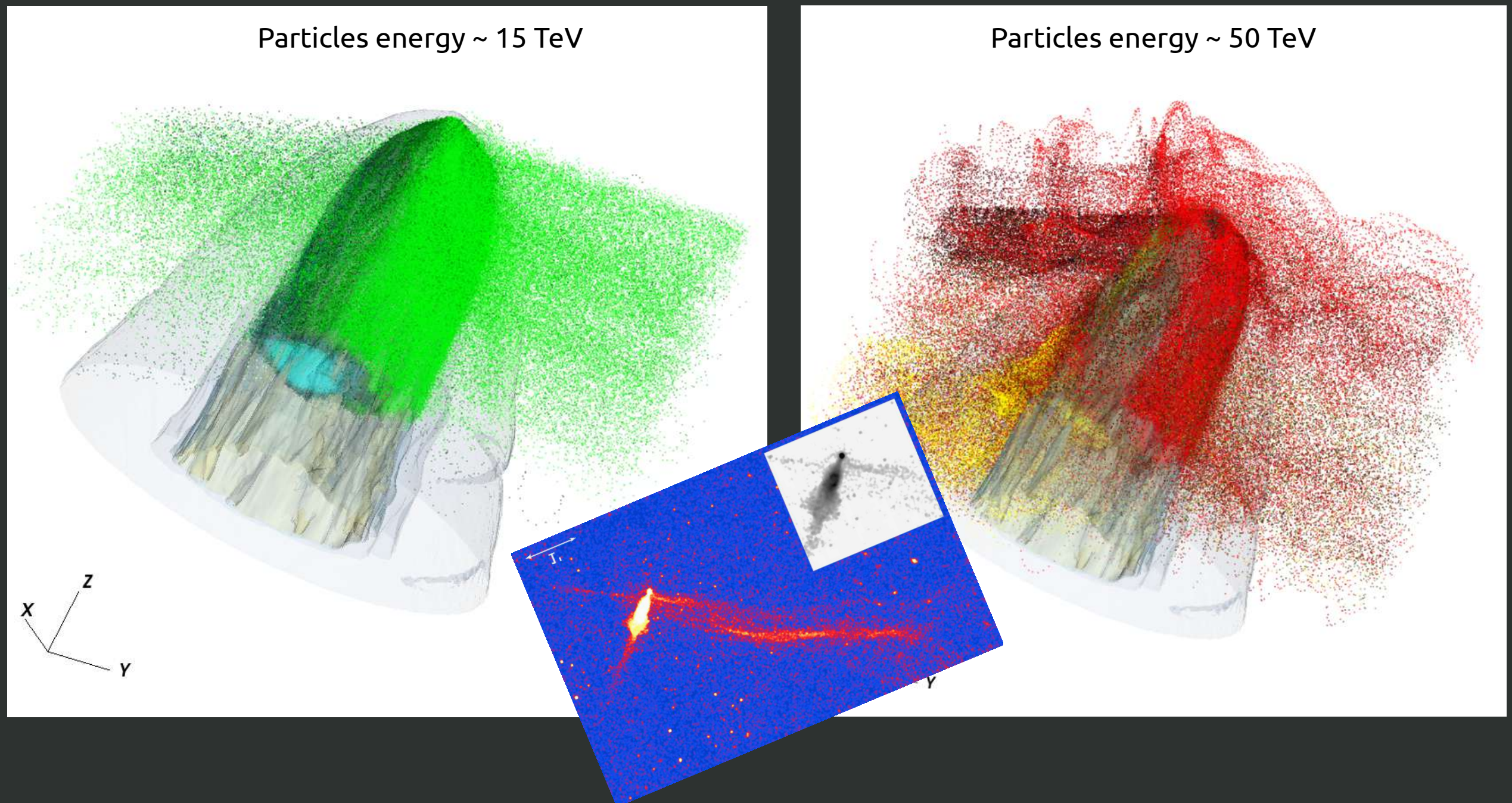


# PARTICLES LEAKAGE IS CHARGE DEPENDENT AND ASYMMETRIC

Particles escape as seen from tail:



# FORMATION OF JETS OR HALOS



Particles can efficiently escape from BSPWNe + escape is energy and charge dependent:

- sporadic escape of **LOW ENERGY** particles through reconnection points between PWN and ISM B field. Escape strongly asymmetric (depending on the system geometry). The charge asymmetry is small (~10%).
- **HIGH ENERGY** particles enter a **diffusive regime** when  $r_L \sim$  thickness of the current sheet. Now the escape flow is less asymmetric but strongly charge separated.

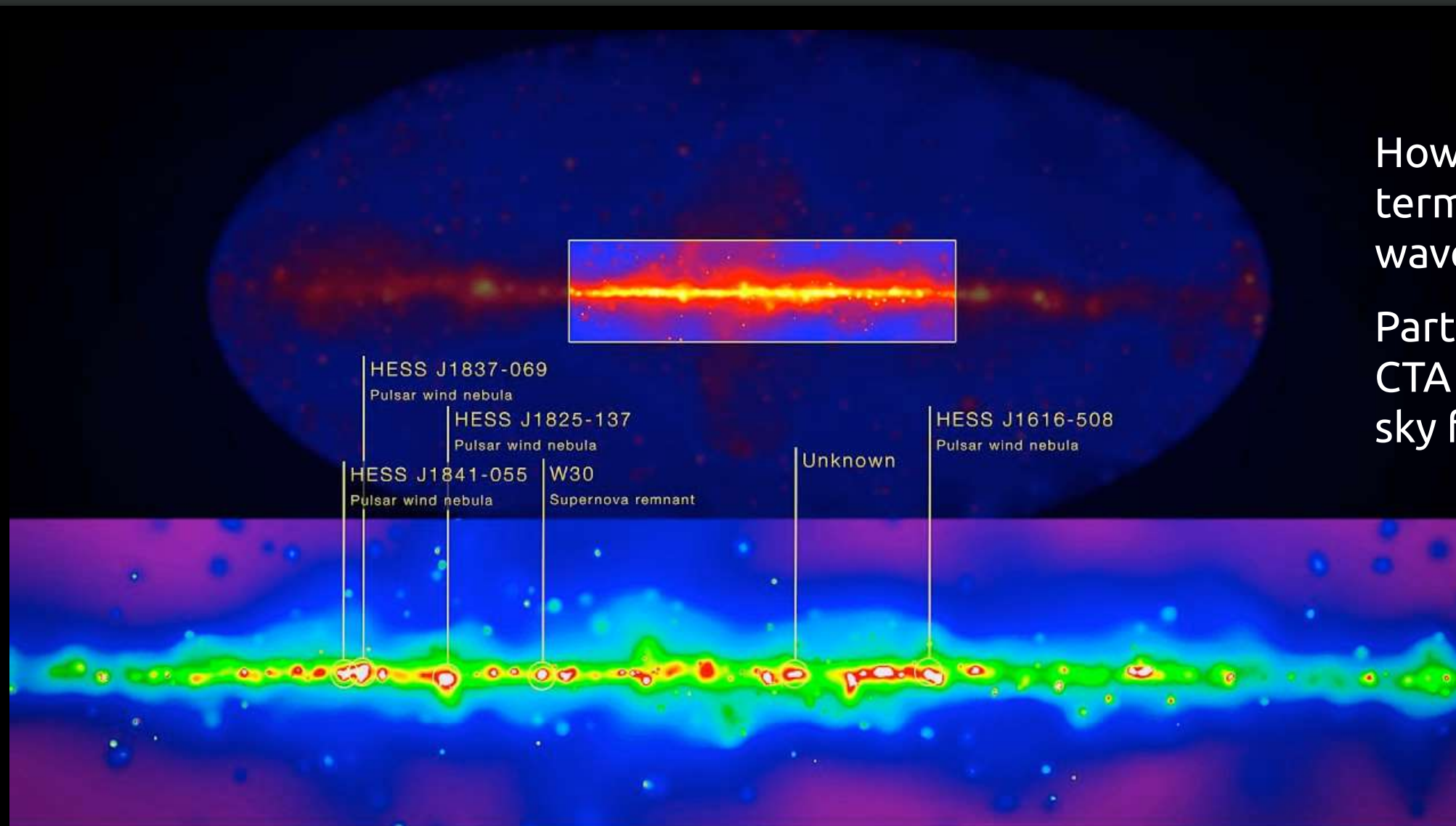
# CONCLUSIONS

MULTI-D MHD simulations have shown to be successful at accounting of many properties of PWNe, but:

Magnetic field can be realistically modeled ONLY in 3D ➡ Huge computational efforts

2D MHD simulations are less demanding ➡ Can realistically describe ONLY the inner nebula, but down to fine details

The very missed part: evolution of particles spectra together with dynamics



How could we model long term evolution + multi-wavelengths emission?

Particularly relevant with CTA coming -> Gamma ray sky full of PWNe!